

Logistics: Final Project

- Project proposals due tonight
 - Ideally you will have done enough investigation to conclude that your plan is achievable.
 - Err on the side of ambition
 - Late addition: include any **resources** you have used or plan to use
- Slip days can't be used on any final project deadline
- Beware Canvas grade averages

Logistics: Exam

- Exam out today
 - Do not discuss with anyone; do not use resources other than those linked from the course webpage

A2 Artifact Results!

• 4 winners (1 first and 3 tied for second place)

Second place (tied)

Dylan Thompson

Second place (tied)

Raleigh Hanson



Second place (tied)

John-Paul Powers



First Place - Nicholas Uhlhorn



Goals

- Know how to draw lines using point sampling, and why this causes variable apparent line widths.
- Know how to draw lines with slope between 0 and 1 using the midpoint algorithm.
- Know how to draw lines with any slope by adjusting the inputs to the midpoint algorithm.
- Know how to interpolate arbitrary quantities across a line drawn using the midpoint algorithm.

Graphics Pipeline: Overview



Remember Wireframe?







M = M_{vp} M_{proj} M_{view} M_{model}
for each line segment a_i, b_i
p = M a_i
q = M b_i
draw_line(p, q) How do we do this?

Line Drawing

This is a **rasterization** problem: given a primitive (line segment), generate fragments (aspiring pixels)







What makes a line good?

Rasterizing lines - possible definition

- Define line as a rectangle
- Specify by two endpoints
- Ideal image: black inside, white outside

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Point sampling

- Approximate
 rectangle by drawing
 all pixels whose
 centers fall within the
 line
- Problem: sometimes turns on adjacent pixels

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Point sampling in action



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Bresenham lines (midpoint alg.)

- Point sampling unit width rectangle leads to uneven line width
- Define line width parallel to pixel grid
- That is, turn on the single nearest pixel in each column
- Note that 45° lines are now thinner

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Midpoint algorithm in action

Point sampling in action



Notes: Midpoint Algorithm

Midpoint Algorithm

- line equation:
 y = b + m x
- Simple algorithm: evaluate line equation per column
- W.I.o.g. $x_0 < x_1$; $0 \le m \le 1$

Algorithm:



Midpoint Algorithm

- line equation:
 y = b + m x
- Simple algorithm: evaluate line equation per column
- W.I.o.g. $x_0 < x_1$; $0 \le m \le 1$

Algorithm:

// compute m, b

```
for x = ceil(x0) to floor(x1)
  y = b + m*x
  // Ex: what goes here?
```



Algorithms for drawing lines

- line equation:
 y = b + m x
- Simple algorithm: evaluate line equation per column
- W.I.o.g. $x_0 < x_1$; $0 \le m \le 1$

Algorithm:

// compute m, b

```
for x = ceil(x0) to floor(x1)
  y = b + m*x
  draw(x, round(y))
```



Optimizing Line Drawing

Can we take stuff out of the inner loop?

Exercise: optimize this

```
function slow_line(p1, p2):
    // compute m, b
    for x = ceil(x0) to floor(x1)
        y = b + m*x
        draw(x, round(y))
```

function fast_line(p1, p2): // compute m, b

for x = ceil(x0) to floor(x1)

draw(x, round(y))

Optimizing Line Drawing Even More

- Rounding is slow too
- At each pixel the only options are E and NE
- Track distance to line:
 - -d = m(x + 1) + b y
 - d > 0.5 decides
 between E and NE



Optimizing Line Drawing Even More

- d = m(x + 1) + b y
- Only need to update d for integer steps in x and y
- Do that with addition
- Known as "DDA" (digital differential analyzer)



Linear interpolation

- We often attach attributes to vertices
 - e.g. computed diffuse color of a hair being drawn using lines
 want color to vary smoothly along a chain of line segments

 Same machinery as we used for y works for other values!



Rasterizing triangles

- Input:
 - three 2D points (the triangle's vertices in pixel space)
 - $(x_0, y_0); (x_1, y_1); (x_2, y_2)$
 - parameter values at each vertex
 - **q**₀₀, ..., **q**_{0n}; **q**₁₀, ..., **q**_{1n}; **q**₂₀, ..., **q**_{2n}
- Output: a list of fragments, each with
 - the integer pixel coordinates (x, y)
 - interpolated parameter values q_0, \ldots, q_n

Rasterizing triangles

- Summary
 - I evaluation of linear functions on pixel grid
 - 2 functions defined by parameter values at vertices
 - 3 using extra
 parameters
 to determine
 fragment set



Incremental linear evaluation

- A linear (affine, really) function on the plane is: $q(x, y) = c_x x + c_y y + c_k$
- Linear functions are efficient to evaluate on a grid:

$$q(x+1,y) = c_x(x+1) + c_y y + c_k = q(x,y) + c_x$$
$$q(x,y+1) = c_x x + c_y(y+1) + c_k = q(x,y) + c_y$$



Pixel-walk (Pineda) rasterization

- Conservatively visit a superset of the pixels you want
- Interpolate linear functions
 - barycentric coords
 (determines when to emit a fragment)
 - colors
 - normals
 - whatever else!

