### Computer Graphics Lecture 13 Acceleration Structures

How expensive? Let's (informally) count some FLOPs. floating-point operations

**Reminder: Barycentric ray-triangle intersection**  $\checkmark \mathbf{p} + t\mathbf{d} = \mathbf{a} + \beta(\mathbf{b} - \mathbf{a}) + \gamma(\mathbf{c} - \mathbf{a}) \boldsymbol{\varsigma}$  $\beta(\mathbf{a} - \mathbf{b}) + \gamma(\mathbf{a} - \mathbf{c}) + t\mathbf{d} = \mathbf{a} - \mathbf{p}$  $\begin{bmatrix} \mathbf{a} - \mathbf{b} & \mathbf{a} - \mathbf{c} & \mathbf{d} \end{bmatrix} \begin{vmatrix} \beta \\ \gamma \\ \epsilon \end{vmatrix} = \begin{bmatrix} \mathbf{a} - \mathbf{p} \end{bmatrix}$  $\begin{bmatrix} x_a - x_b & x_a - x_c & x_d \\ y_a - y_b & y_a - y_c & y_d \\ z_a - z_b & z_a - z_c & z_d \end{bmatrix} \begin{bmatrix} \beta \\ \gamma \\ t \end{bmatrix} = \begin{bmatrix} x_a - x_p \\ y_a - y_p \\ z_a - z_p \end{bmatrix} \begin{cases} \lambda_{\text{in}} \cdot \boldsymbol{s} \boldsymbol{s}. \end{cases}$ 

- This is a linear system: Ax = b
- Various ways to solve, but a fast one uses *Cramer's rule*.
- See 4.4.2 for the TL;DR formula
- See 5.3.2 for an explanation of Cramer's rule

$$\begin{array}{c} \text{Reminder:} \\ \textbf{Barycentric ray-triangle intersection} \\ \mathbf{p} + t\mathbf{d} = \mathbf{a} + \beta(\mathbf{b} - \mathbf{a}) + \gamma(\mathbf{c} - \mathbf{a}) \\ \beta(\mathbf{a} - \mathbf{b}) + \gamma(\mathbf{a} - \mathbf{c}) + t\mathbf{d} = \mathbf{a} - \mathbf{p} \\ \begin{bmatrix} \mathbf{a} - \mathbf{b} & \mathbf{a} - \mathbf{c} & \mathbf{d} \end{bmatrix} \begin{bmatrix} \beta \\ \gamma \\ t \end{bmatrix} = \begin{bmatrix} \mathbf{a} - \mathbf{p} \end{bmatrix} \\ \begin{bmatrix} x_a & x_b & x_a & x_c & x_d \\ y_a & -y_b & y_a & -y_c & y_d \\ z_a & z_b & z_a & -z_c & z_d \end{bmatrix} \begin{bmatrix} \beta \\ \gamma \\ t \end{bmatrix} = \begin{bmatrix} x_a & x_p \\ y_a & -y_p \\ z_a & -z_p \end{bmatrix} \\ \begin{array}{c} \textbf{9} \text{ subtractions} \\ \textbf{Pre-calculate} \\ \textbf{entries and} \\ \textbf{rename:} & \begin{bmatrix} a & d & g \\ b & e & h \\ c & f & i \end{bmatrix} \begin{bmatrix} \beta \\ \gamma \\ t \end{bmatrix} = \begin{bmatrix} j \\ k \\ l \end{bmatrix} \end{array}$$

### Barycentric Ray-Triangle Intersection



Assume (conservatively) that on average, we calculate  $\beta$  and determine that it doesn't intersect (because  $\beta < 0$  or  $\beta > 1$ )

> = 2,836,684,800 = 2.8 GFLOPs

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A typical laptop can currently can do about 100-200 GFLOPS gigaflops per second

so what's the problem?

https://polycount.com/discussion/comment/2742856/

<u>#Comment\_2742856</u>

for each pixel: 720p = 1280×720 = 921600 pixels
for each triangle: computer game model: 40k triangles
 compute barycentric intersection 27 flops

= 995,328,000,000 = 995 GFLOPs ~= 1 TFLOP

Want to render this for an interactive game? Simply do this 30+ times per second.

# What can we do?

- Optimize the inner-inner loop: more efficient intersection routines
- ✓• Carefully reduce triangle count

these only go so far...

- Intersect fewer things
  - Most ray intersections don't hit the object!
  - Basic strategy: efficiently find big chunks of the scene that definitely **don't** intersect your ray

# **Bounding Volumes**

- Quick way to avoid intersections: bound object with a simple volume
  - -Object is fully contained in the volume
  - -If it doesn't hit the volume, it doesn't hit the object
  - -So test bvol first, then test object if it hits



**Chapter 12.3.1** 

# **Bounding Volumes**

**Chapter 12.3.1** 



# **Bounding Volumes**

**Chapter 12.3.1** 

Algorithm: if ray intersects bounding volume: if ray intersects object: do stuff

Cost: more for hits and near misses, but less for far misses

Is this worth it?

- bvol intersection should be much cheaper than object intersection
  - works best for simple bvols, complicated objects
- bvol should bound object as tightly as possible

#### Tradeoff: efficient intersection vs tightness

#### Chapter 12.3.2

### **Bounding Volume Hierarchy**

- Bvols around objects *might* help
- Bvols around groups of objects will help
- Bvols around parts of complex objects will help
- Idea: use bounding volumes all the way from the whole scene down to groups of a few objects

# **Building the Hierarchy**

- Ideally: bound nearby clusters of objects
- Practical solution: partition along axis

#### **BVH construction example**



#### **BVH ray-tracing example**



# Implementation

- New kind of object: BoundedObject
  - stores references to contained objects (may be BoundedObjects themselves!)
- New ray\_intersect routine for BoundedObject:
  - Intersect with each child; if any, return closest.

#### **Chapter 12.3.3**

# Other Approaches:

Uniform Space Subdivision



### **Uniform Space Subdivision**



• Grid cells store references to overlapping objects

# Compute the grid cells intersected by a ray

Constant offset between cell edge intersections in each dimension:



### Problems: AABB Construction and Intersection

How do we intersect with an axis-aligned bounding box (AABB)?

### **Construction**:

#### Intersection:

- AABB for a sphere
- AABB for a triangle
- AABB for a collection of AABBs

- 1D: intersect a slab
- 3D: intersect the intersection of 3 slabs