

CSCI 497P/597P: Computer Vision



Lecture 18

Pinhole Camera Model

360 (Spherical) Panoramas

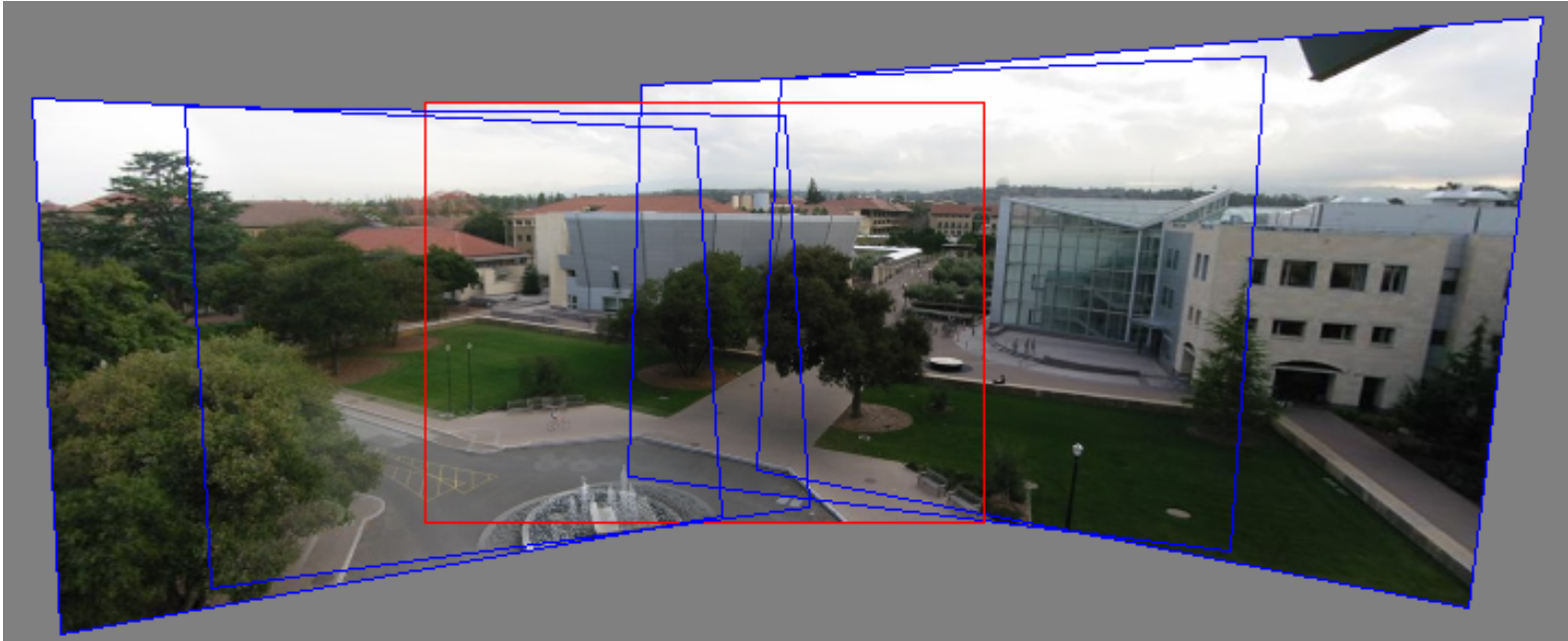
Announcements

- Deadline to pair up for P2 is Wednesday night.
 - Include your github usernames in your email.
- Reminder/597 update: Letter grade surveys
 - 497: opt in for letter grade by June 5
 - 597 opt in for P/NP by May 22

Goals

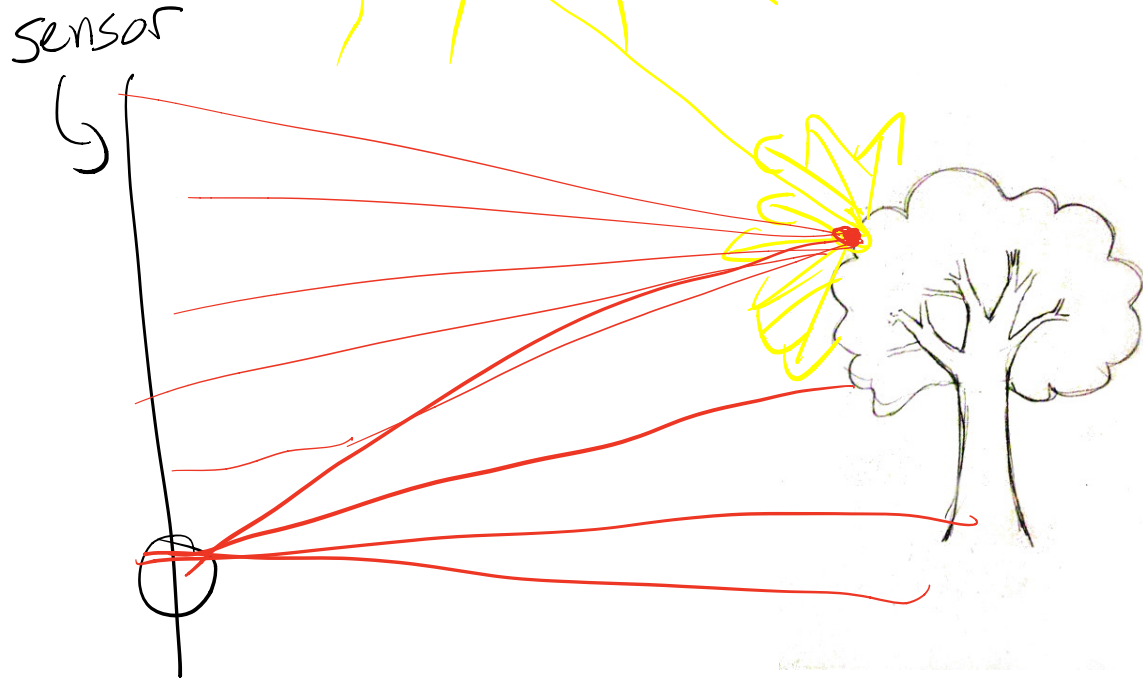
- Understand where images come from (under the [pinhole camera model](#))
 - Be able to derive the 3x4 [pinhole projection matrix](#)
 - Understand the interpretation of planar panorama stitching in terms of using homographies to map images onto a common plane.
- Know how to create 360 degree panoramas by mapping images onto a spherical surface instead.

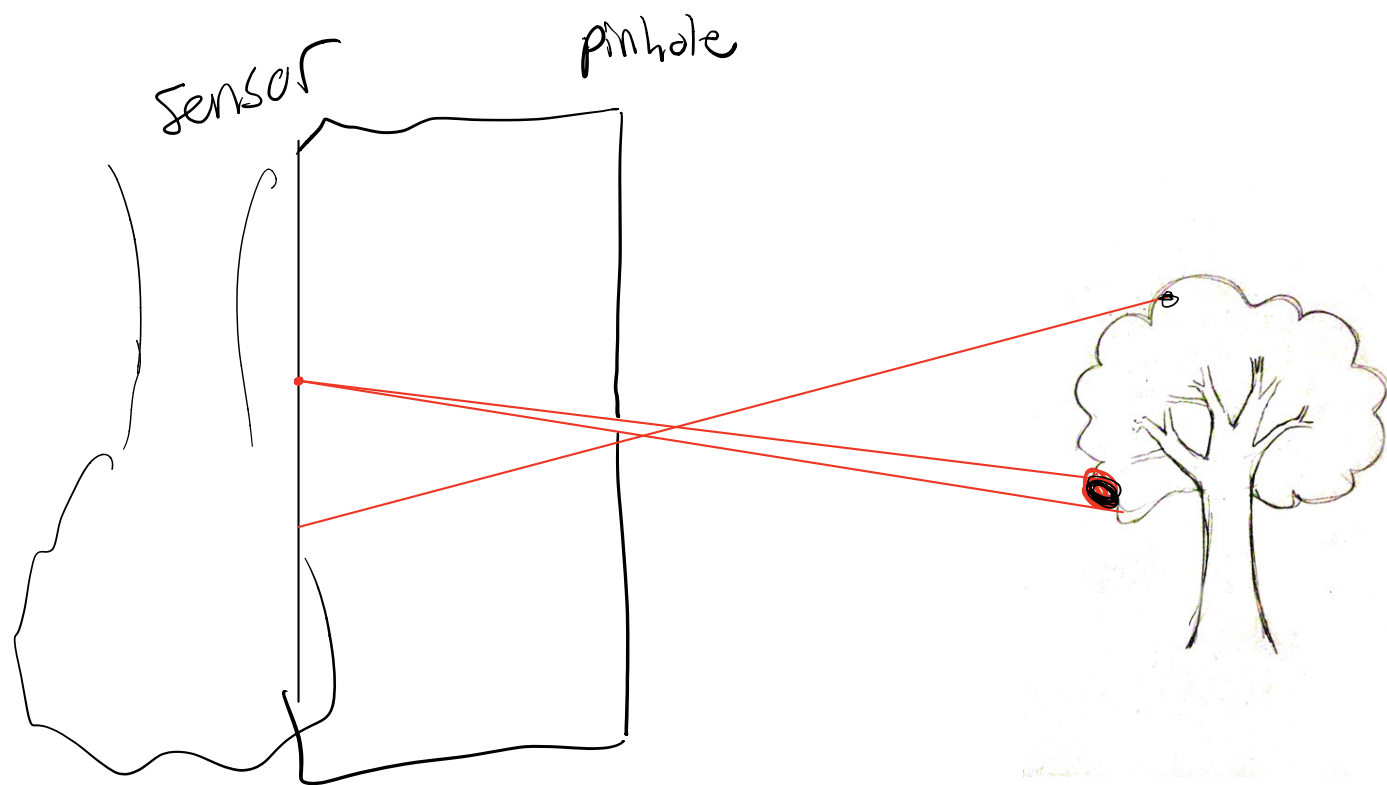
Can we make 360 panoramas?



To answer this, we need to know how these images came to be. Why can we even make **any** panoramas with homographies?

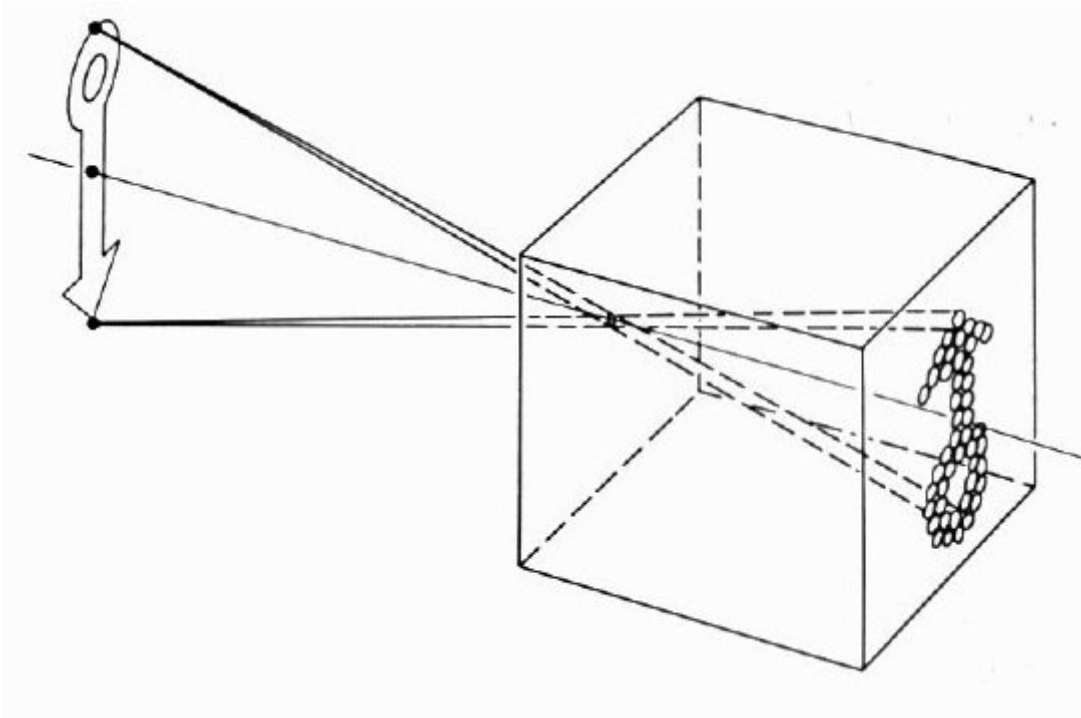
Where do images come from?





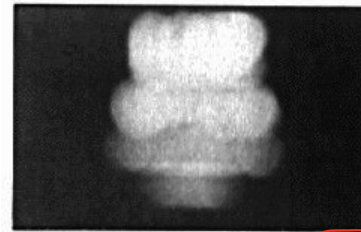
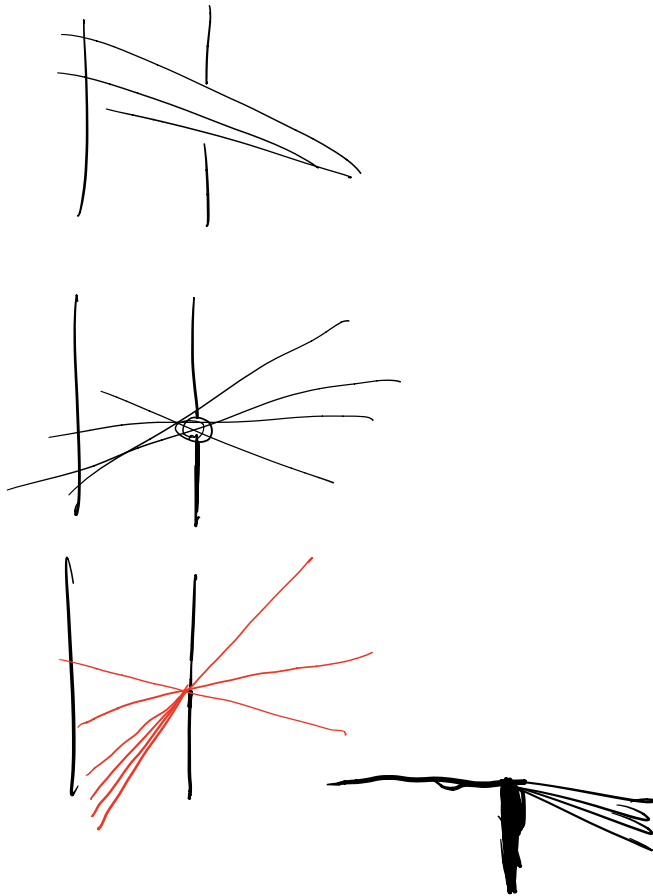
497Cam, Mk II

Camera Obscura (pinhole camera)





The Effect of Pinhole Size



2 mm



1 mm



0.6 mm



0.35 mm

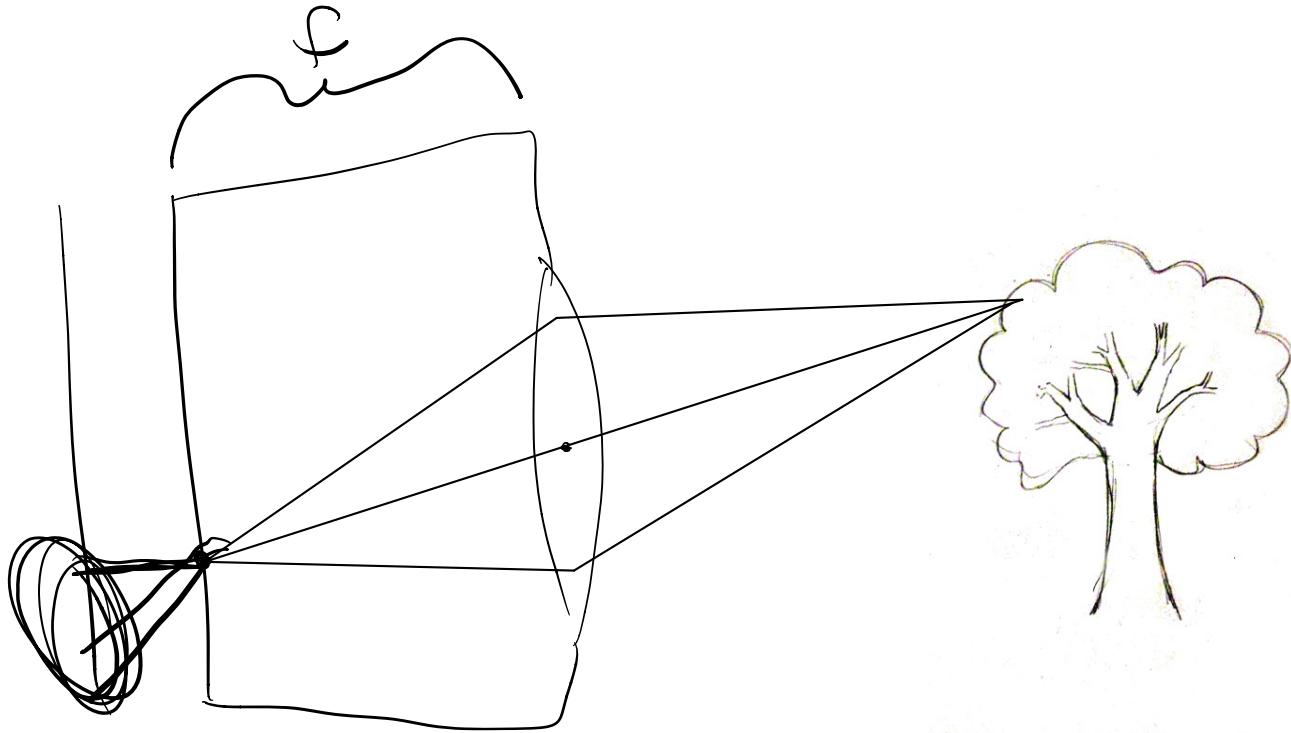


0.15 mm



0.07 mm

Aside: What about Lenses?





CoolOpticalIllusions.com

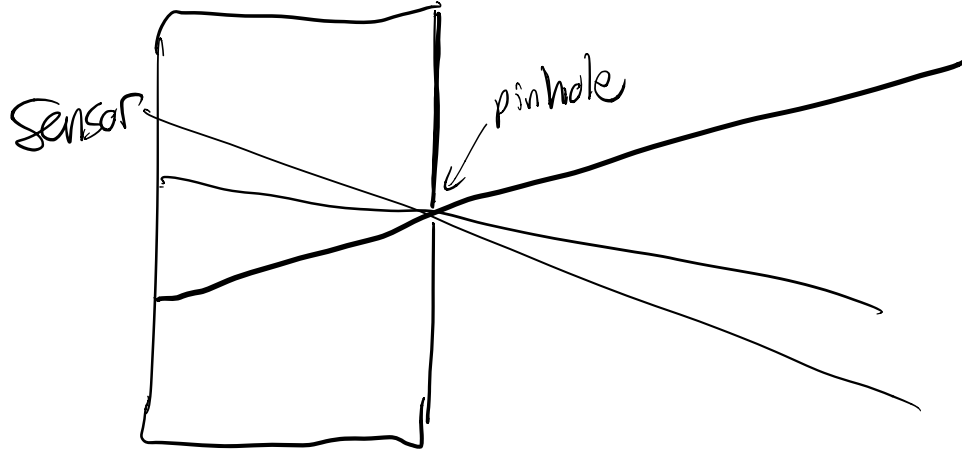
JULIAN BEEVER



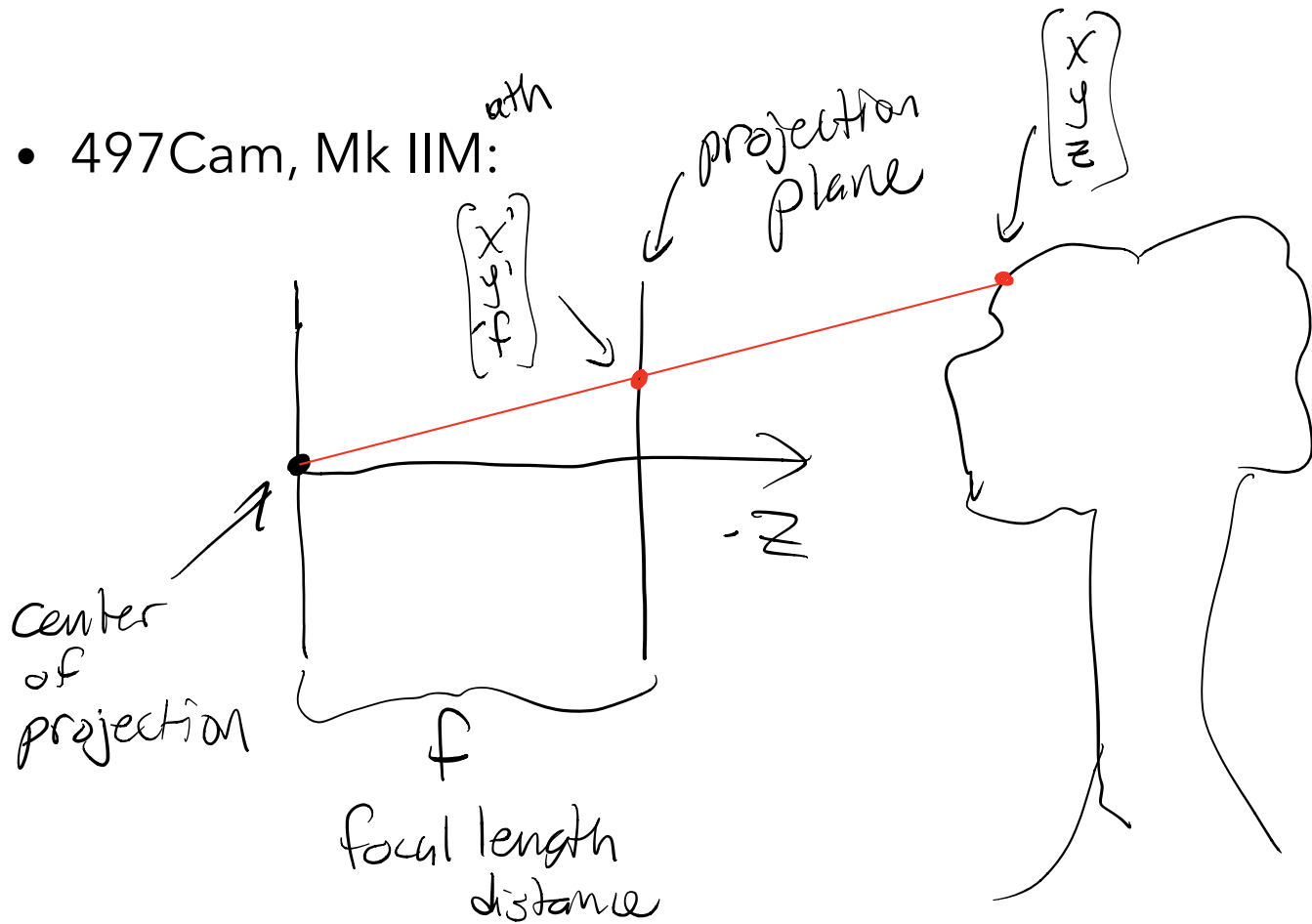
CoolOpticalIllusions.com

The Pinhole Camera Model

- 497Cam, Mk II:

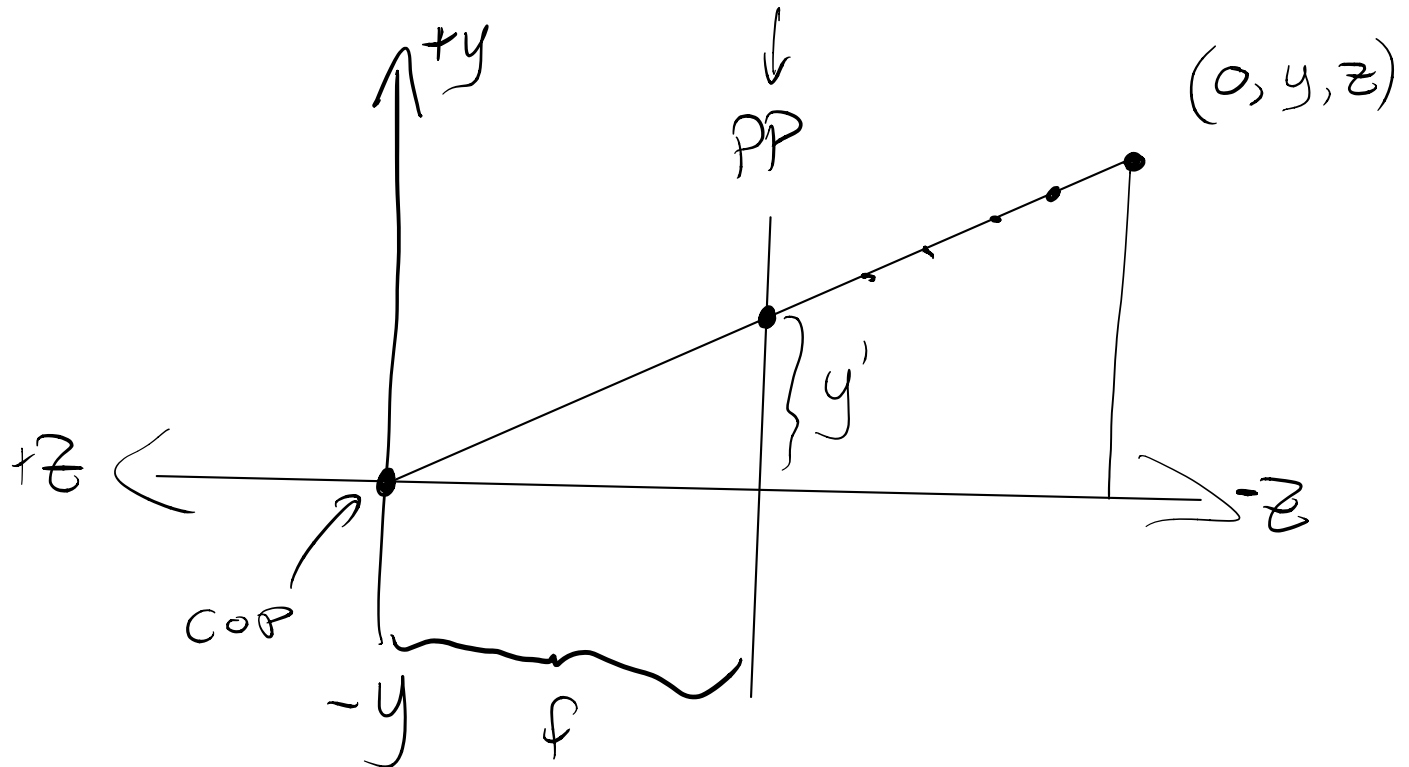


- 497Cam, Mk IIM:

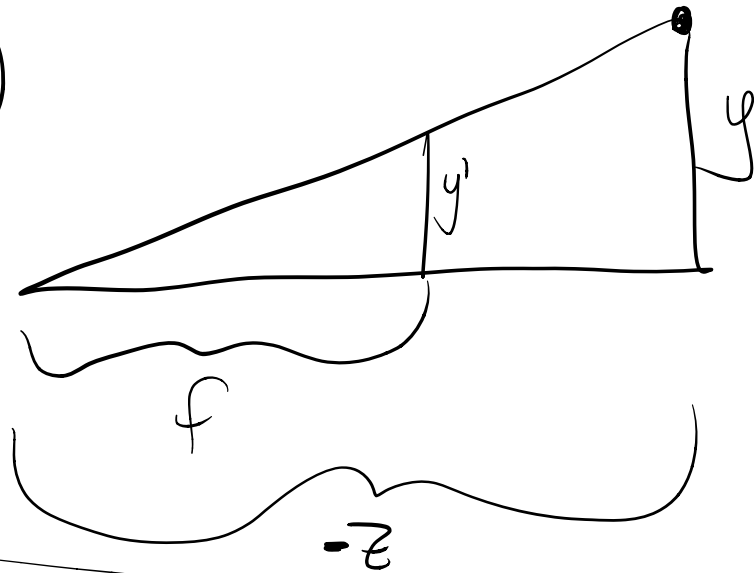


Projection in a Pinhole Camera

- Ms. Collins' geometric (10th grade) way:



$$y \mid y' = \frac{f}{z} y$$



$$\begin{aligned} y' &= -\frac{fy}{z} \\ x' &= -\frac{fx}{z} \\ z' &= -f \end{aligned}$$

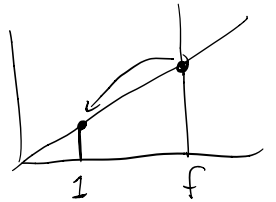
← these are 3D (non homogeneous) coordinates.

In the image, the coordinates will

be:

$$\begin{bmatrix} -fx \\ -fy \\ -f \\ 1 \end{bmatrix}$$

because if we divide out the f , all cameras would have $f=1$:



Projection in a Pinhole Camera

Scott fails 15th grade :'

- Dr. Swenton's (15th grade) way:

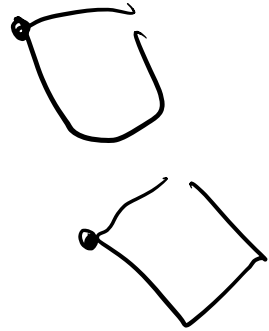
$$\begin{pmatrix} -f/x \\ z \\ -f/y \\ z \\ 1 \end{pmatrix} \approx \begin{pmatrix} -fx \\ -fy \\ z \end{pmatrix} \approx \begin{pmatrix} x \\ y \\ -z/f \end{pmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -f & 0 \end{bmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}$$

↑ what we want to end up with
 ↑ get rid of division
 ↑ put all weirdness in one place
 ↑ pinhole projection matrix
 ↑ 3D homog. scene coords

Reinterpreting Homographies

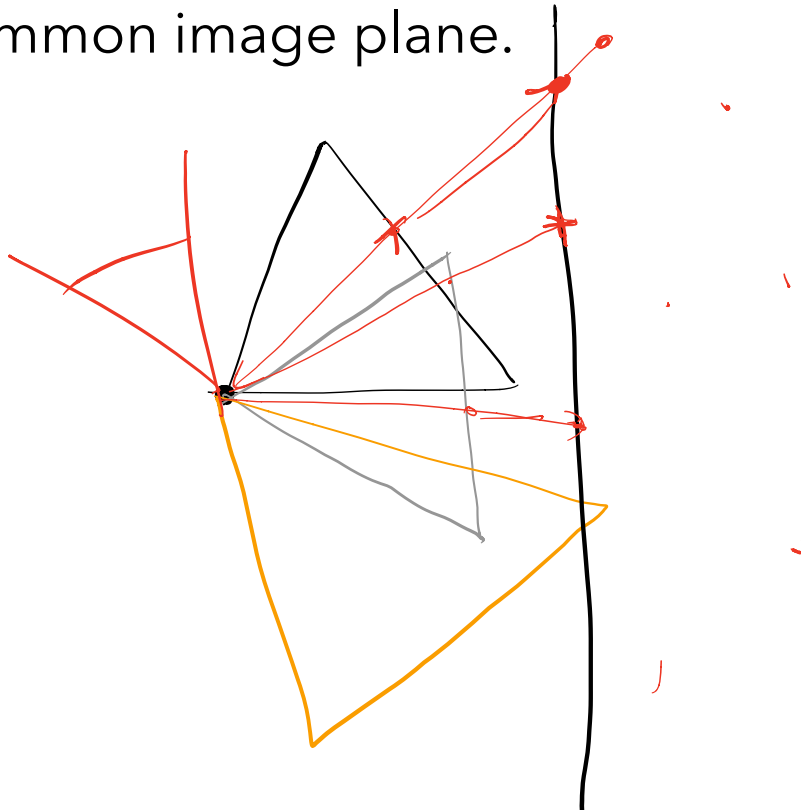
A **3x3 linear transformation**, applied to a projection **plane**.

origin
↓
•

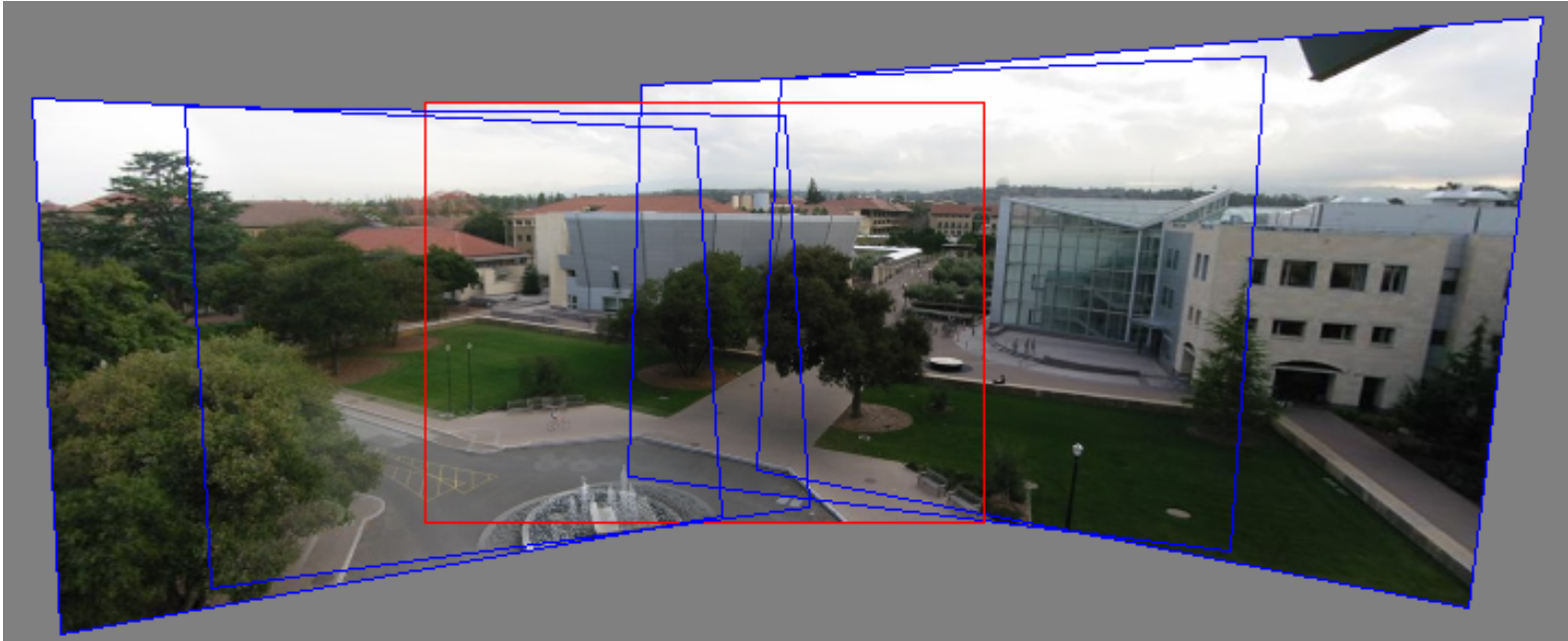


Reinterpreting Homography-aligned Panoramas

- Several image planes are warped (projected) onto a common image plane.



I'll ask it again:
Can we make 360 panoramas?



Spherical Panoramas

Idea: project images onto a **sphere** instead of a plane.

What motion model do we use?

