

CSCI 497P/597P: Computer Vision



Lecture 25

Structure From Motion

Multiview Stereo

Introduction to Recognition

Announcements

- P3 due in 1 week
- HW4 due Friday

Goals

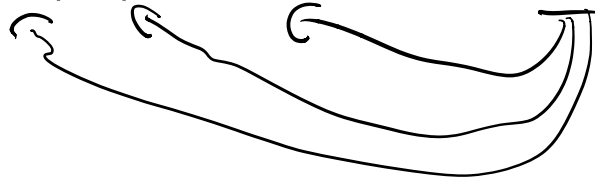
- Understand the Structure From Motion problem and the general idea behind how it is solved.
- Understand the Multiview Stereo problem and the general idea behind how it's solved.

Two questions:

- We derived **F** assuming that **K**, **R**, and **t** are known.
- Can we find **F** without them?

yes - normalized 8-point algorithm, among others

- Can we find **K**, **R**, and **t** if we have **F**?



match

$$q^T F p = 0$$

What about more than 2 views?

- 2 views: fundamental matrix

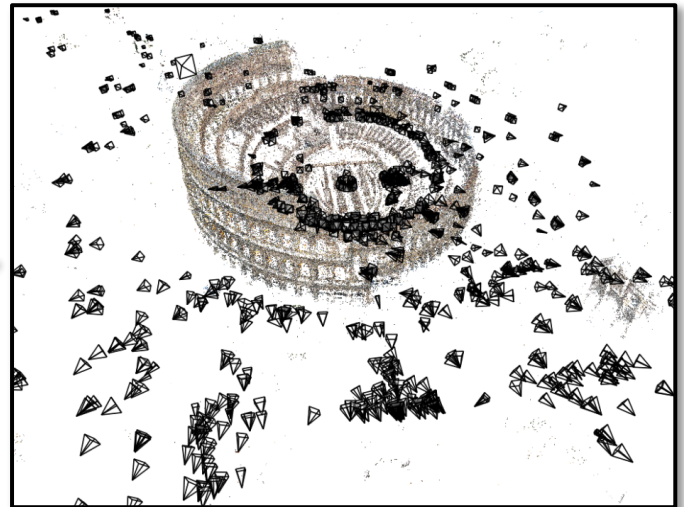
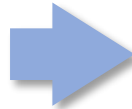
- 3 views: trifocal tensor

- 4 views: *quadrifocal* tensor

- more views: it's called **Structure From Motion**

Structure from Motion

- Given many photos, reconstruct:
 - positions of the cameras
 - positions of 3D points



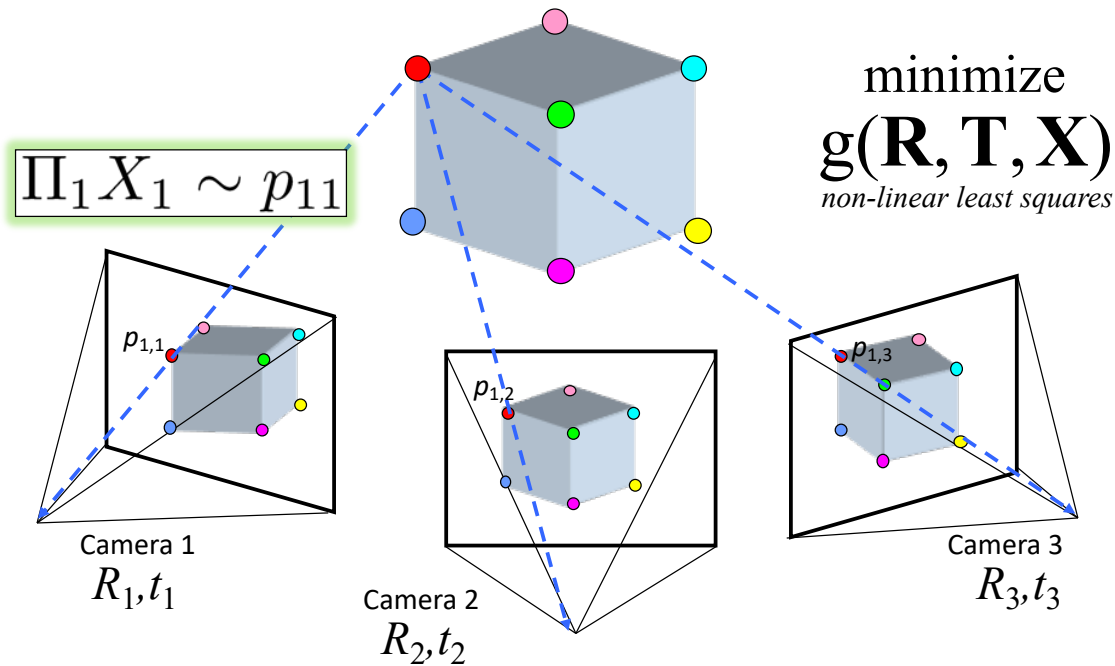
Large-scale structure from motion

- <https://www.youtube.com/watch?v=sQegEro5Bfo>

Chicken/Egg

- Step 1: solve for relative pose of pairs (or triples) of cameras using correspondences from feature matching.
- Step 2: alternate between solving:
 - given camera positions, solve for point locations
 - given point locations, solve for camera positions

Structure From Motion



$$g(\mathbf{X}, \mathbf{R}, \mathbf{T}) = \sum_{i=1}^m \sum_{j=1}^n w_{ij} \cdot \left\| \underbrace{\mathbf{P}(\mathbf{x}_i, \mathbf{R}_j, \mathbf{t}_j)}_{\text{predicted image location}} - \underbrace{\begin{bmatrix} u_{i,j} \\ v_{i,j} \end{bmatrix}}_{\text{observed image location}} \right\|^2$$

indicator variable:
is point i visible in image j ?

Applications

- Hyperlapse <https://www.youtube.com/watch?v=SOpwHaQnRSY>
- SLAM: <https://medium.com/scape-technologies/building-the-ar-cloud-part-three-3d-maps-the-digital-scaffolding-of-the-21st-century-465fa55782dd>
- Graphics, movies, games, self-driving cars, robots, ...

SfMFlex

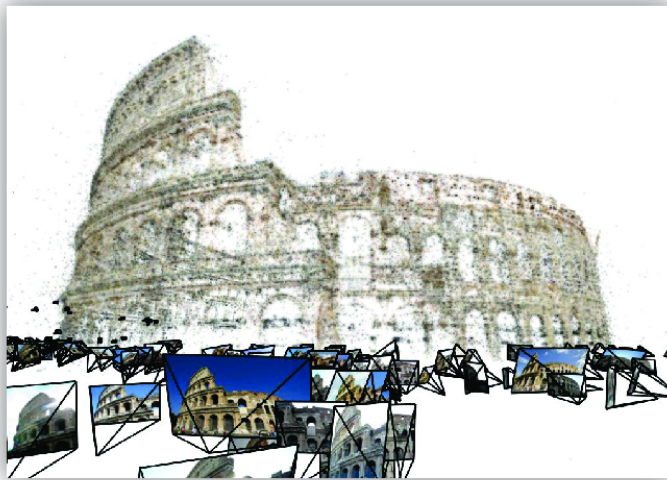


Visualizing Spectral Bundle Adjustment Uncertainty
Kyle Wilson and Scott Wehrwein, 3DV 2020.

Project webpage: <https://wilsonkl.github.io/sfmflex-release/>

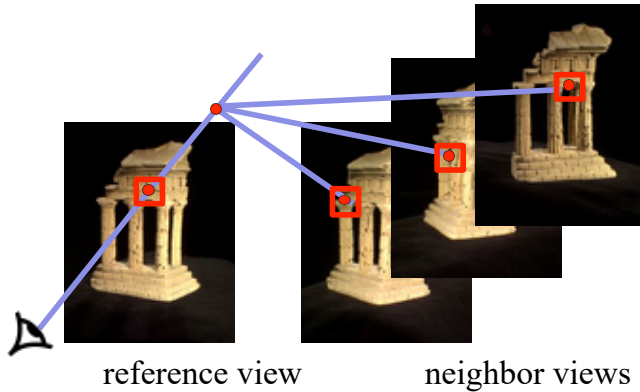
Multiview Stereo

- Once you've solved for all those camera positions, how good a 3D model can you create?

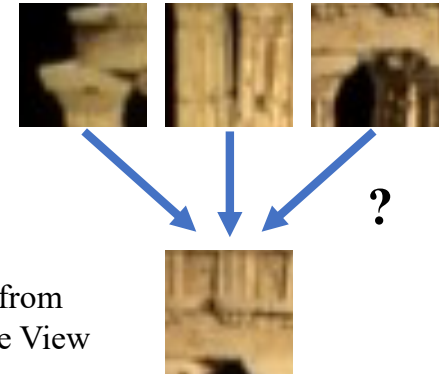


Multiview Stereo: Basic Idea

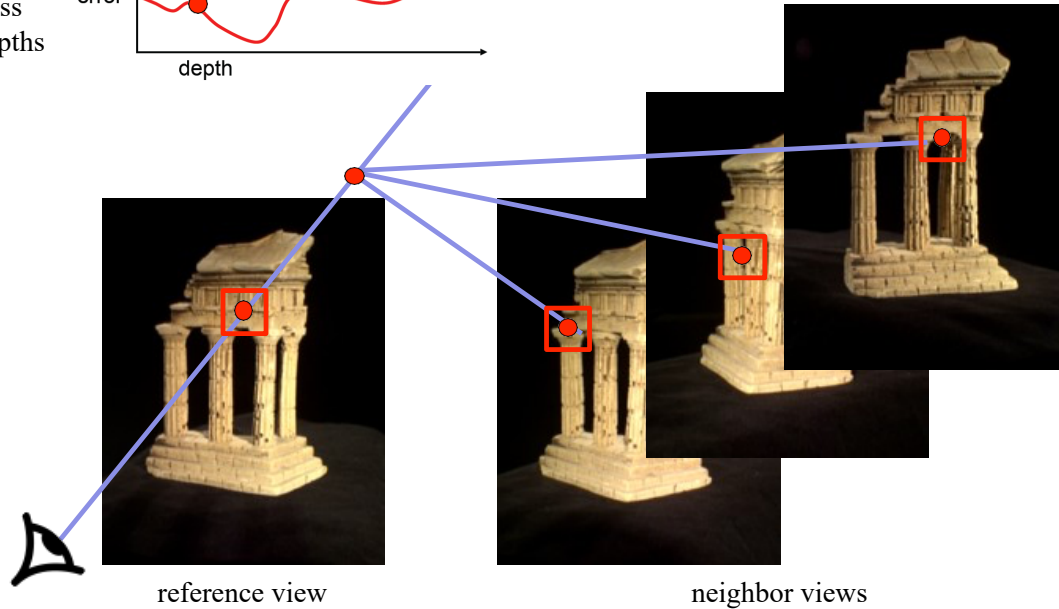
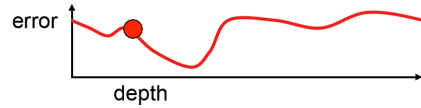
Evaluate the likelihood of geometry at a particular depth for a particular reference patch:



Corresponding patches at depth guess in other views

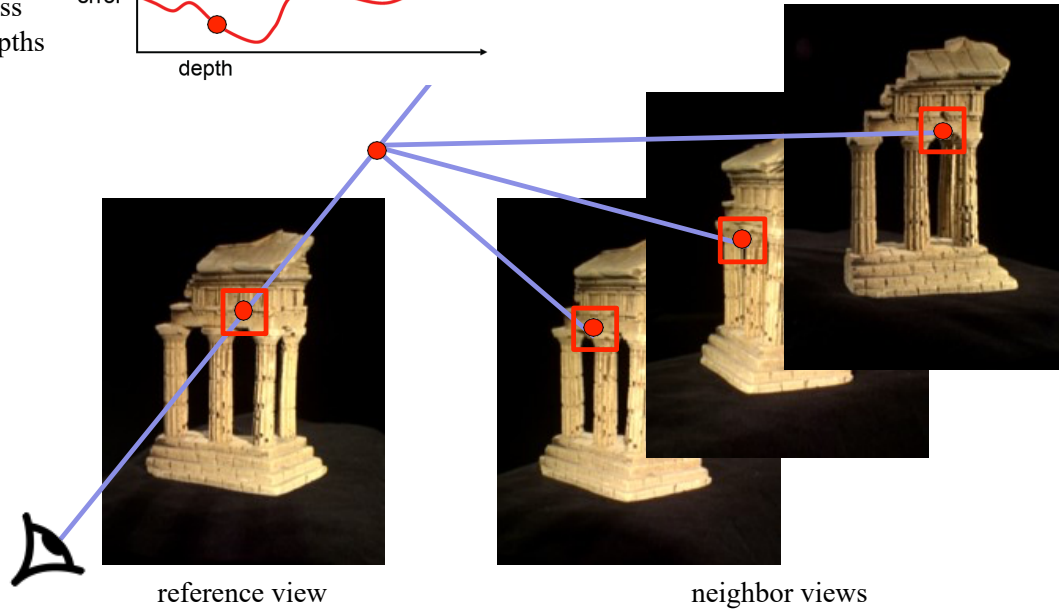
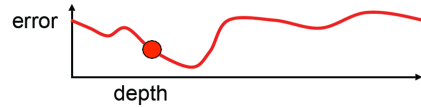


Photometric error across different depths



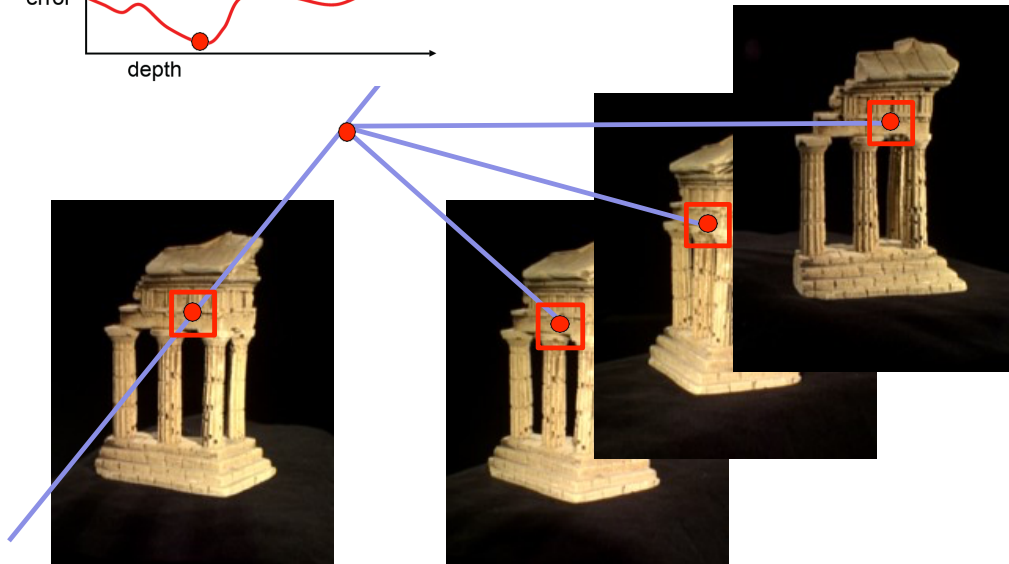
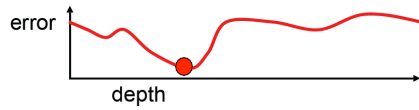
Source: Y. Furukawa

Photometric error across different depths



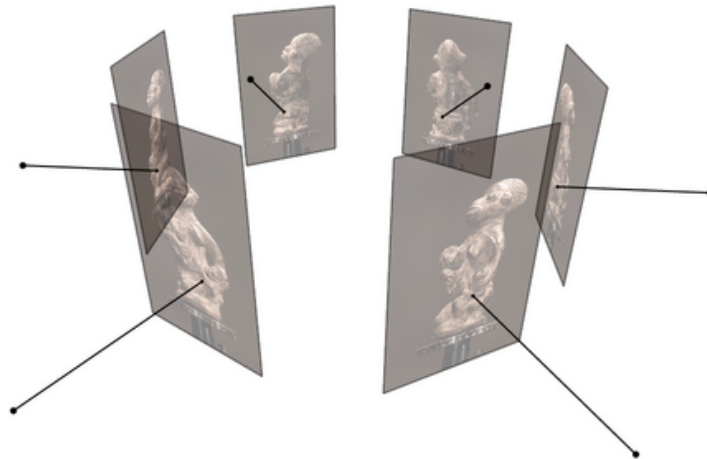
Source: Y. Furukawa

Photometric error across different depths



Depth map fusion

- Compute depth maps for multiple cameras, then fuse them into a 3D model



Figures by Carlos Hernandez

Result

- 3D Google Earth:
<https://www.youtube.com/watch?v=N6Douyfa7I8>