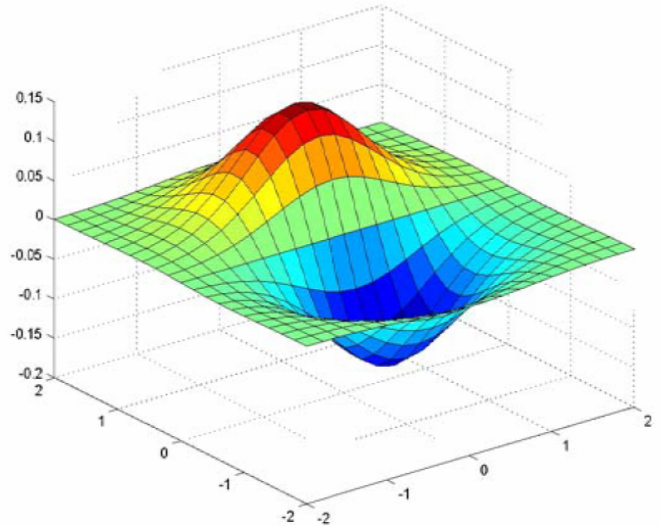
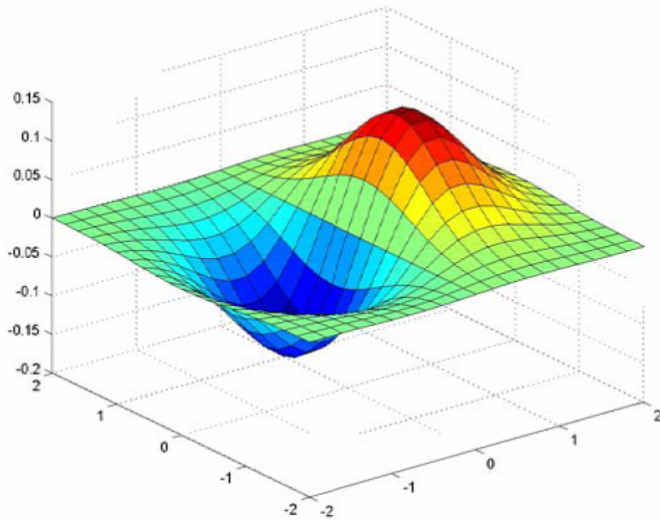


CSCI 497P/597P: Computer Vision



Lecture 4: Edges, Gradients, Frequency Content

Goals

- Understand the limitations of linear filtering
- Know how to compute image derivatives using convolution filters

- Understand how the Sobel filter works to detect edges.

- Have an intuitive understanding of what constitutes **high frequency** and **low frequency** image content.

- Know how to make images smaller:

- The naive way via subsampling (and why this is bad)
- The better way by prefiltering (and why this is better)

next time!

Stepping back:

- Filtering:

output pixel depends on input neighborhood

- Linear filtering:

output pixel is a weighted average of input neighborhood
(must always use the same weights to be linear)

- Cross-correlation is a kind of linear filtering:

output pixel = weighted average(neighborhood)

must have same weights for all pixels

- Convolution: cross-correlation, but first flip the kernel horizontally and vertically

Linear Filtering: Questions

- What happens at the edges?

padding
modes

output
sizes

- What properties does this operator have?

shift invariance

associativity (parentheses)

linearity

commutativity (order)

- What can and can't this operator do?

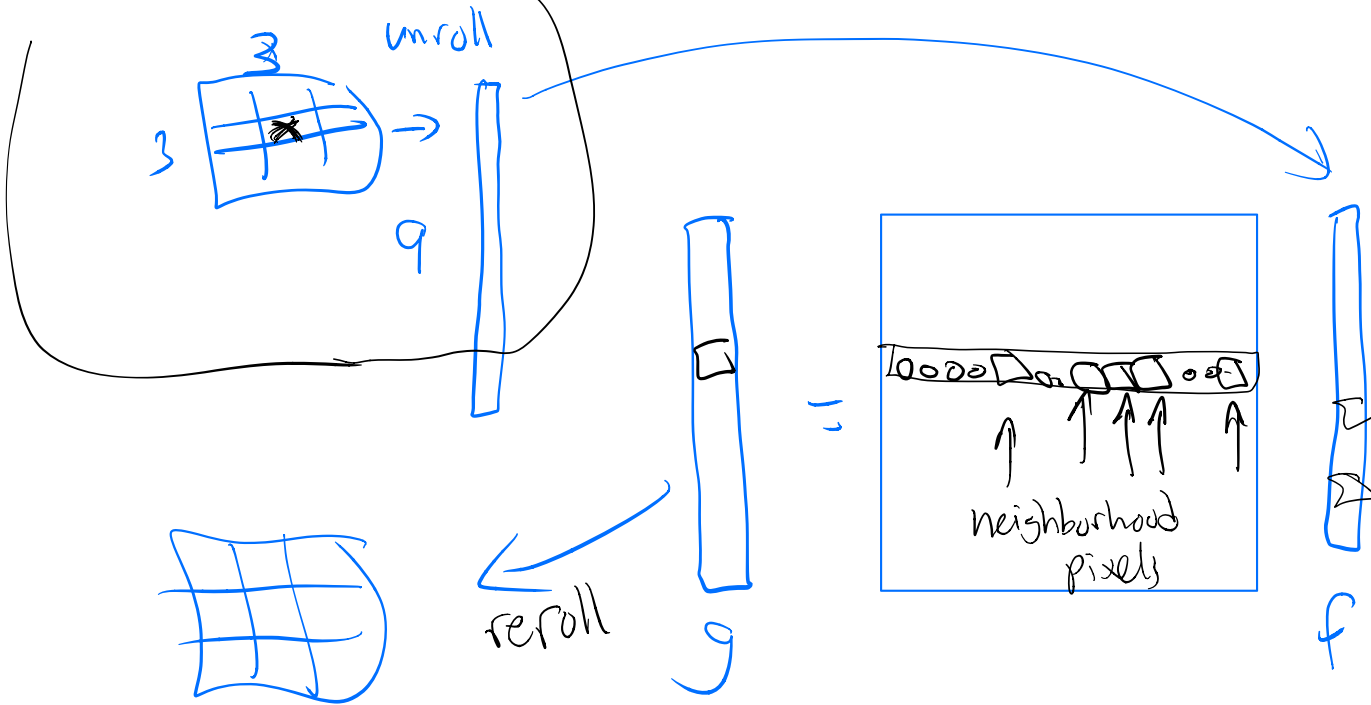
can:

blur shift
sharpen

can't: ?

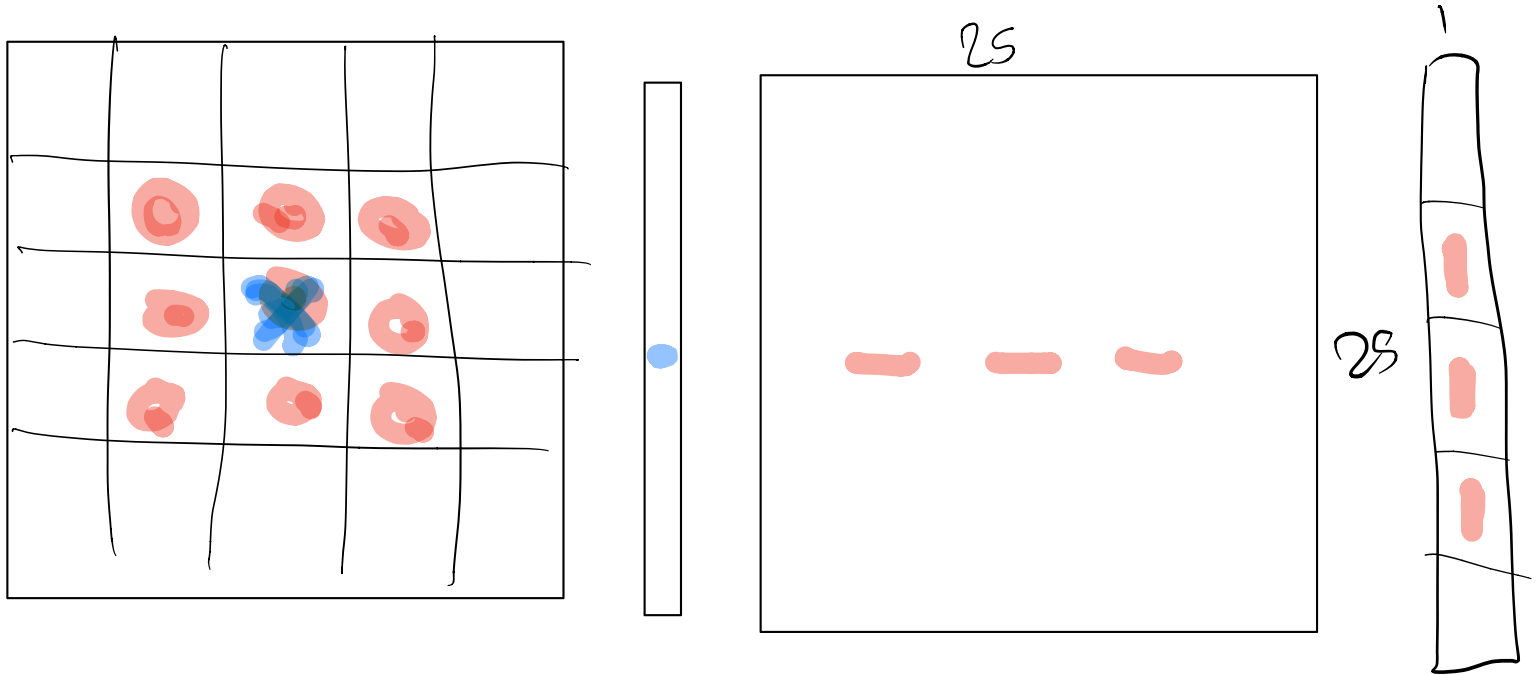
Aside:

Doesn't linear mean matrices?



Aside:

Doesn't linear mean matrices?



output pixel is the result of a dot product (i.e., weighted average)

Can a linear filter do this?

Discuss in breakout rooms, answer on Socrative:

- Output pixel = max value in the neighborhood

- Output pixel is

- 255 if input pixel is > 127

- 0 otherwise



- Compute a finite-difference approximation of the derivative of the image function?

~~Maximum:~~

~~$?$~~

0	0	1
0	0	0
0	0	0

~~f~~

1	2	3
1	2	2
1	1	1

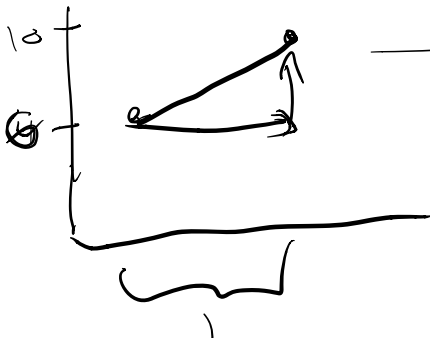
~~Threshold:~~

Derivative

$$\begin{aligned} & -1 \cdot 6 + 1 \cdot 10 \\ & = 4 \end{aligned}$$

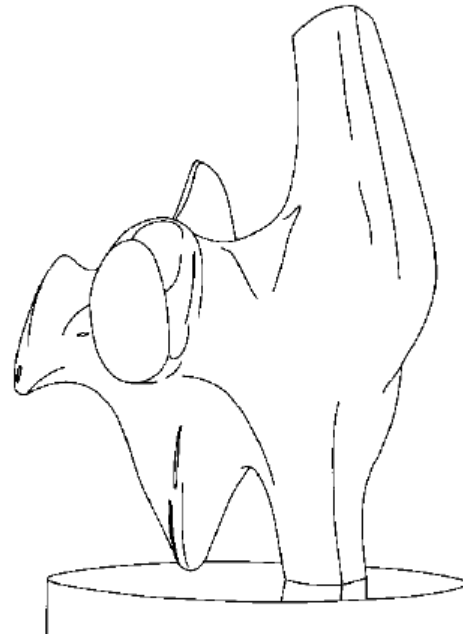
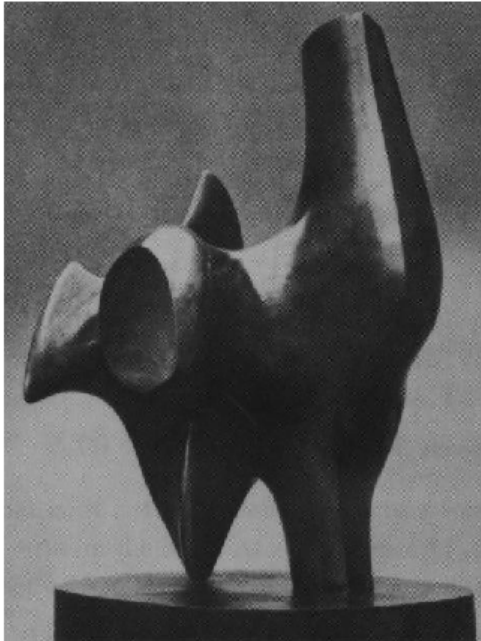
0	0	0
-1	1	0
0	0	0

6	10

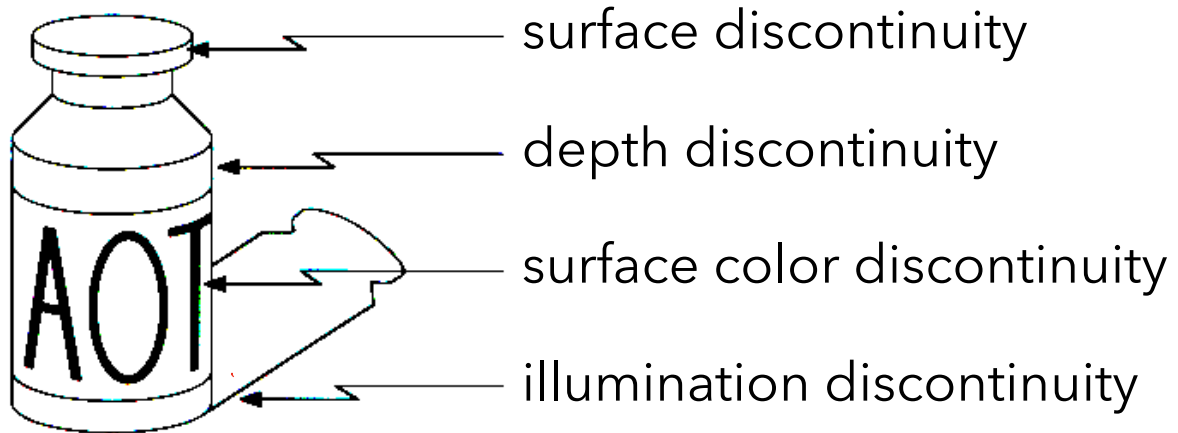


Calculus!?

- Edge detection: a classic vision problem.



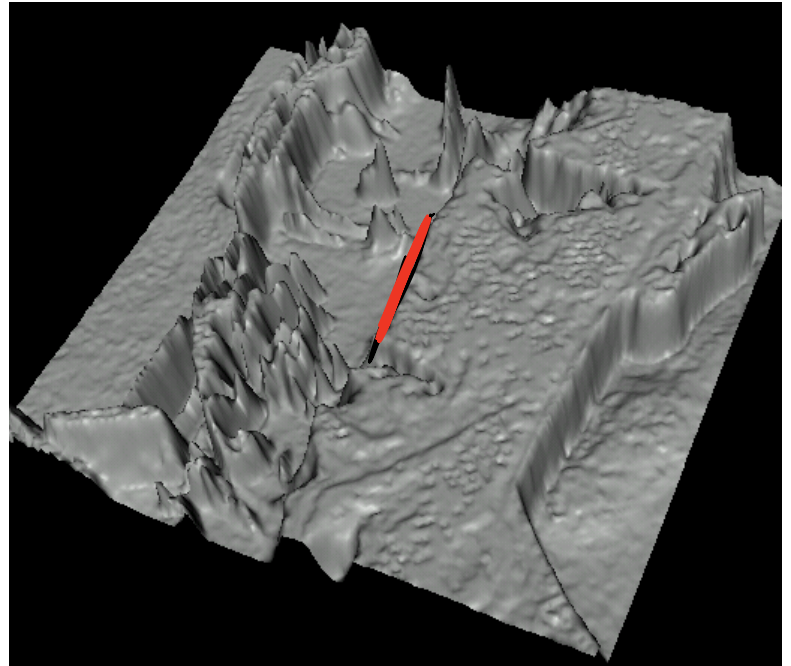
What is an edge?



How do we find them?

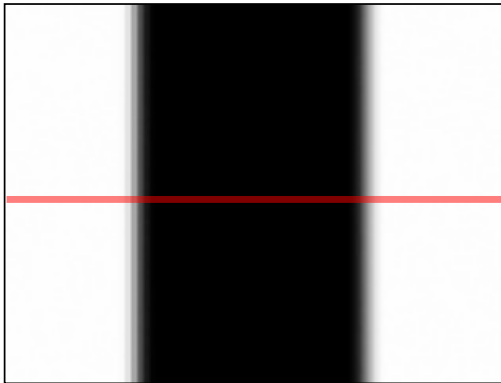


$f(x,y)$ as brightness

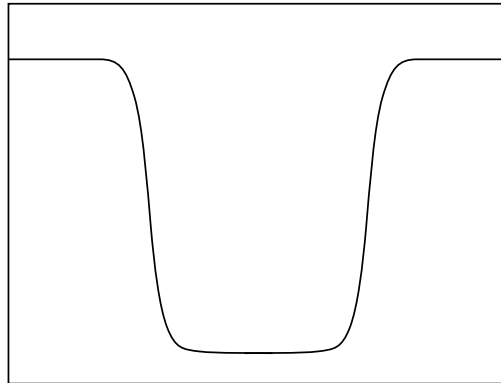


$f(x,y)$ as height

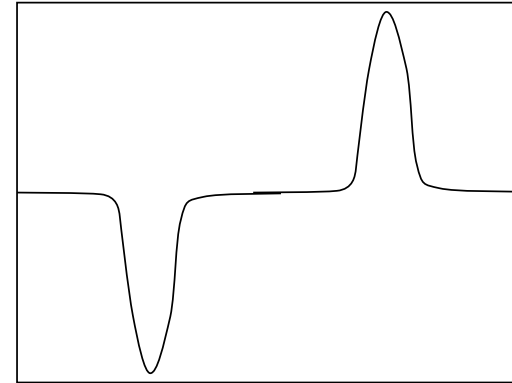
Characterizing edges



image



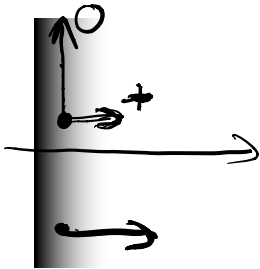
1D scanline



first derivative

Partial Derivatives

- Images are 2D - have x and y **partial derivatives**



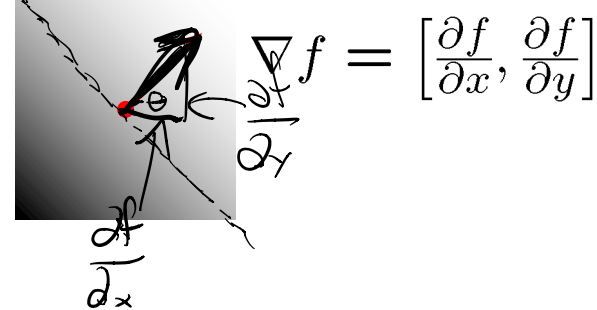
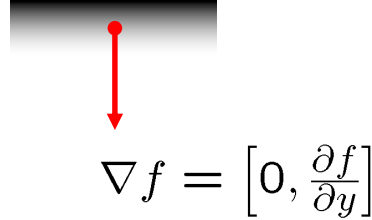
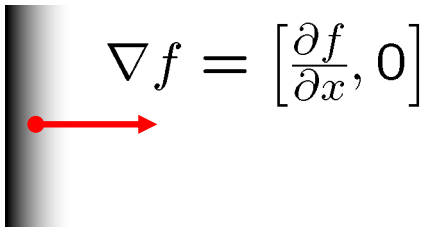
$$f(x, y) \quad \frac{\partial f}{\partial x}$$

- The partial derivatives together in a 2-vector are the **image gradient**:

$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$$

Image Gradient as Edge Detector

$$\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right]$$



What is the edge **strength**?

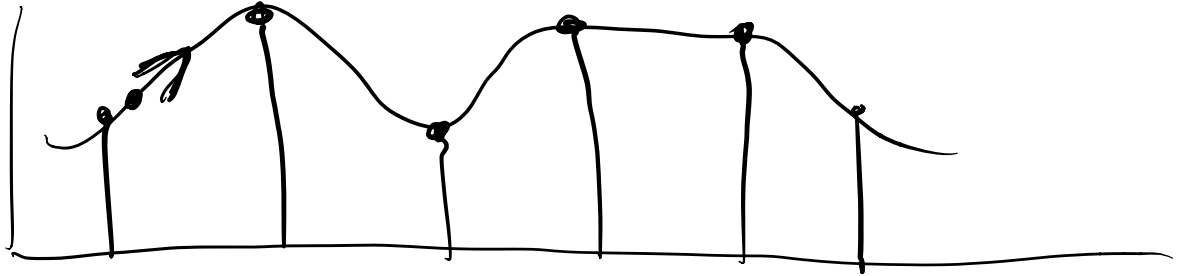
$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

What is the edge **direction**?

$$\tan^{-1}\left(\frac{\frac{\partial f}{\partial y}}{\frac{\partial f}{\partial x}}\right)$$

Image Derivatives

- How do we differentiate a discrete (sampled) image?
 - Reconstruct a continuous function and compute the derivative



- Use **finite differences**

Derivative Filters

- How do we differentiate a discrete digital image?
 - Use finite differences

Derivative Filters

- How do we differentiate a discrete digital image?
 - Use finite differences

1	1	0
1	1	0
1	0	0

not centered

0	0	0
-1	1	0
0	0	0

0	0	0
0	1	0
0	-1	0

centered

0	0	0
-1	0	1
0	0	0

0	1	0
0	0	0
0	-1	0

Derivative Filters

- How do we differentiate a discrete digital image?
 - Use finite differences

$$\begin{array}{cccc}
 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 \\
 0 & 0 & 1 & 1 \\
 0 & 0 & 1 & 1 \\
 0 & 0 & 1 & 1
 \end{array}
 *
 \begin{array}{ccc}
 0 & 0 & 0 \\
 -1 & 0 & 1 \\
 0 & 0 & 0
 \end{array}
 =
 \begin{array}{ccc}
 0 & 1 & 1 \\
 0 & 1 & 1 \\
 1 & 1 & 0 \\
 1 & 1 & 0
 \end{array}$$

Exercise: Compute the horizontal (x) derivative using the centered finite difference filter. Assume "repeat" padding mode, "same" output size.

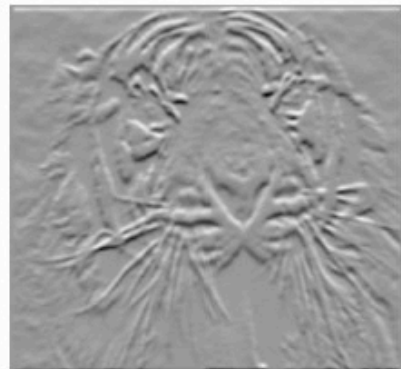
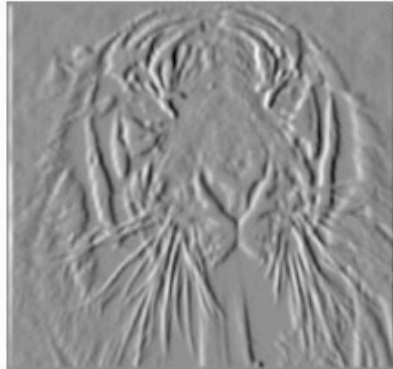
Image Gradient: Visually

$$f(x, y)$$



$$\|\nabla f\|$$

$$\frac{\partial f}{\partial x}$$



$$\frac{\partial f}{\partial y}$$