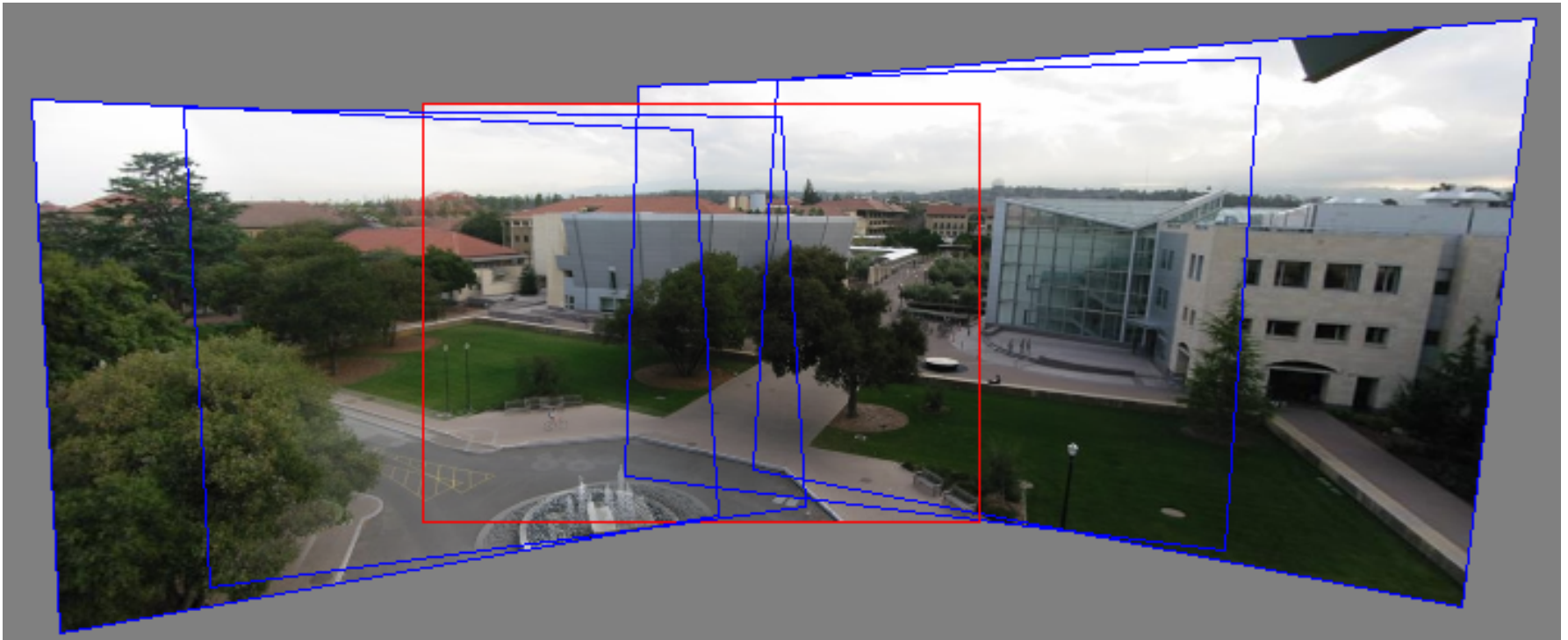
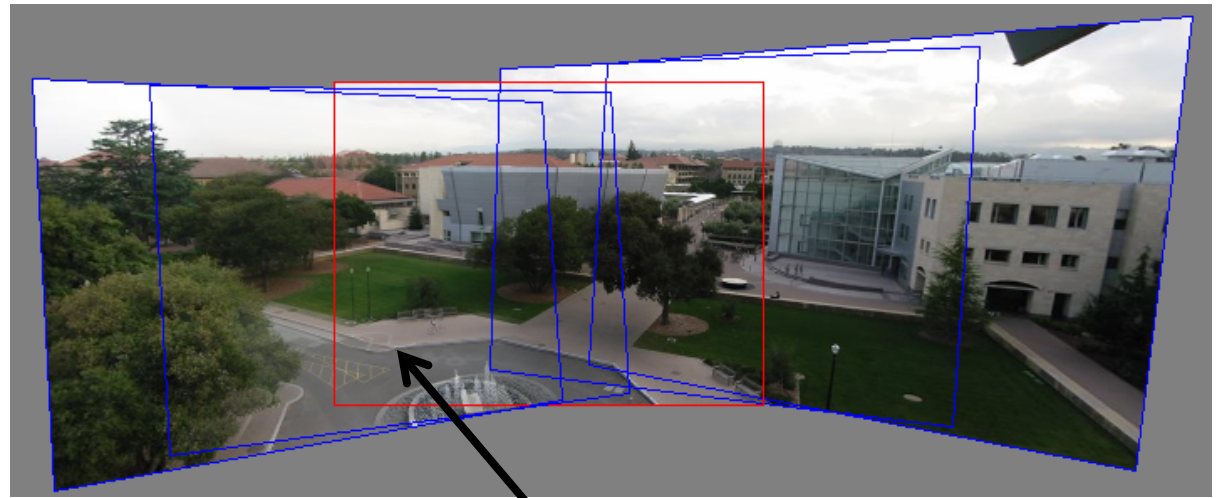
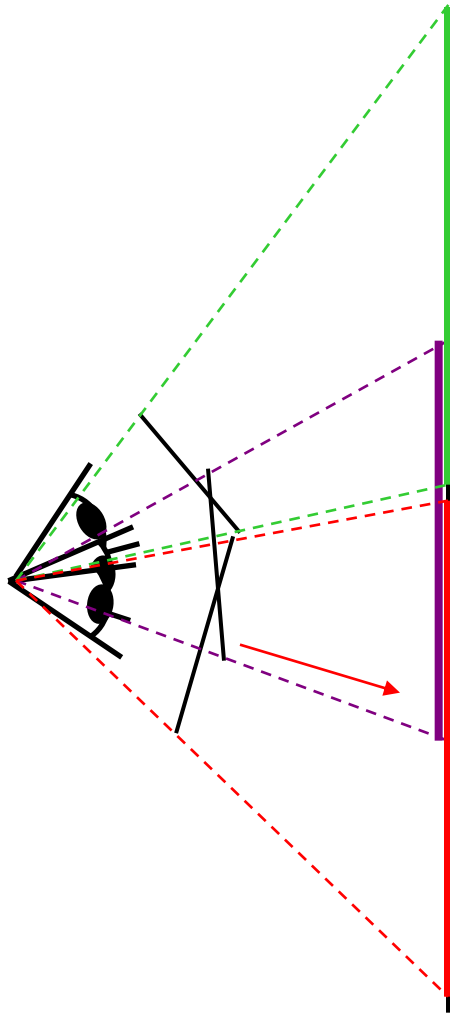


# Panoramas



We can't use homographies to create a 360 degree panorama.

# Homographies project images onto a common plane.



each image is warped  
with a homography  $\mathbf{H}$

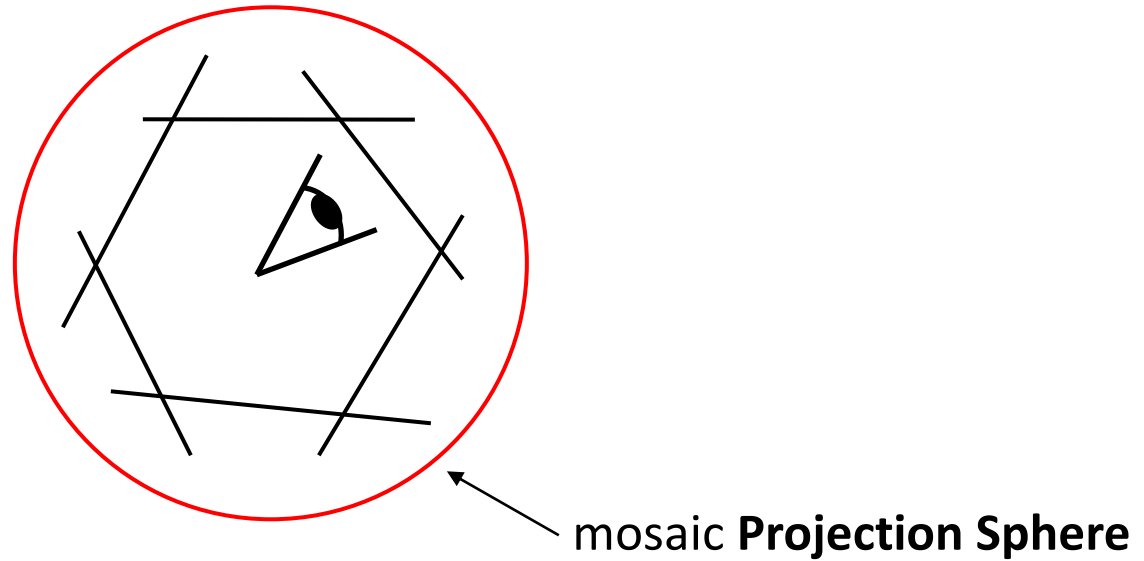
We'll see what this homography means in  
terms of cameras and projection later.

First -- Can't create a 360 panorama this way...

mosaic **Projection Plane**

# Panoramas

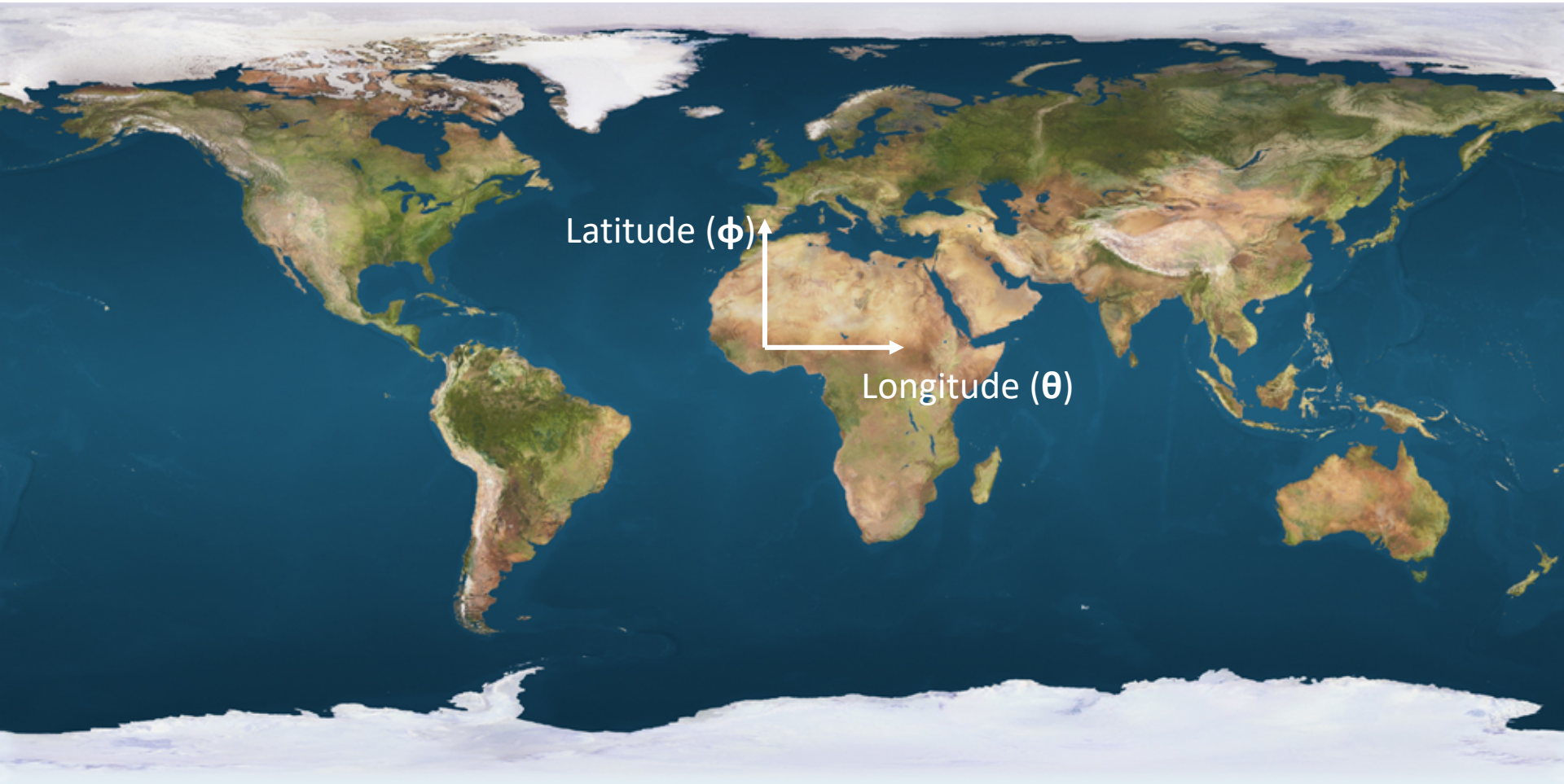
- What if you want a 360° field of view?





# Unwrapping a sphere

Credit: JHT's Planetary Pixel Emporium

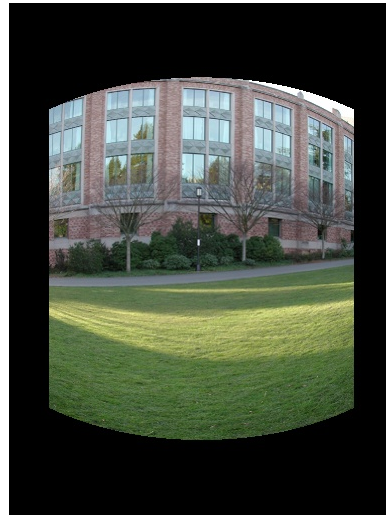




# Spherical reprojection



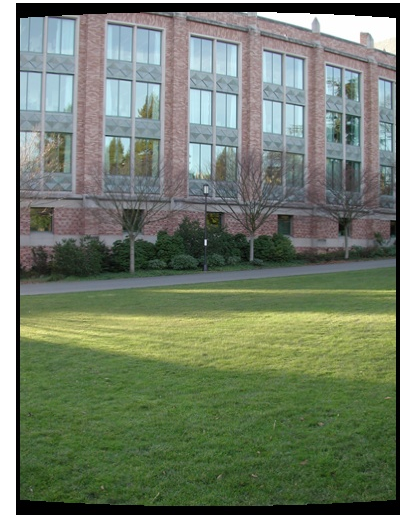
input



$f = 200$  (pixels)



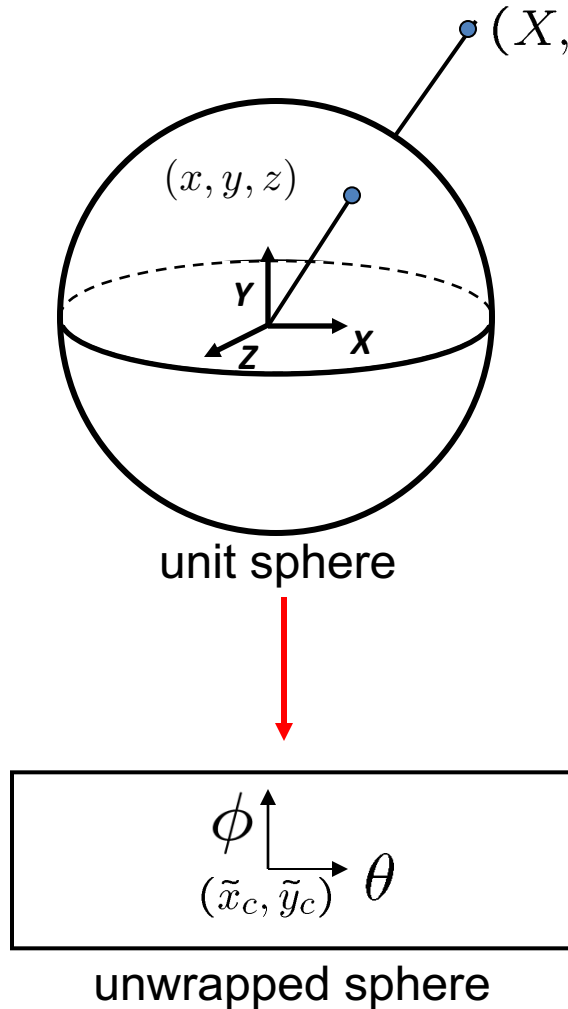
$f = 400$



$f = 800$

- Map image to spherical coordinates
  - need to know the focal length

# Spherical projection: Forward process



- Map 3D point  $(X, Y, Z)$  onto sphere

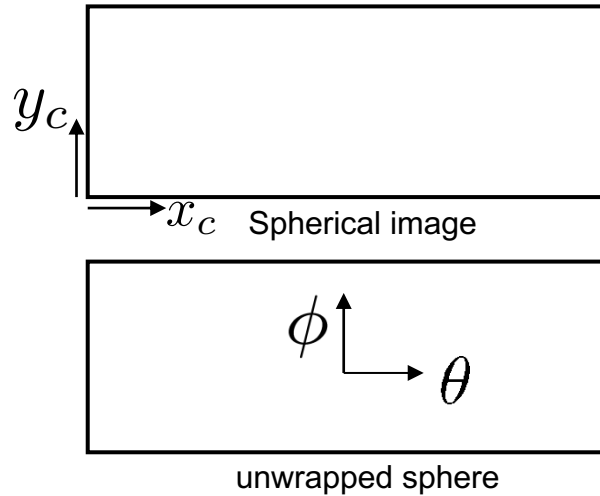
$$(\hat{x}, \hat{y}, \hat{z}) = \frac{1}{\sqrt{X^2 + Y^2 + Z^2}}(X, Y, Z)$$

- Convert to spherical coordinates
- Convert to spherical image coordinates

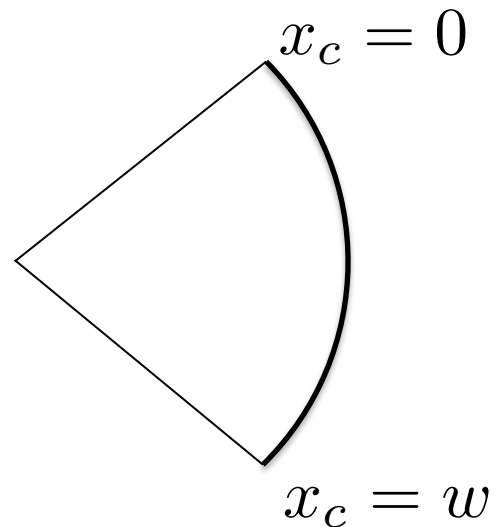
$$(\tilde{x}, \tilde{y}) = (s\theta, s\phi) + (\tilde{x}_c, \tilde{y}_c)$$

- $s$  defines size of the final image
  - » Usually set  $s = \text{camera focal length}$

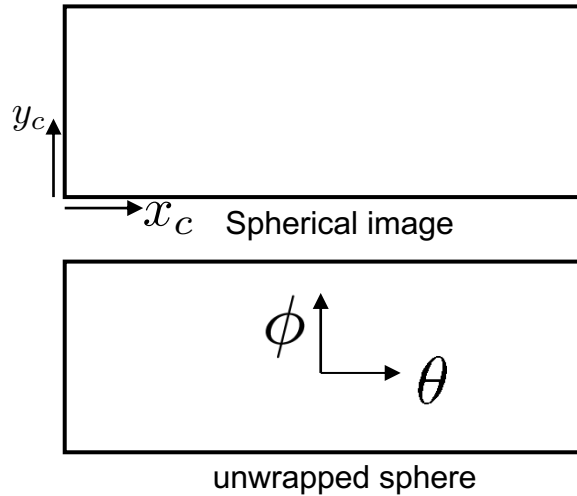
# Spherical projection: Inverse Process



- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:

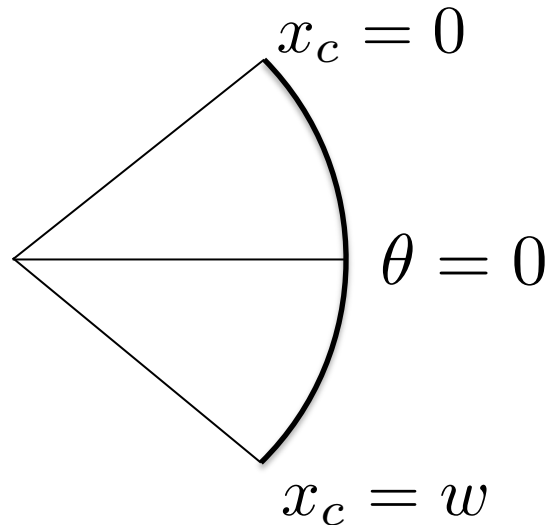


# Spherical projection: Inverse Process



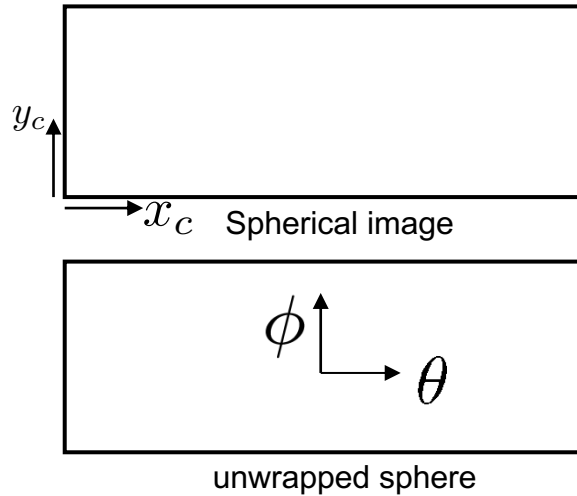
- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:

$$\theta = ??(x_c)$$



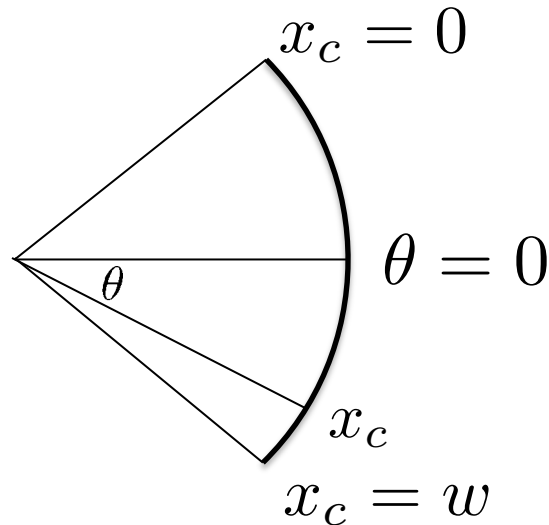


# Spherical projection: Inverse Process

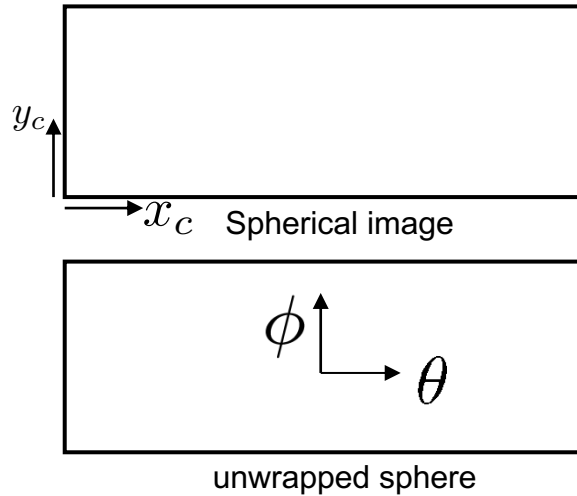


- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:

$$\theta = ??(x_c)$$

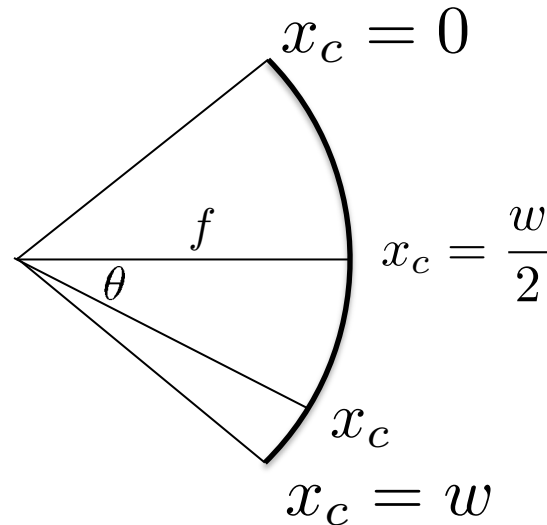


# Spherical projection: Inverse Process



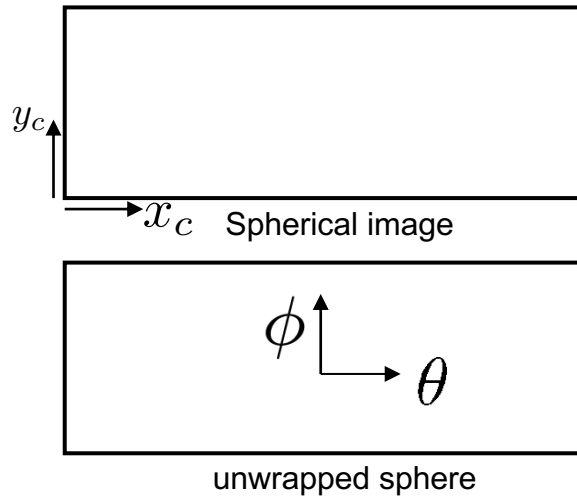
- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:

$$\theta = ??(x_c)$$

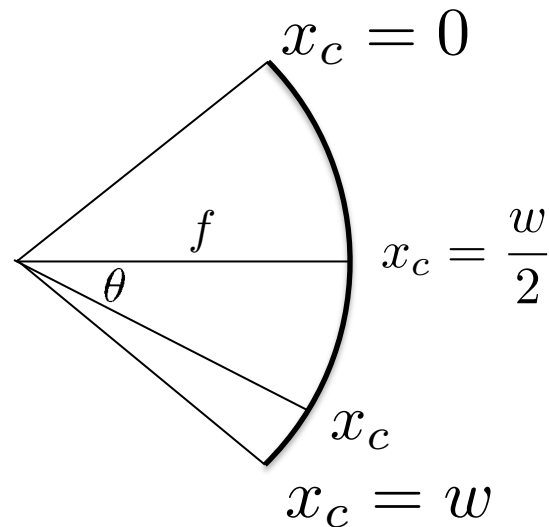


$$\frac{\text{angle}}{\text{circle}} \theta = \frac{\text{arc}}{\text{Circumf.}} \frac{x_c - \frac{w}{2}}{2\pi f}$$

# Spherical projection: Inverse Process



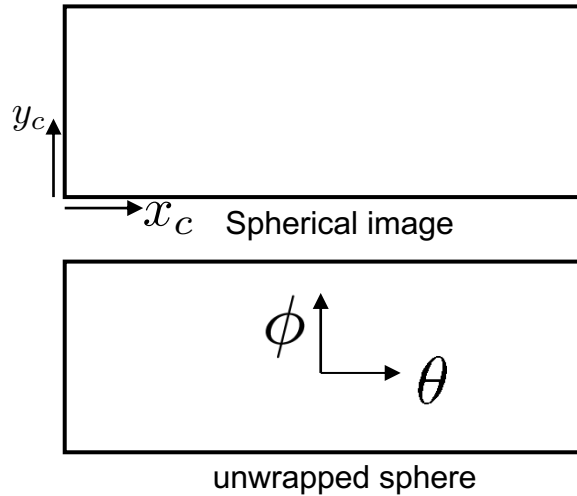
- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:



$$\frac{\theta}{2\pi} = \frac{x_c - \frac{w}{2}}{2\pi f}$$

$$\theta = \frac{1}{f} \left( x_c - \frac{w}{2} \right)$$

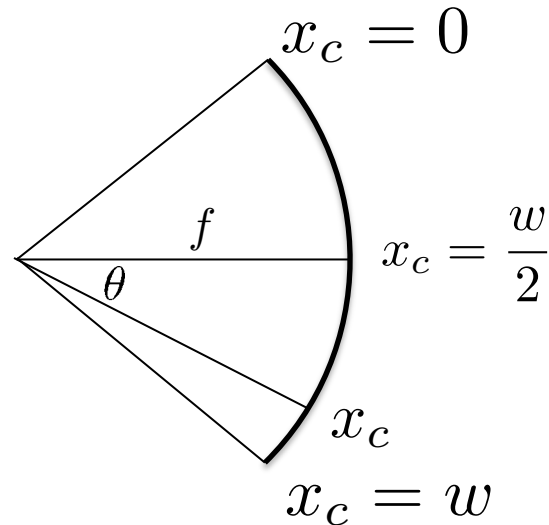
# Spherical projection: Inverse Process



- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:

$$\theta = \frac{1}{f} \left( x_c - \frac{w}{2} \right)$$

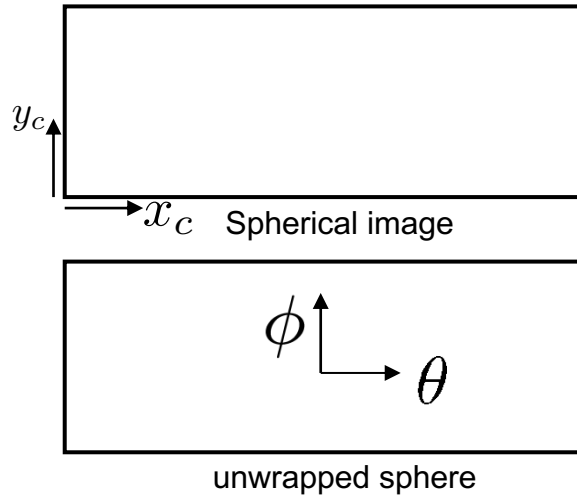
$$\phi = \frac{1}{f} \left( y_c - \frac{h}{2} \right)$$



$$\frac{\theta}{2\pi} = \frac{x_c - \frac{w}{2}}{2\pi f}$$

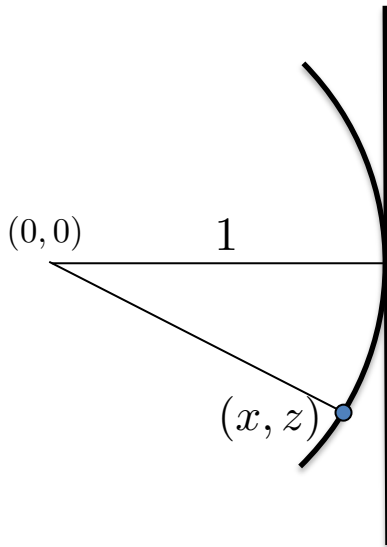
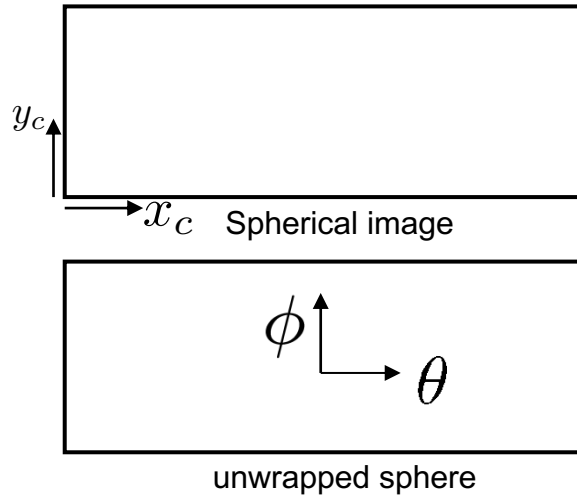
$$\theta = \frac{1}{f} \left( x_c - \frac{w}{2} \right)$$

# Spherical projection: Inverse Process



- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with (0,0) at center of image:  
$$\theta = \frac{1}{f}(x_c - \frac{w}{2})$$
$$\phi = \frac{1}{f}(y_c - \frac{h}{2})$$
- Convert angles to (x,y,z) coordinates on a unit sphere:  
$$x = \sin \theta \cos \phi$$
$$y = \sin \phi$$
$$z = \cos \theta \cos \phi$$

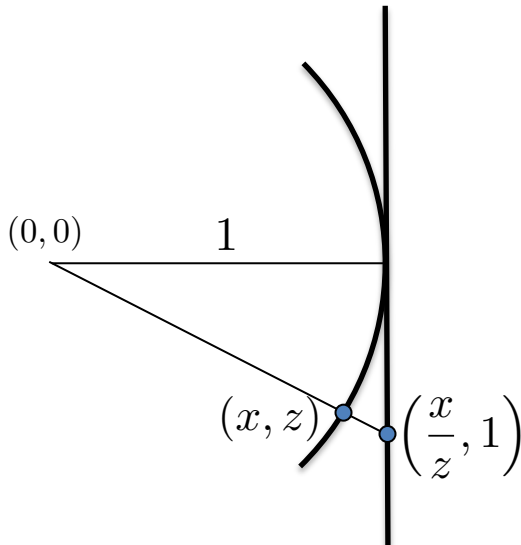
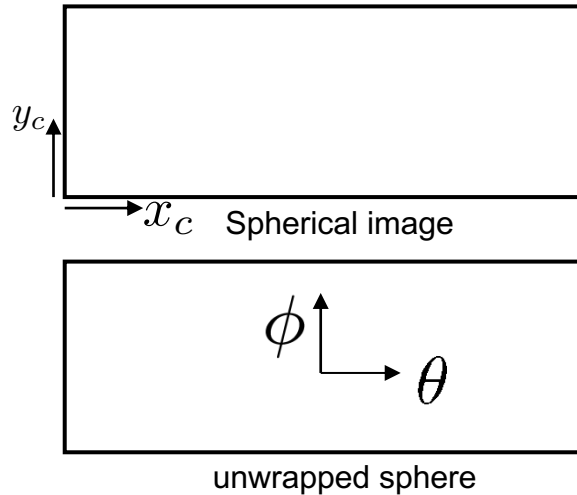
# Spherical projection: Inverse Process



- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:  
$$\theta = \frac{1}{f}(x_c - \frac{w}{2})$$
$$\phi = \frac{1}{f}(y_c - \frac{h}{2})$$
- Convert angles to  $(x,y,z)$  coordinates on a unit sphere:  
$$x = \sin \theta \cos \phi$$
$$y = \sin \phi$$
$$z = \cos \theta \cos \phi$$
- Project  $(x,y,z)$  coordinates onto the image plane at  $Z=1$  by dividing by  $z$ :



# Spherical projection: Inverse Process



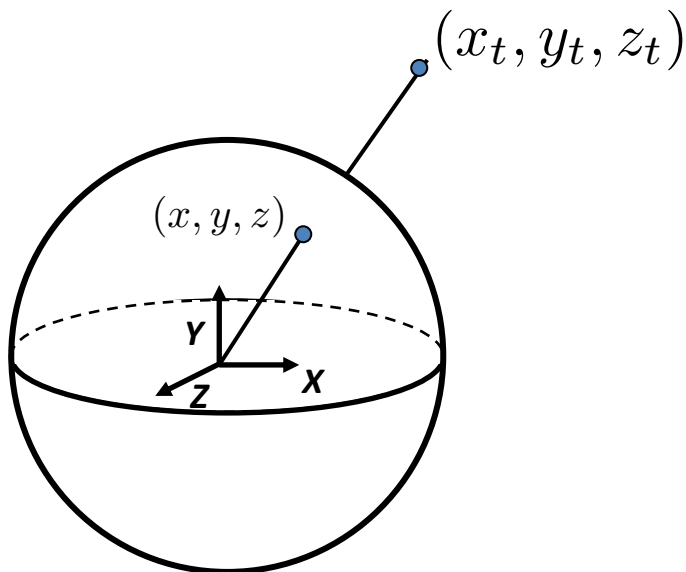
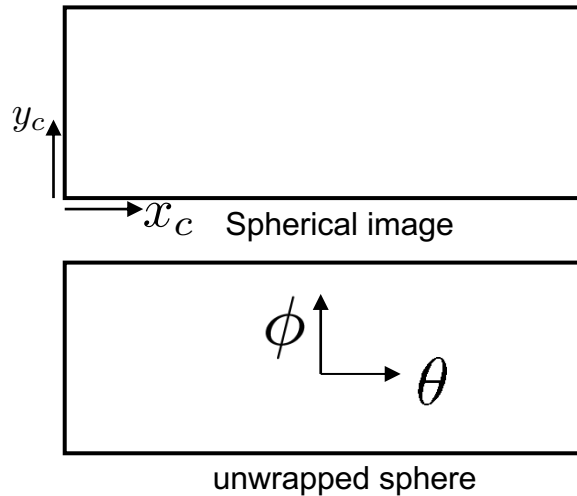
- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:
 
$$\theta = \frac{1}{f}(x_c - \frac{w}{2})$$

$$\phi = \frac{1}{f}(y_c - \frac{h}{2})$$
- Convert angles to  $(x,y,z)$  coordinates on a unit sphere:
 
$$x = \sin \theta \cos \phi$$

$$y = \sin \phi$$

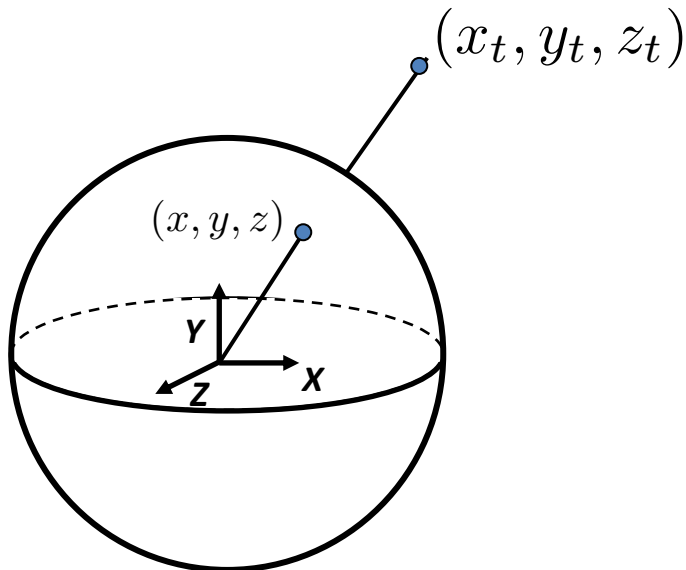
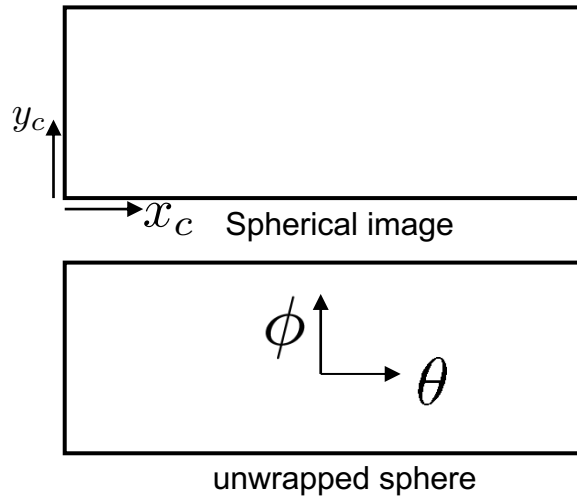
$$z = \cos \theta \cos \phi$$
- Project  $(x,y,z)$  coordinates onto the image plane at  $Z=1$  by dividing by  $z$ :
 
$$(x_t, y_t, z_t) = \left( \frac{x}{z}, \frac{y}{z}, 1 \right)$$

# Spherical projection: Inverse Process



- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:  
$$\theta = \frac{1}{f}(x_c - \frac{w}{2})$$
$$\phi = \frac{1}{f}(y_c - \frac{h}{2})$$
- Convert angles to  $(x,y,z)$  coordinates on a unit sphere:  
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- Project  $(x,y,z)$  coordinates onto the image plane at  $Z=1$  by dividing by  $z$ :  
$$(x_t, y_t, z_t) = \left( \frac{x}{z}, \frac{y}{z}, 1 \right)$$

# Spherical projection: Inverse Process



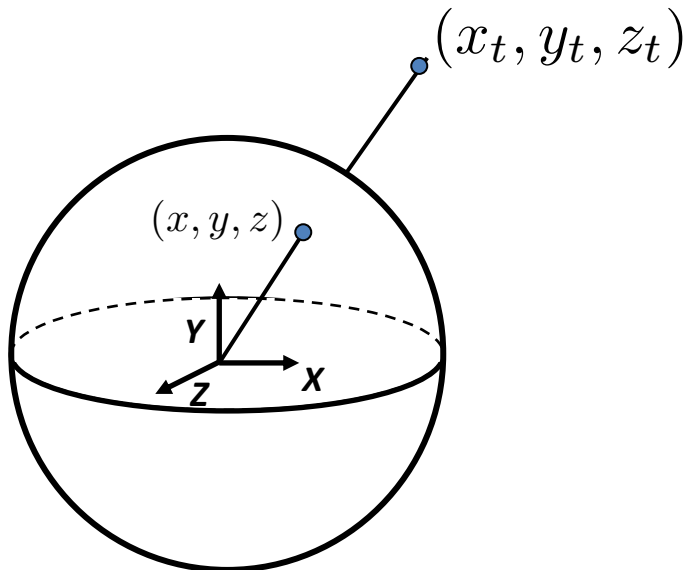
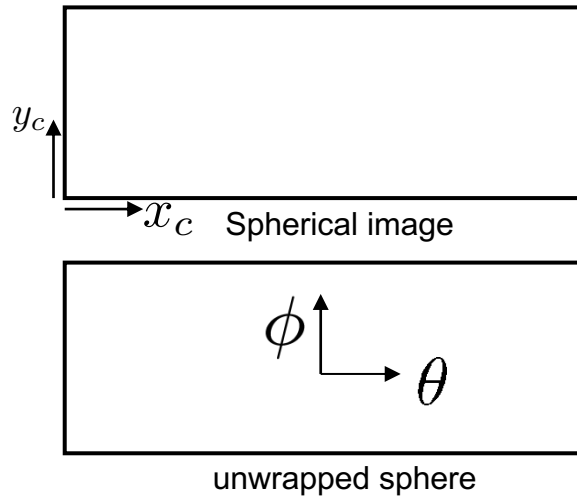
- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:
 
$$\theta = \frac{1}{f}(x_c - \frac{w}{2})$$

$$\phi = \frac{1}{f}(y_c - \frac{h}{2})$$
- Convert angles to  $(x,y,z)$  coordinates on a unit sphere:
 
$$x = \sin \theta \cos \phi$$

$$y = \sin \theta \sin \phi$$

$$z = \cos \theta \cos \phi$$
- Project  $(x,y,z)$  coordinates onto the image plane at  $Z=1$  by dividing by  $z$ :
 
$$(x_t, y_t, z_t) = \left( \frac{x}{z}, \frac{y}{z}, 1 \right)$$
- Convert from image plane to original pixel coordinates:

# Spherical projection: Inverse Process



- Begin with spherical image coordinates  $(x_c, y_c)$
- Convert to angles with  $(0,0)$  at center of image:
 
$$\theta = \frac{1}{f}(x_c - \frac{w}{2})$$

$$\phi = \frac{1}{f}(y_c - \frac{h}{2})$$
- Convert angles to  $(x,y,z)$  coordinates on a unit sphere:
 
$$x = \sin \theta \cos \phi$$

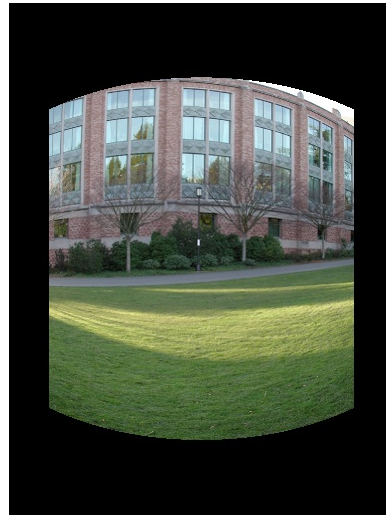
$$y = \sin \phi$$

$$z = \cos \theta \cos \phi$$
- Project  $(x,y,z)$  coordinates onto the image plane at  $Z=1$  by dividing by  $z$ :
 
$$(x_t, y_t, z_t) = \left( \frac{x}{z}, \frac{y}{z}, 1 \right)$$
- Convert from image plane to original pixel coordinates:
 
$$x_n = \frac{w}{2} + f * x_t \quad y_n = \frac{h}{2} + f * y_t$$

# Spherical reprojection



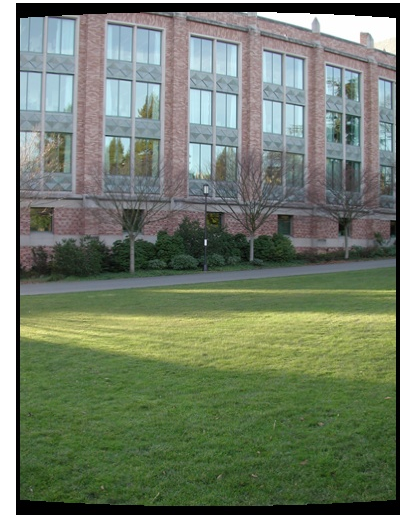
input



$f = 200$  (pixels)



$f = 400$



$f = 800$

- Map image to spherical coordinates
  - need to know the focal length

# Aligning spherical images

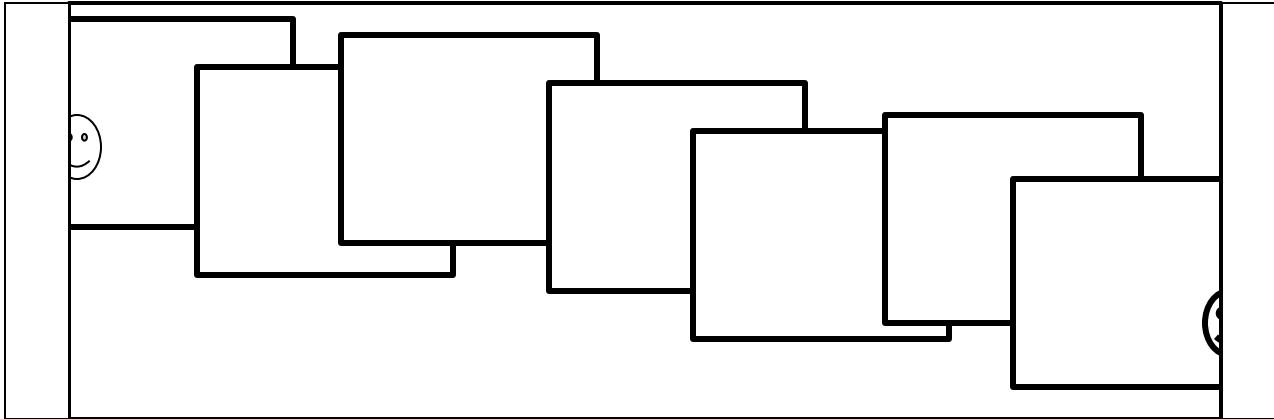


- Suppose we rotate the camera by  $\theta$  about the vertical axis
  - How does this change the spherical image?



# Problem: Drift

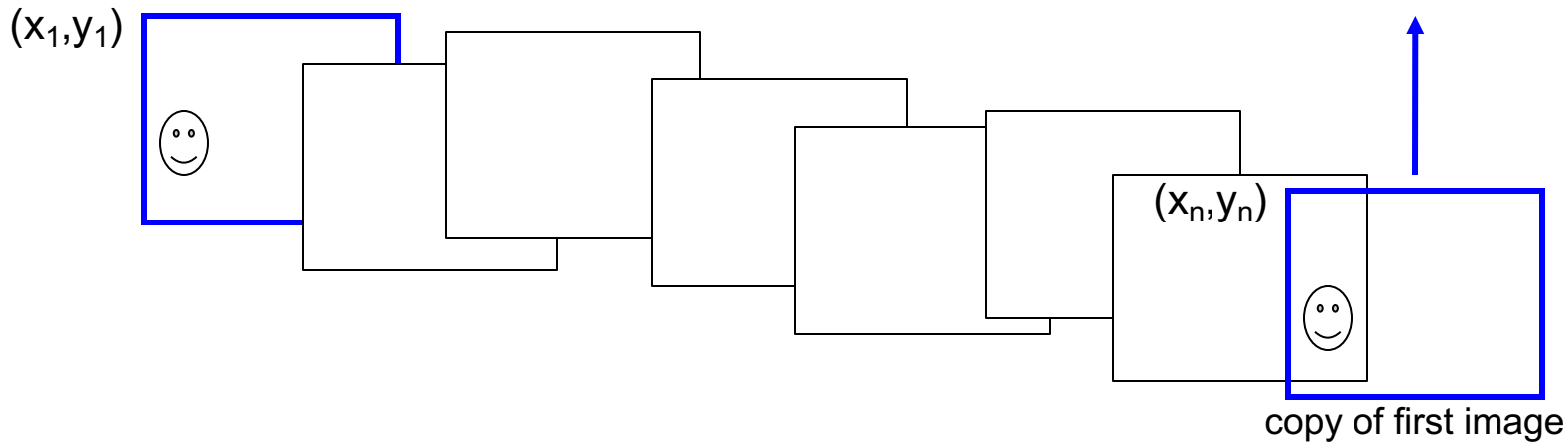
---



- Error accumulation
  - small errors accumulate over time

# Problem: Drift

---



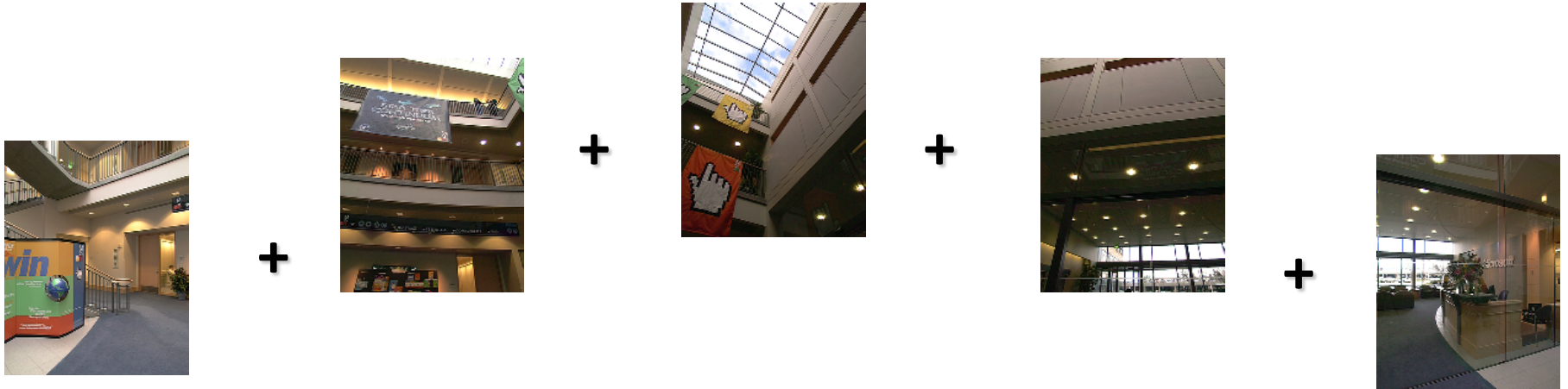
- Solution

- add another copy of first image at the end
- this gives a constraint:  $y_n = y_1$
- there are a bunch of ways to solve this problem
  - add displacement of  $(y_1 - y_n)/(n - 1)$  to each image after the first
  - **apply an affine warp:  $y' = y + ax$  [you will implement this for P3]**
  - run a big optimization problem, incorporating this constraint
    - best solution, but more complicated
    - known as “bundle adjustment”

# Project 3

- Take pictures on a tripod (or handheld)
- Warp to spherical coordinates (optional if using homographies to align images)
- Extract features
- Align neighboring pairs using RANSAC
- Write out list of neighboring translations
- Correct for drift
- Read in warped images and blend them
- Crop the result and import into a viewer
  
- Roughly based on Autostitch
  - By Matthew Brown and David Lowe
  - <http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html>

# Spherical panoramas



Microsoft Lobby: <http://www.acm.org/pubs/citations/proceedings/graph/258734/p251-szeliski>

# Different projections are possible



Cube-map



# Blending

- We've aligned the images – now what?



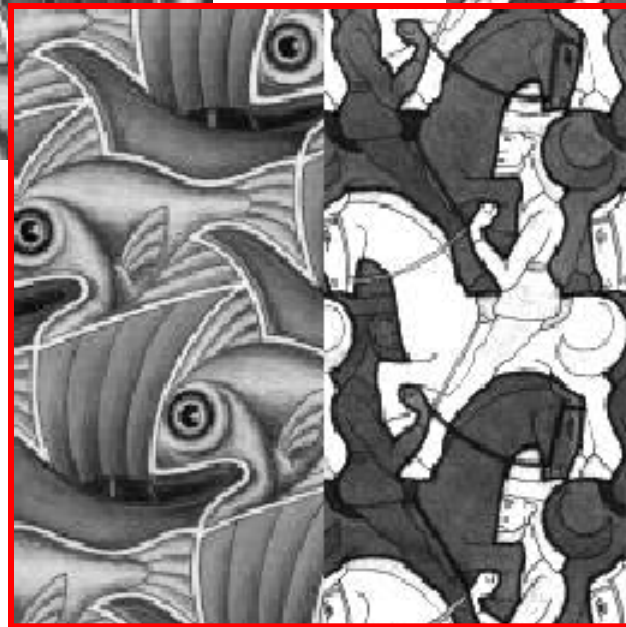
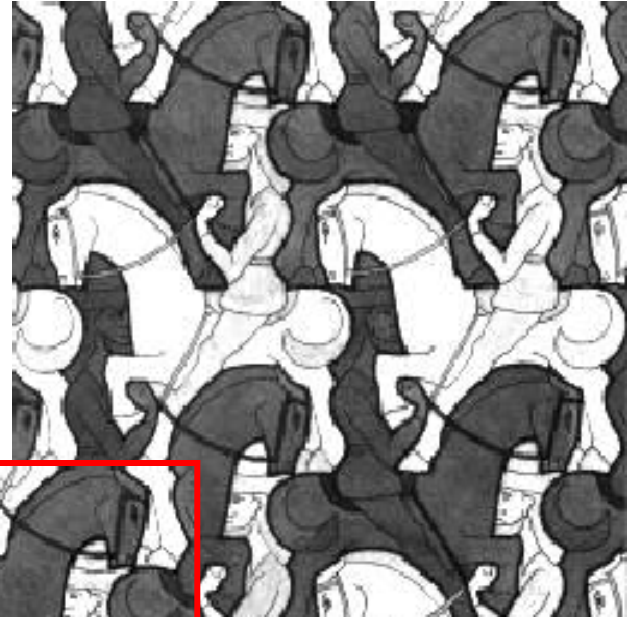
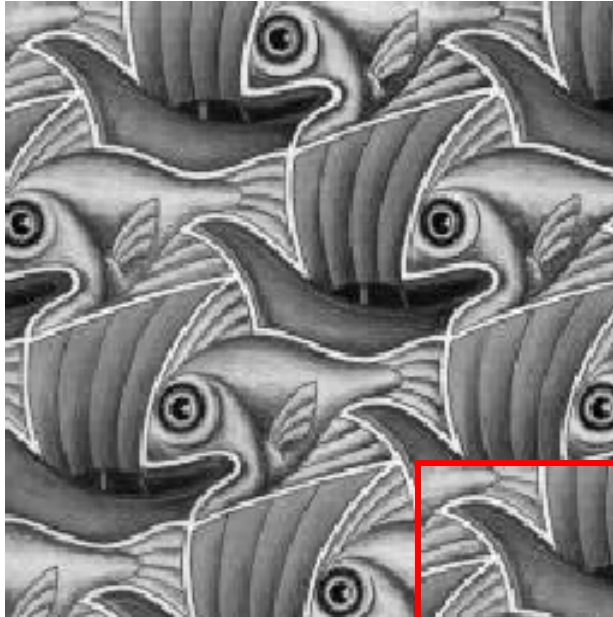


# Blending

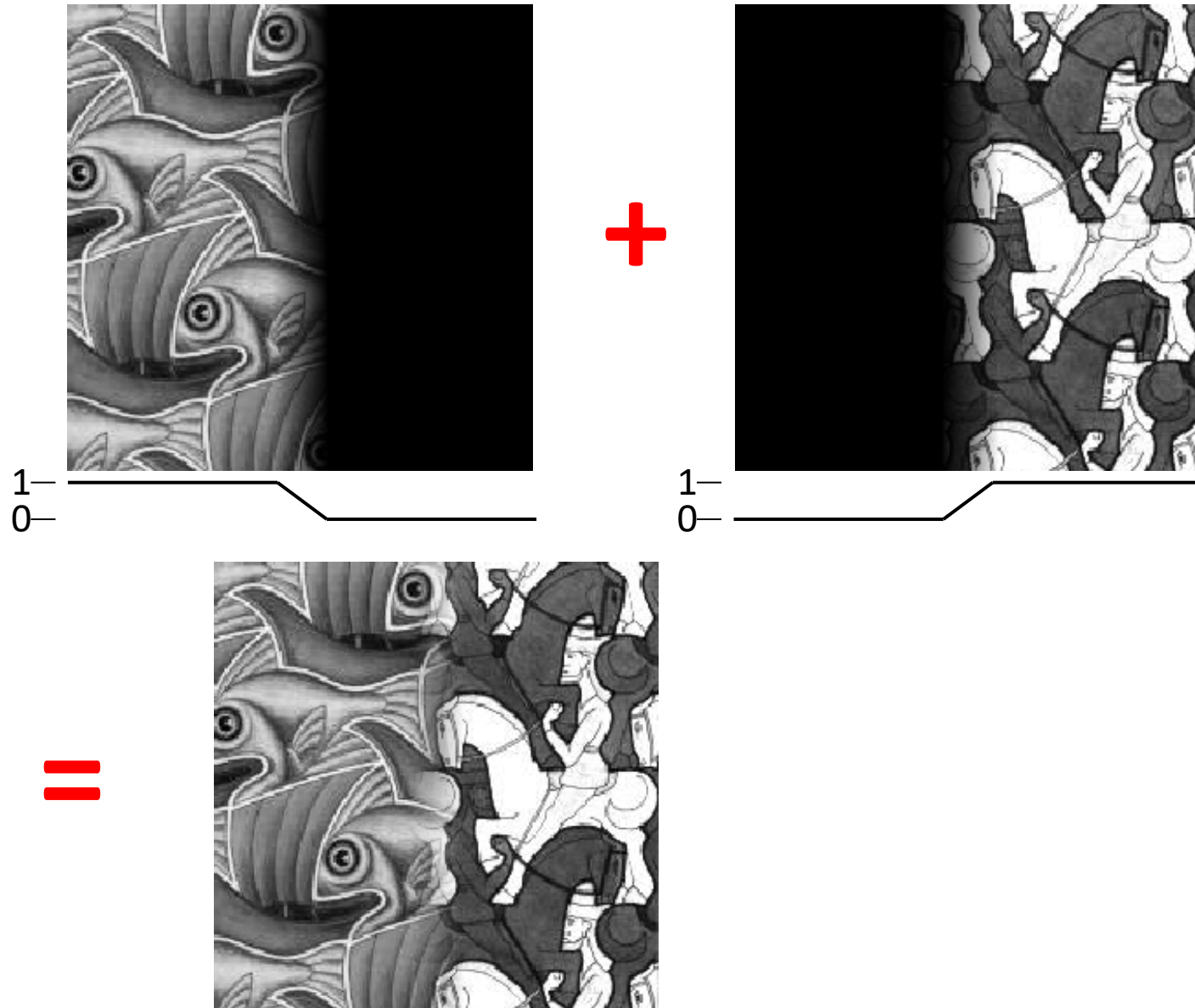
- Want to seamlessly blend them together



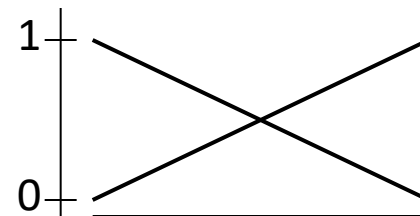
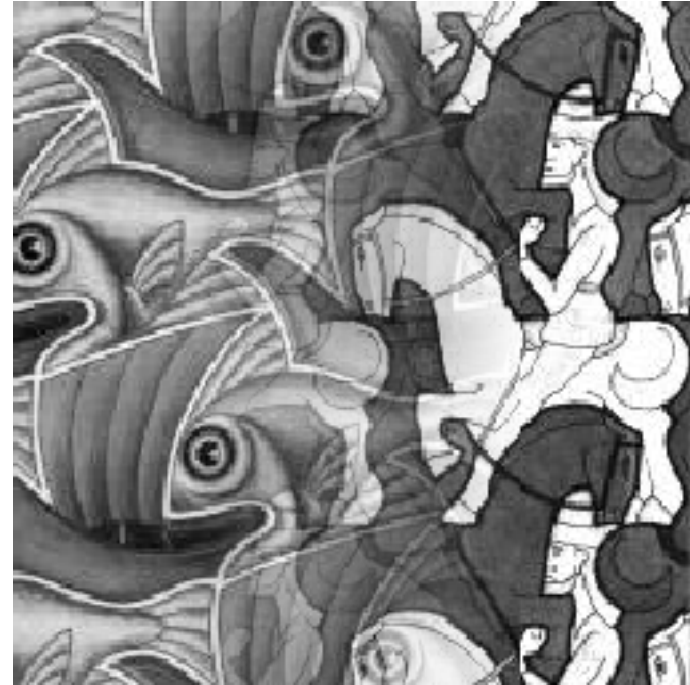
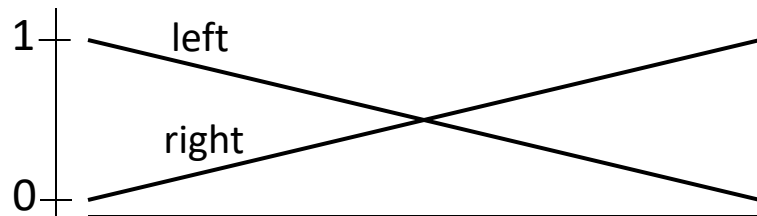
# Image Blending



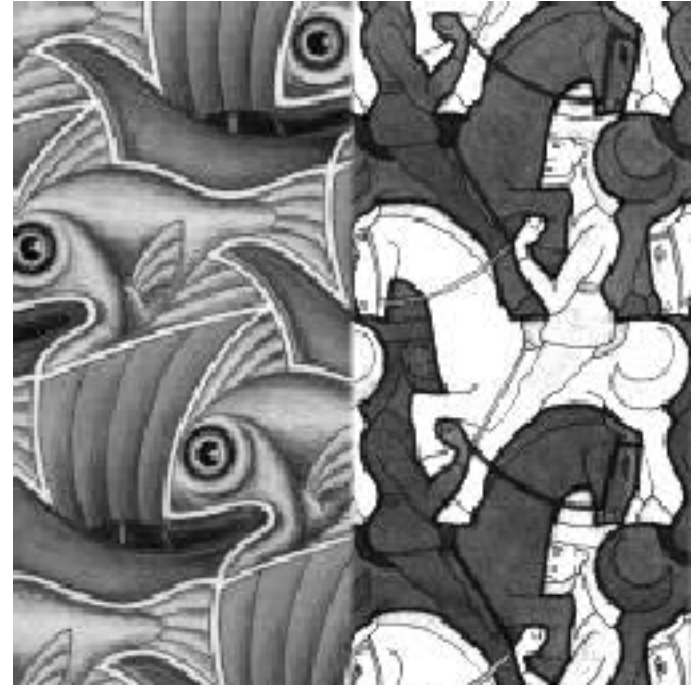
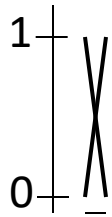
# Feathering



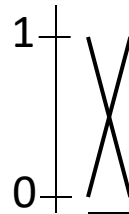
# Effect of window size



# Effect of window size



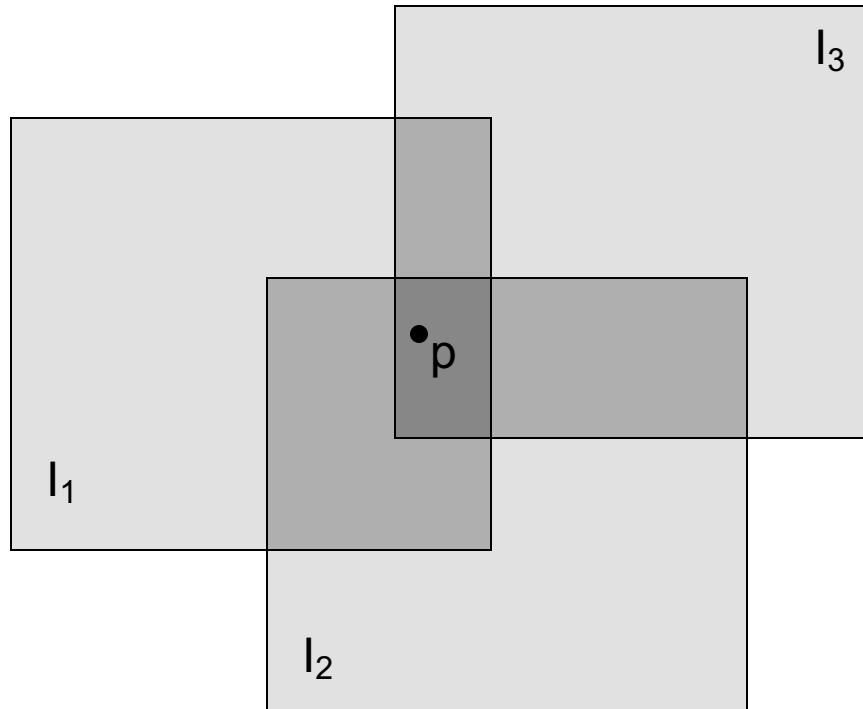
# Good window size



Best window: smooth but not ghosted

- Doesn't always work...
- Fancier blending tricks exist.

# With more images: Alpha Blending



Encoding blend weights:  $I(x,y) = (\alpha R, \alpha G, \alpha B, \alpha)$

color at  $p = \frac{(\alpha_1 R_1, \alpha_1 G_1, \alpha_1 B_1) + (\alpha_2 R_2, \alpha_2 G_2, \alpha_2 B_2) + (\alpha_3 R_3, \alpha_3 G_3, \alpha_3 B_3)}{\alpha_1 + \alpha_2 + \alpha_3}$

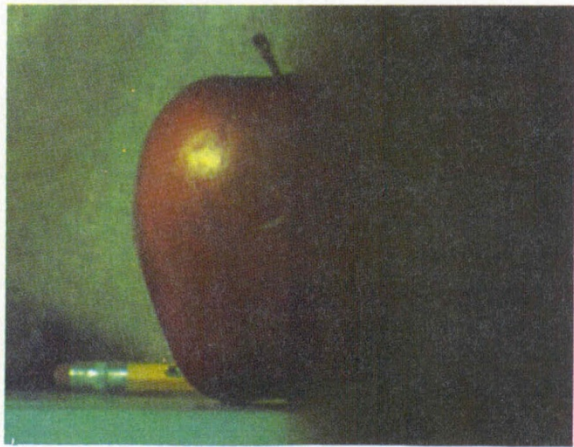
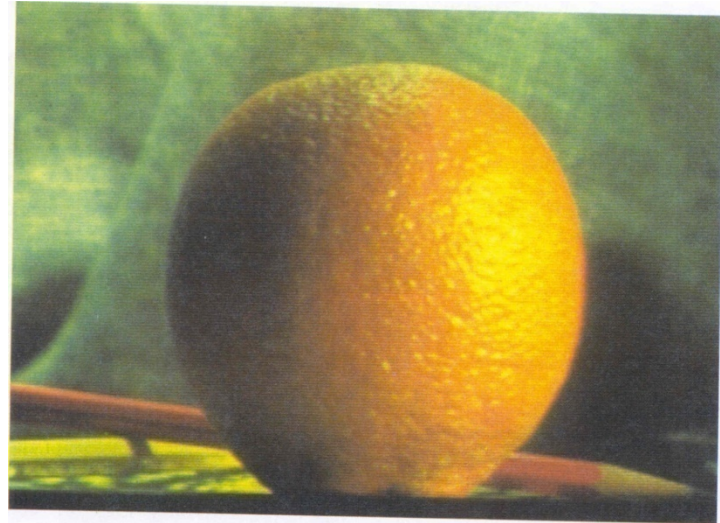
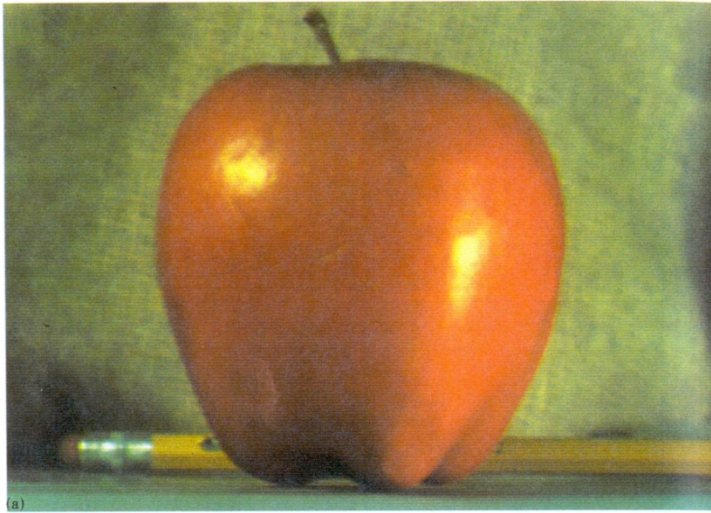
Implement this in two steps:

1. accumulate: add up the ( $\alpha$  premultiplied) RGB $\alpha$  values at each pixel
2. normalize: divide each pixel's accumulated RGB by its  $\alpha$  value

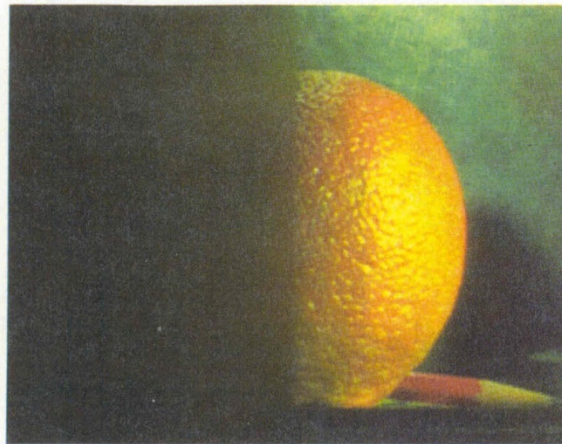
Q: what if  $\alpha = 0$ ?



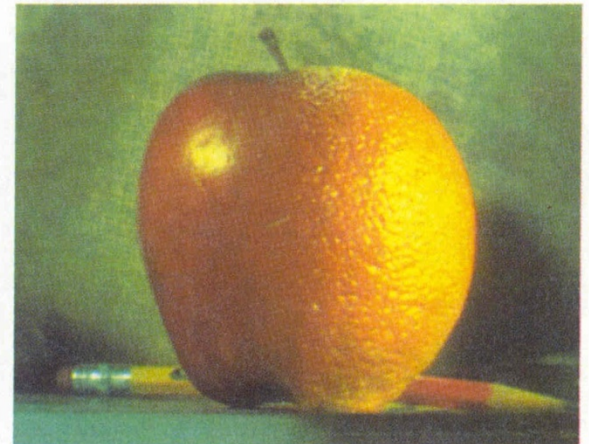
# Pyramid blending



(d)



(h)



(l)

Create a Laplacian pyramid, blend each level

- Burt, P. J. and Adelson, E. H., [A multiresolution spline with applications to image mosaics](#), ACM Transactions on Graphics, 42(4), October 1983, 217-236.