Computer Graphics

Lecture 22
The Graphics Pipeline
Announcements
Mid-Late Term Exam

- Take-home exam out Friday 11/4
  Due Monday 11/7 at 10pm.

- Similar to the homeworks, but no collaboration and no google.
  - Book is ok. Writing code is ok.
Final Project

- Group formation due Wednesday
- Proposals due Friday
Questions?
Goals

• Understand the basic phases of "The Graphics Pipeline"

• Know how to perform hidden surface removal

• Know how to use z-buffering to handle occlusion, and why this is used instead of the painter's algorithm.

• Know how the near and far planes affect z buffer precision, and why we use $1/z$ instead of $z$ for interpolating.
Graphics Pipeline: Overview

you are here ➔ APPLICATION

COMMAND STREAM

3D transformations; shading ➔ VERTEX PROCESSING

TRANSFORMED GEOMETRY

conversion of primitives to pixels ➔ RASTERIZATION

FRAGMENTS

blending, compositing, shading ➔ FRAGMENT PROCESSING

FRAMEBUFFER IMAGE

user sees this ➔ DISPLAY
Application sends geometric primitives to renderer (e.g., to GPU)

Vertices are transformed to image space (we've done lots of this!)

Primitives are converted into pixel-shaped "fragments"; values are interpolated across primitives.

Fragments are shaded, blended, and composited to determine pixel colors.

Pixel colors written to the framebuffer appear on the screen.
Command Stream

Application sends geometric primitives to renderer (e.g., to GPU)

What primitives?

- Points
- Line segments
  - and chains of connected line segments
- Triangles
- And that’s all!
  - Curves? Approximate them with chains of line segments
  - Polygons? Break them up into triangles
  - Curved surfaces? Approximate them with triangles
- Trend over the decades: toward minimal primitives
  - simple, uniform, repetitive: good for parallelism
Vertex Processing

Vertices are transformed to clip space
Vertex values are computed
(we've done most of this!)
Rasterization algorithms: starting Friday

- First job: enumerate the pixels covered by a primitive
  - which pixels fall inside triangle?
  - includes "clipping" content outside view volume
- Second job: interpolate values across the primitive
  - e.g. colors computed at vertices
  - e.g. normals at vertices
  - e.g. texture coordinates
Fragment Processing

*Painter's algorithm; Z buffering: today*

- Hidden surface removal (occlusion) - only the closest object is drawn
- Per-fragment shading:
  - determine color of the pixel based on a shading model
  - diffuse color might come from a texture
- Blending, compositing - e.g.:
  - anti-aliasing
  - transparency / alpha blending
Hidden Surface Removal

Two motivations: realism and efficiency
Back face culling

- For closed shapes you will never see the inside
  - therefore only draw surfaces that face the camera
  - implement by checking $\mathbf{n} \cdot \mathbf{v} > 0$
Back face culling

• For closed shapes you will never see the inside
  – therefore only draw surfaces that face the camera
  – implement by checking $\mathbf{n} \cdot \mathbf{v} > 0$

Q: In which space would you prefer to do backface culling?

A: Model
B: World
C: Camera
D: Clip (/NDC/CVV)
Handling Occlusion

• What if multiple triangles are facing the viewer at different depths?

How would you deal with this?
Handling Occlusion

• What if multiple triangles are facing the viewer at different depths?

• **Painter's algorithm**: draw them back-to-front

• Topological sort on the occlusion graph:
  • if A ever occludes B, it must come after B in the drawing order

Works great if the ordering is easy to find...

... but often it isn't.

**Example: z.obj**
The z buffer

- In many (most) applications maintaining a z sort is too expensive
  - changes all the time as the view changes
  - many data structures exist, but complex
- Solution: draw in any order, keep track of closest
  - allocate extra channel per pixel to keep track of closest depth so far
  - when drawing, compare object’s depth to current closest depth and discard if greater
  - this works just like any other compositing operation
The z buffer

- another example of a memory-intensive brute force approach that works and has become the standard
- store z as an integer for speed and memory efficiency (at the expense of precision!)
Precision in z buffer: Throwback

\[
P = \begin{bmatrix}
  n & 0 & 0 & 0 & 0 \\
  0 & n & 0 & 0 & 0 \\
  0 & 0 & n + f & -fn & 0 \\
  0 & 0 & 1 & 0 & 0
\end{bmatrix}
\]

- The precision is distributed between the near and far clipping planes
  - this is why these planes have to exist
  - also why you can’t always just set them to very small and very large distances

- Generally use \( z' \) (not world \( z \)) in z buffer
Interpolating in projection

linear interp. in screen space ≠ linear interp. in world (eye) space

instead of using the smallest $z$, use the largest $1/z$
How did this happen?

Instead of using the smallest $z'$, use the largest $\frac{1}{z'}$. 

$z' = f + n - \frac{fn}{z}$

$z' = k_1 - k_2 \frac{1}{z}$

$z' \propto -1 \frac{1}{z}$

$z \propto -1 \frac{1}{z'}$
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