

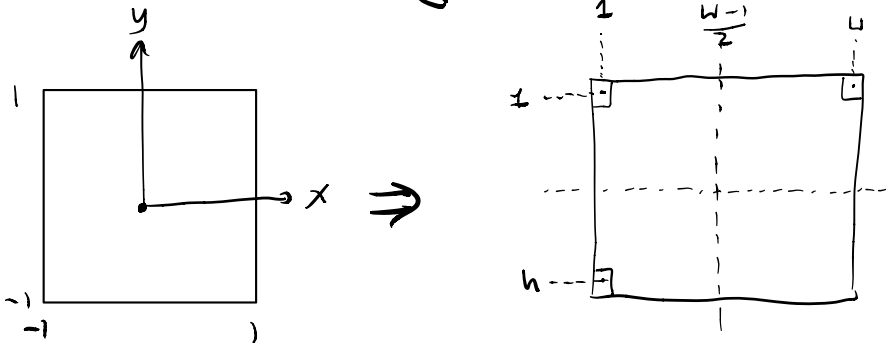
# Viewport Matrix

$$\text{In: } x, y, z \in [-1, 1]^3$$

$$\text{Out: } x \in [1, w]$$

$$y \in [1, h]$$

$$z \in [-1, 1] \text{ (unchanged)}$$



1. Scale  $x, y$

$$x: \frac{w-1}{2}$$

$$y: \frac{h-1}{2} \text{ (flipped!)}$$

2. Translate

$$0, 0 \rightarrow \frac{w-1}{2}, \frac{h-1}{2}$$

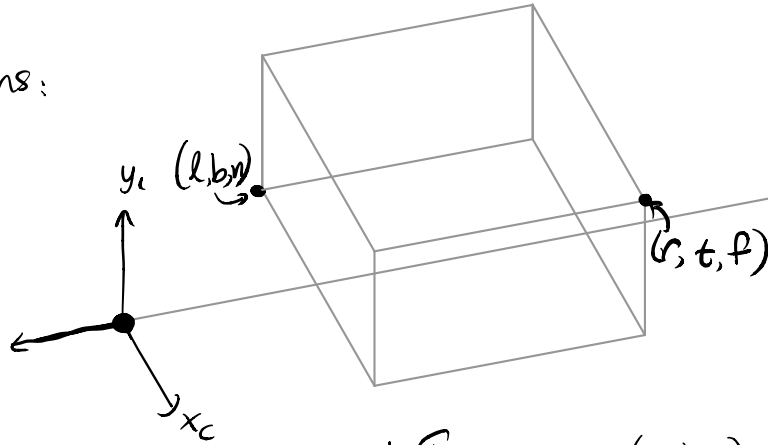
# Projection Matrix: Orthographic

In: camera coordinates

Out:  $x, y, z$  in  $[-1, 1]^3$

Viewport dims:

$x = l$   
 $x = r$   
 $y = b$   
 $y = t$   
 $z = n$   
 $z = f$



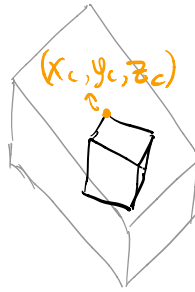
1. Translate  $(l, b, n) \rightarrow (0, 0, 0)$

2. Scale  $r-l \rightarrow 2$   
 $t-b \rightarrow 2$   
 $f-n \rightarrow 2$

3. Translate  $(1, 1, 1) \rightarrow (0, 0, 0)$

# Camera Matrix

Given:  $\vec{u}, \vec{v}, \vec{w}, \vec{p}$



$$\begin{bmatrix} x_w \\ y_w \\ z_w \end{bmatrix} = x_c \vec{u} + y_c \vec{v} + z_c \vec{w} + \vec{p}$$

$$\begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix} = \begin{bmatrix} \vec{u} & \vec{v} & \vec{w} & \vec{p} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_c \\ y_c \\ z_c \\ 1 \end{bmatrix}$$

↪ frame-to-canonical!

Canonical-to-frame?  
↪ orthogonal

$$\text{inv} \left( \begin{array}{c} \boxed{\vec{u} \quad \vec{v} \quad \vec{w}} \quad \vec{p} \\ 0 \quad 0 \quad 0 \quad 1 \end{array} \right)$$

$$\begin{bmatrix} Q & p \\ 0 & 1 \end{bmatrix}^{-1} = \begin{bmatrix} \vec{u}^T & -\vec{u}^T p_x \\ \vec{v}^T & -\vec{v}^T p_y \\ \vec{w}^T & -\vec{w}^T p_z \\ 0 & 1 \end{bmatrix}$$