

Logistics: Final Project

- Project proposals due tonight
	- Ideally you will have done enough investigation to conclude that your plan is achievable.
	- Err on the side of ambition
	- Late addition: include any **resources** you have used or plan to use
- Slip days can't be used on any final project deadline
- Beware Canvas grade averages

Logistics: Exam

- Exam out today
	- Do not discuss with anyone; do not use resources other than those linked from the course webpage

A2 Artifact Results!

• 4 winners (1 first and 3 tied for second place)

Second place (tied)

Dylan Thompson

O

Second place (tied)

Raleigh Hanson

Second place (tied)

John-Paul Powers

First Place - Nicholas Uhlhorn

Goals

- Know how to draw lines using point sampling, and why this causes variable apparent line widths.
- Know how to draw lines with slope between 0 and 1 using the midpoint algorithm.
- Know how to draw lines with any slope by adjusting the inputs to the midpoint algorithm.
- Know how to interpolate arbitrary quantities across a line drawn using the midpoint algorithm.

Graphics Pipeline: Overview

Remember Wireframe?

 $M = M_{VP} M_{proj} M_{view} M_{model}$ for each line segment **a**i**, b**ⁱ $p = M a_i$ $q = M b_i$ draw $line(p, q)$ How do we do this?

Line Drawing

This is a **rasterization** problem: given a primitive (line segment), generate fragments (aspiring pixels)

What makes a line good?

Rasterizing lines - possible definition

- Define line as a rectangle
- Specify by two endpoints
- Ideal image: black inside, white outside

Point sampling

- Approximate rectangle by drawing all pixels whose centers fall within the line
- Problem: sometimes turns on adjacent pixels

Point sampling in action

Bresenham lines (midpoint alg.)

- Point sampling unit width rectangle leads to uneven line width
- Define line width parallel to pixel grid
- That is, turn on the single nearest pixel in each column
- Note that 45° lines are now thinner

Midpoint algorithm in action

Point sampling in action

Notes: Midpoint Algorithm

Midpoint Algorithm

- line equation: $y = b + m x$
- Simple algorithm: evaluate line equation per column
- W.l.o.g. $x_0 < x_1$; $0 \leq m \leq 1$

Algorithm:

Midpoint Algorithm

- line equation: $y = b + m x$
- Simple algorithm: evaluate line equation per column
- W.l.o.g. $x_0 < x_1$; $0 \leq m \leq 1$

Algorithm:

// compute m, b

```
for x = ceil(x0) to floor(x1)y = b + m \cdot xEx: what goes here?
```


Algorithms for drawing lines

- line equation: $y = b + m x$
- Simple algorithm: evaluate line equation per column
- W.l.o.g. $x_0 < x_1$; $0 \leq m \leq 1$

Algorithm:

// compute m, b

for $x = ceil(x0)$ to floor $(x1)$ $y = b + m \cdot x$ $draw(x, round(y))$

Optimizing Line Drawing

Can we take stuff out of the inner loop?

Exercise: optimize this

```
function slow_line(p1, p2):
// compute m, b
for x = ceil(x0) to floor(x1)y = b + m \cdot xdraw(x, round(y))
```
function fast_line(p1, p2): // compute m, b

for $x = ceil(x0)$ to floor($x1$)

 $draw(x, round(y))$

Optimizing Line Drawing Even More

- Rounding is slow too
- At each pixel the only options are E and NE
- Track distance to line:
	- $d = m(x + 1) + b y$
	- *d* > 0.5 decides between E and NE

Optimizing Line Drawing Even More

- $d = m(x + 1) + b y$
- Only need to update *d* for integer steps in *x* and *y*
- Do that with addition
- Known as "DDA" (digital differential analyzer)

Linear interpolation

- We often attach attributes to vertices
	- e.g. computed diffuse color of a hair being drawn using lines
	- want color to vary smoothly along a chain of line segments

• Same machinery as we used for y works for other values!

Rasterizing triangles

- Input:
	- three 2D points (the triangle's vertices in pixel space)
		- $(x_0, y_0); (x_1, y_1); (x_2, y_2)$
	- parameter values at each vertex
		- *q*00, …, *q*⁰*n*; *q*10, …, *q*¹*n*; *q*20, …, *q*²*ⁿ*
- Output: a list of fragments, each with
	- the integer pixel coordinates (*x*, *y*)
	- interpolated parameter values *q*0, …, *qn*

Rasterizing triangles

- Summary
	- evaluation of linear functions on pixel grid
	- 2 functions defined by parameter values at vertices
	- 3 using extra parameters to determine fragment set

Incremental linear evaluation

- A linear (affine, really) function on the plane is: $q(x, y) = c_x x + c_y y + c_k$
- Linear functions are efficient to evaluate on a grid:

$$
q(x + 1, y) = c_x(x + 1) + c_y y + c_k = q(x, y) + c_x
$$

$$
q(x, y + 1) = c_x x + c_y (y + 1) + c_k = q(x, y) + c_y
$$

Pixel-walk (Pineda) rasterization

- Conservatively visit a superset of the pixels you want
- Interpolate linear functions
	- barycentric coords (determines when to emit a fragment)
	- colors
	- normals
	- whatever else!

