

# Computer Graphics

Lecture 9  
**Specular Shading**  
**Shadows**

# Announcements

- Watch 2 videos before class on Monday:

L10A, L10B

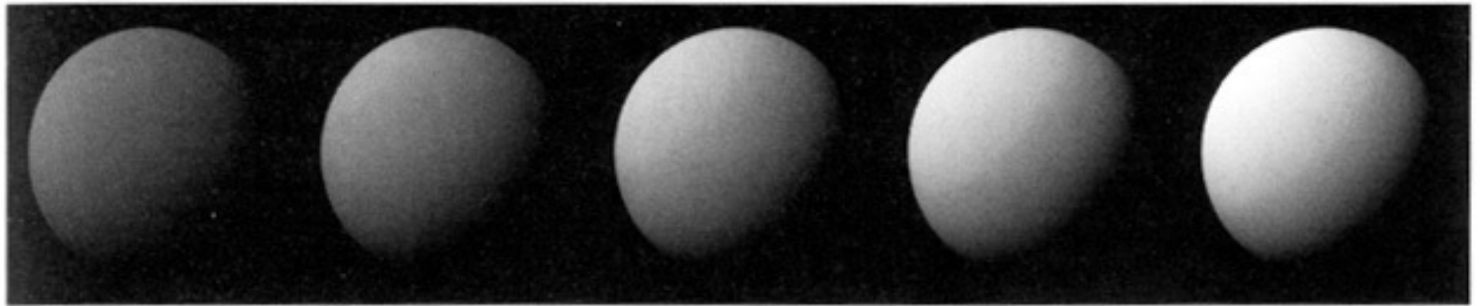
- A1, HW1 due Monday
- A2, HW2 out Monday

- must work with a different partner than A1

Start pairing now! must have partner by Tuesday

# Diffuse (Lambertian) Shading

$$L_d = k_d I \max(0, \vec{n} \cdot \vec{\ell})$$



[Foley et al.]

$k_d$   $\longrightarrow$

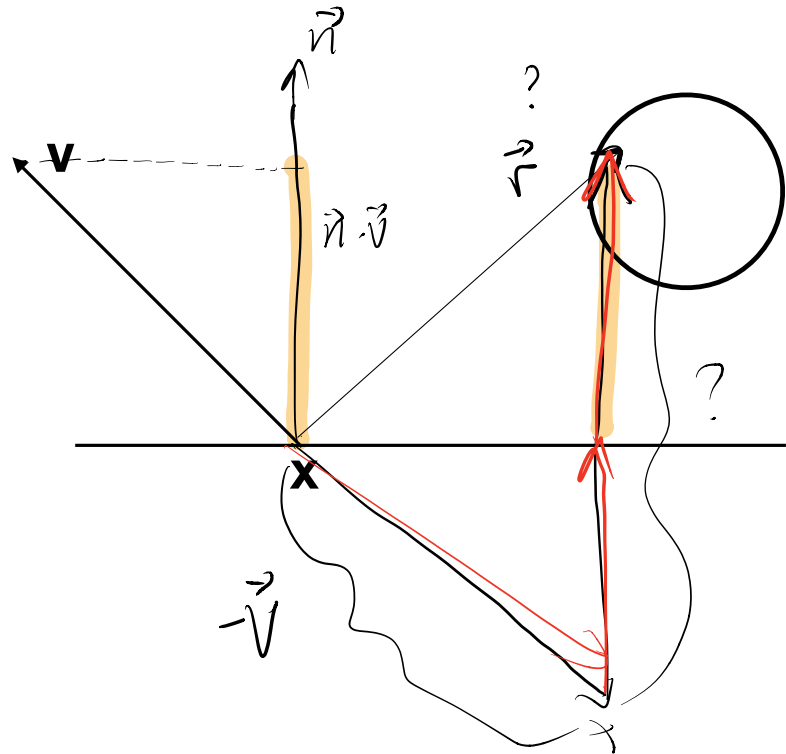
For colored objects,  $k_d$  is a 3-vector of R, G, and B reflectances.

# Mirror Reflection

What does a camera see when it looks at a mirror? 

A

$$\vec{c} = -v + 2 \cdot (\vec{n} \cdot \vec{v}) \vec{n}$$

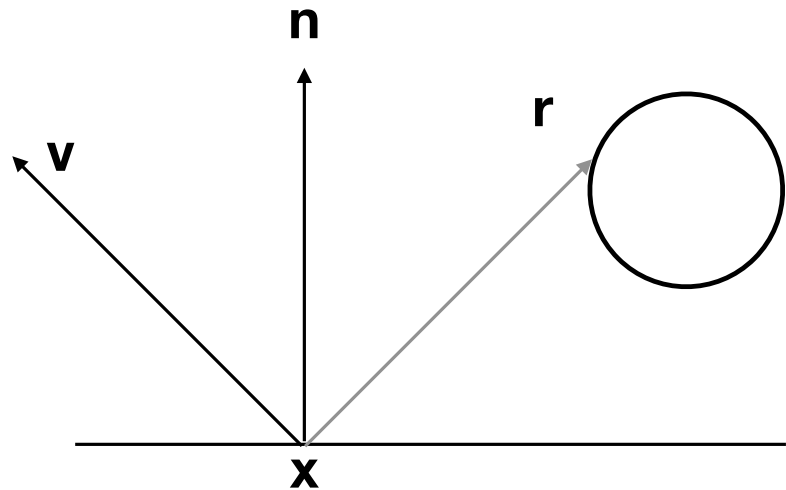


# Mirror Reflection

What does a camera see when it looks at a mirror? 

From last time:

$$\vec{r} = -\vec{v} + 2(\vec{v} \cdot \vec{n})\vec{n}$$



Hint: 

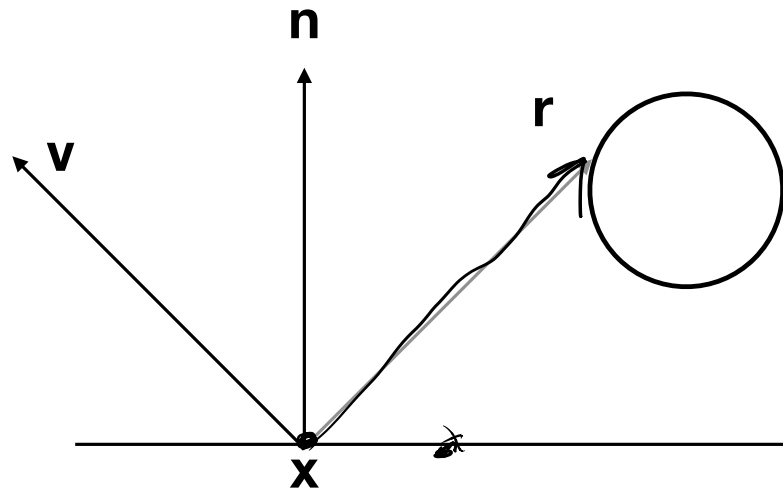
How do we do this using the tools we already have?

# Mirror Reflection

What does a camera see when it looks at a mirror? 

From last time:

$$\vec{r} = -\vec{v} + 2(\vec{v} \cdot \vec{n})\vec{n}$$



`mirr_ray.origin = x`  
`mirr_ray.direction = r`  
`color = traceray(scene,`

Hint: 

small value to avoid hitting the surface x lies on

`mirr_ray,` `epsilon`, `Inf`):  
*t<sub>min</sub>* *t<sub>max</sub>*

# Recursion!?

```
traceray(ray, scene):
```

```
    t, rec = find_intersection(ray, scene)
```

```
    if rec.obj is a mirror:
```

```
        ↪ compute r, the reflection direction
```

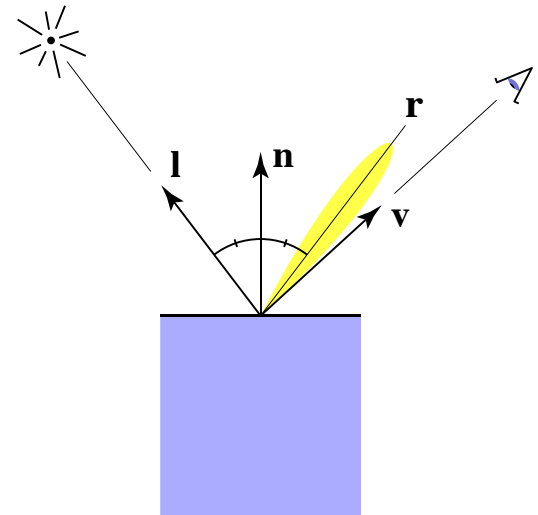
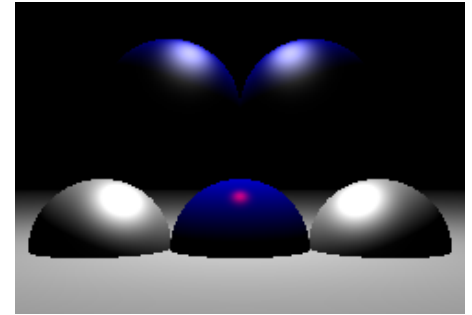
```
        ↪ mirror_ray = Ray(rec.x, r)
```

```
        return traceray(mirror_ray, scene)
```

```
    # other cases, ...
```

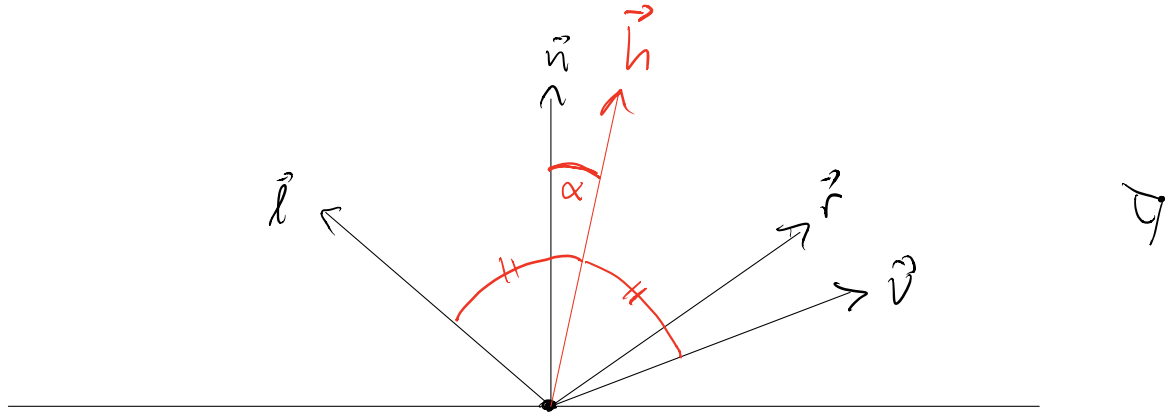
# Specular Reflection

- What about non-mirror shiny surfaces?
- They appear brighter *near* "mirror" configuration
- Phong reflection: specular reflection is a function of angle between  $\mathbf{r}$  and  $\mathbf{v}$ .





# Phong Reflection



Phong Reflection

Intuitive:  $f(\vec{r}, \vec{v}) = f(\cos \alpha) = (\vec{r} \cdot \vec{v})^p$

Blinn-Phong Reflection

Alternative:  $f(\vec{h}, \vec{n}) = \dots (\vec{h} \cdot \vec{n})^p$

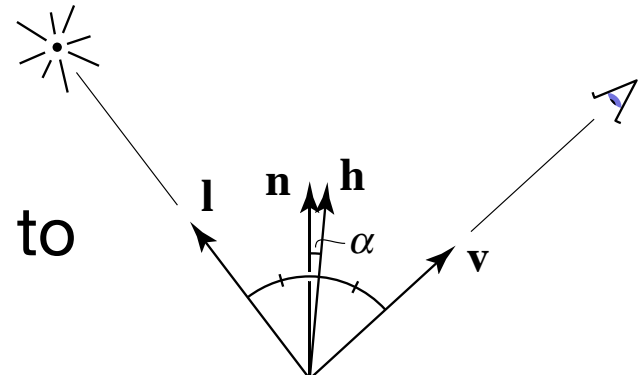


# Specular Reflection

- Blinn-Phong: specular reflection is a function of angle between (**half-way vector** between view and light) and (the **normal**).

- $h = \text{bisector}(\mathbf{v}, \mathbf{l})$

- Reflected light proportional to



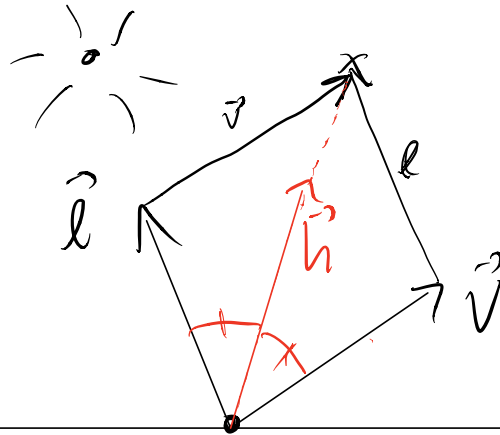
$$k_s \max(0, \vec{n} \cdot \vec{h})^p$$

specular coefficient:  
determines strength of  
specularity term

sharpness  
specular exponent:  
determines shininess

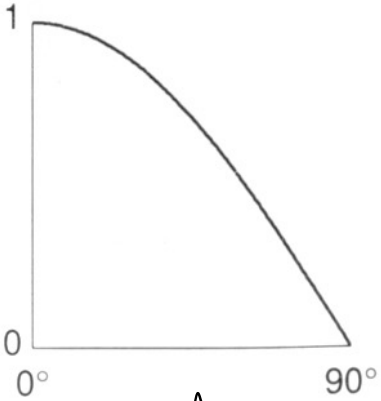
# Computing h

$$\text{bisector}(\vec{v}, \vec{\ell}) = \frac{\vec{\ell} + \vec{v}}{\|\vec{\ell} + \vec{v}\|}$$

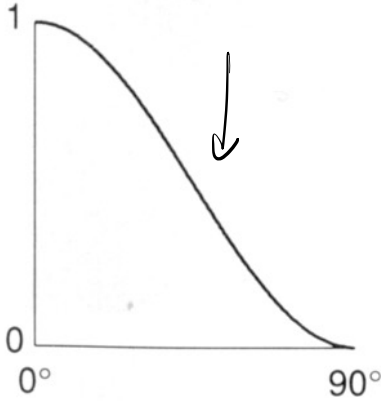


# Effect of $p$

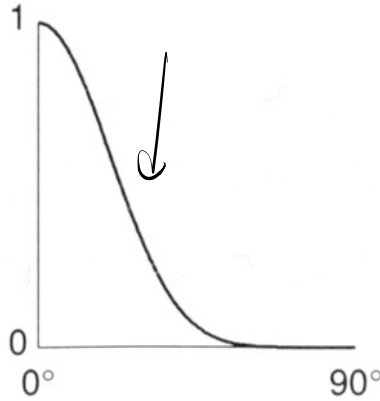
$\cos \alpha$



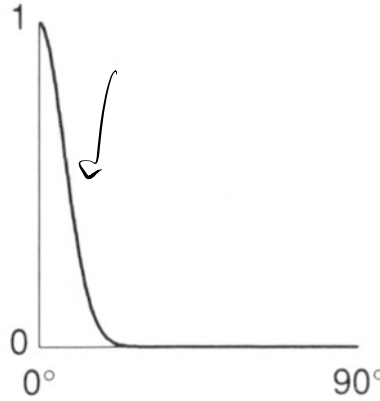
$\cos^2 \alpha$

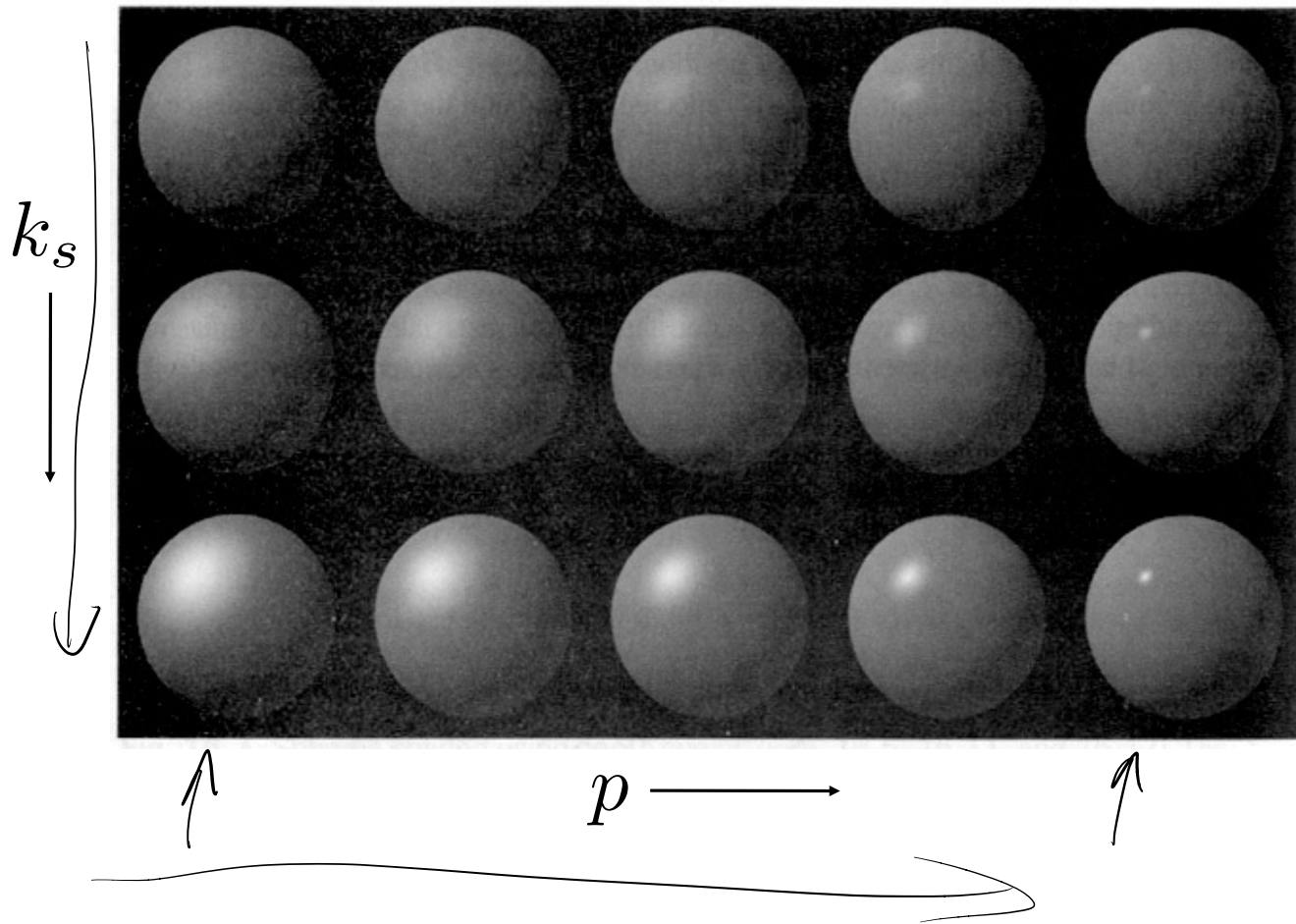


$\cos^8 \alpha$



$\cos^{64} \alpha$





# Putting it all Together: Blinn-Phong Reflection Model

Usually surfaces have both diffuse *and* specular components, so we'll combine the two:

$$\begin{aligned} \text{light reflected } L &= L_d + L_s \\ &= k_d I \max(0, \vec{n} \cdot \vec{l}) + k_s I \max(0, \vec{n} \cdot \vec{h})^p \end{aligned}$$

diffuse reflection      specular reflection

diffuse coefficient (surface brightness and color)

light intensity

normal

light direction

specular coefficient (strength [and color] of specularity)

half-vector between  $\mathbf{l}$  and  $\mathbf{v}$

specular exponent (sharpness of specularity)

In code: `function shade_light(light, hitrec, ...)`

# What if there are multiple lights?

Light is additive - add them together:

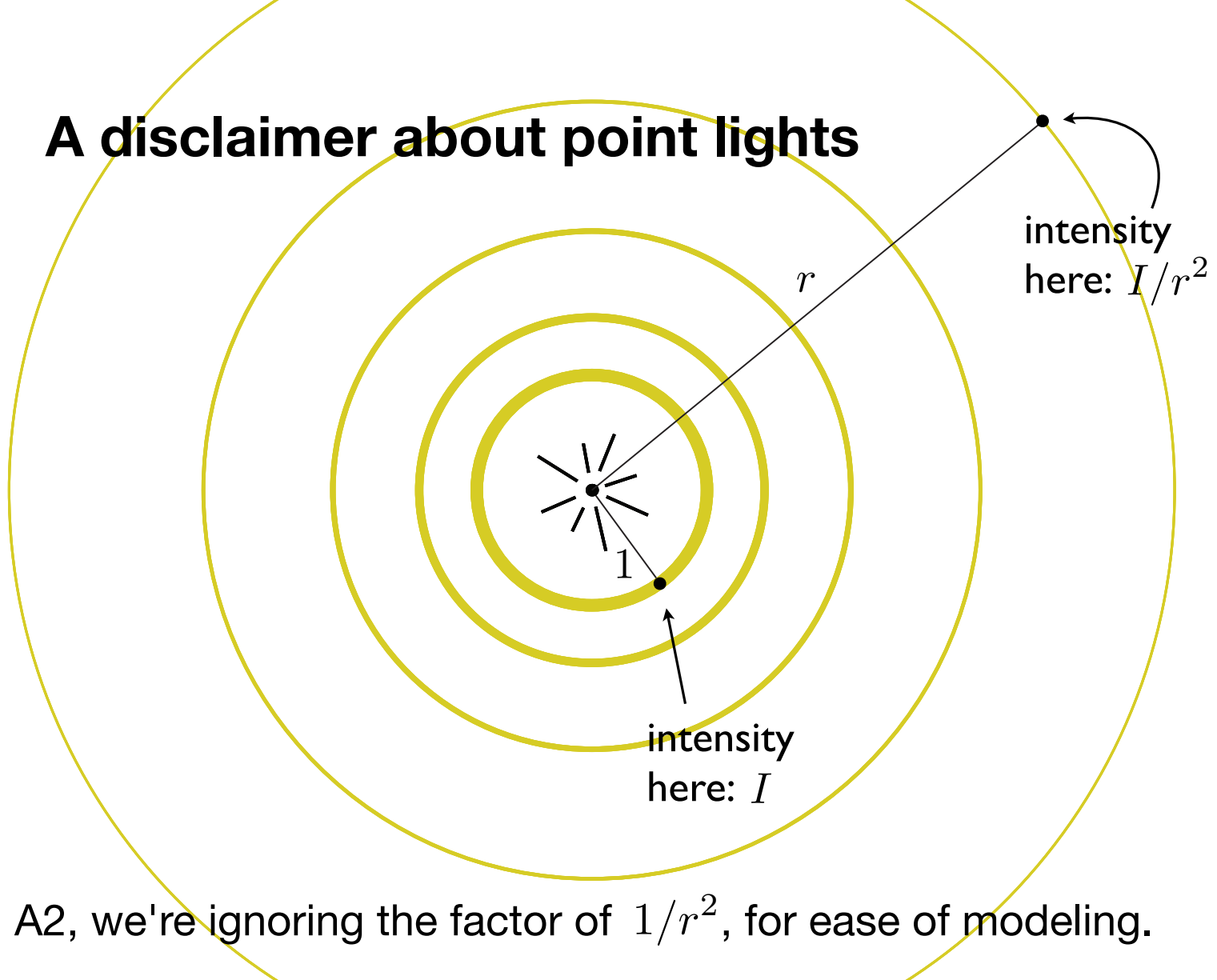
$$L = \sum_{i=1}^{\# \text{ lights}} k_d I \max(0, \vec{n} \cdot \vec{l}_i) + k_s I \max(0, \vec{n} \cdot \vec{h}_i)^p$$

In code:

```
function determine_color(hitrec, ray, scene, ...):  
    color = black  
    for light in scene.lights:  
        color += shade_light(light, hitrec, ...)
```



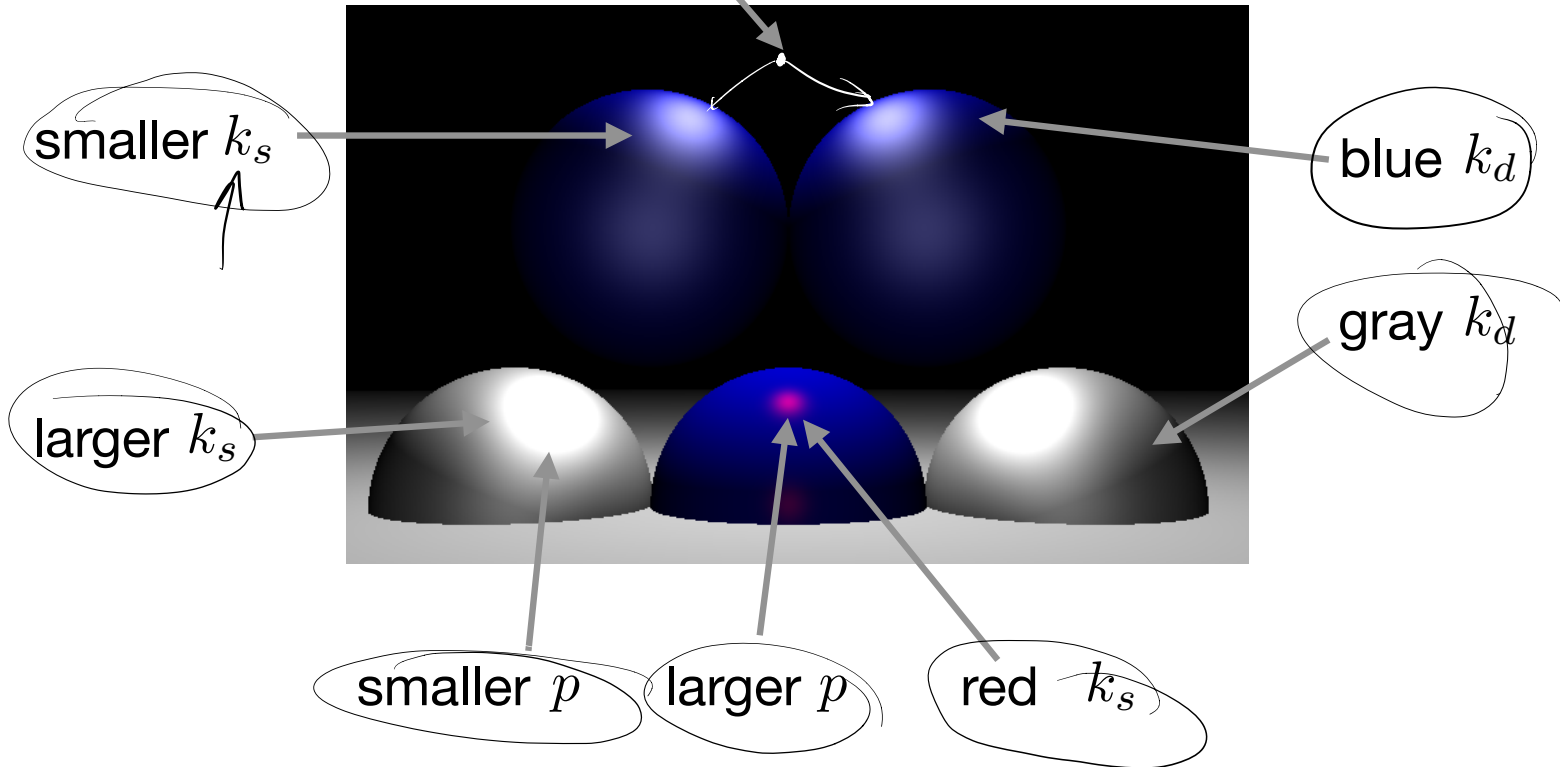
# A disclaimer about point lights



In A2, we're ignoring the factor of  $1/r^2$ , for ease of modeling.

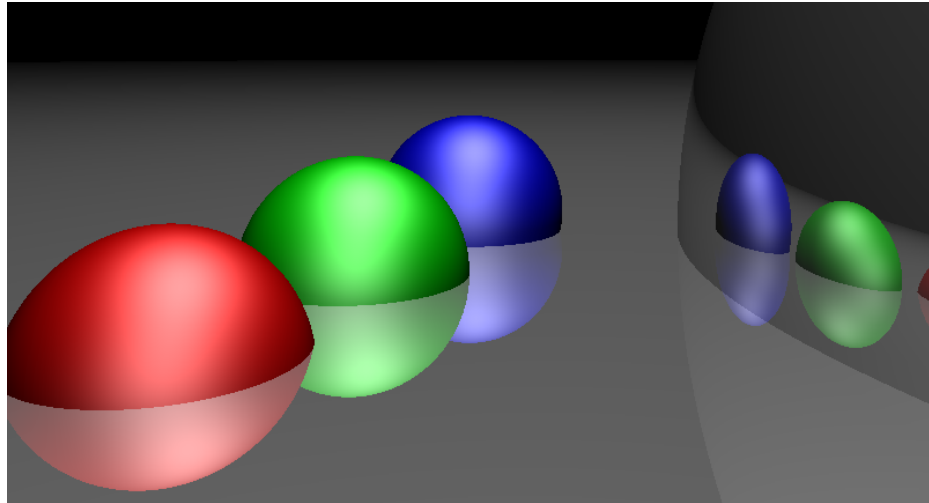
# Our images so far:

Point light

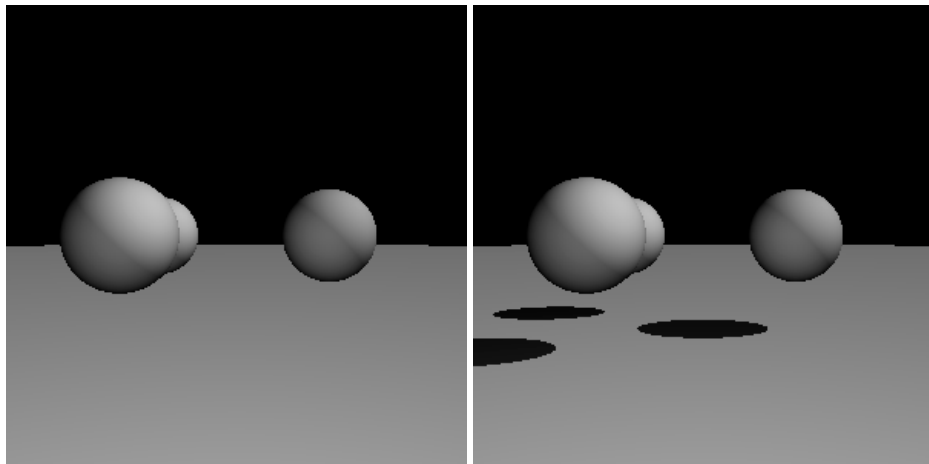


# What's next?

Mirror-reflective surfaces



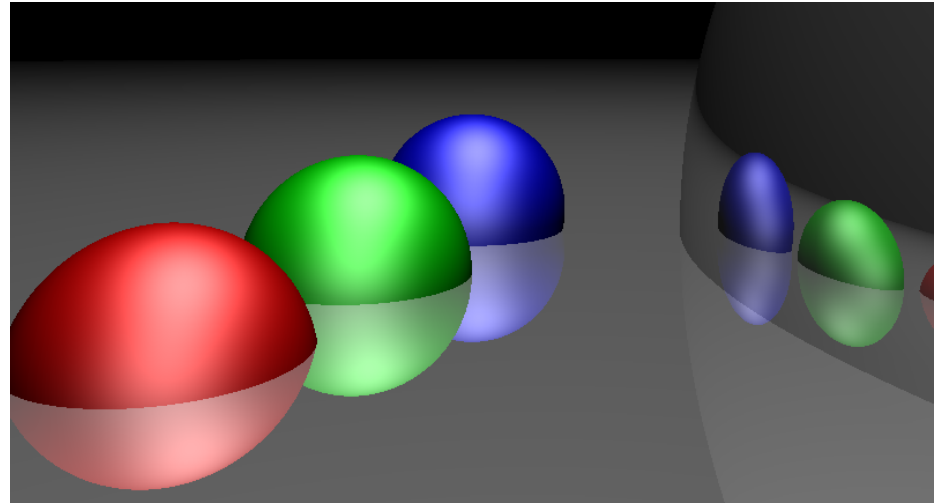
Shadows



# Partially-Mirrored Surfaces

Notice the floor is gray but also mirror-reflective.

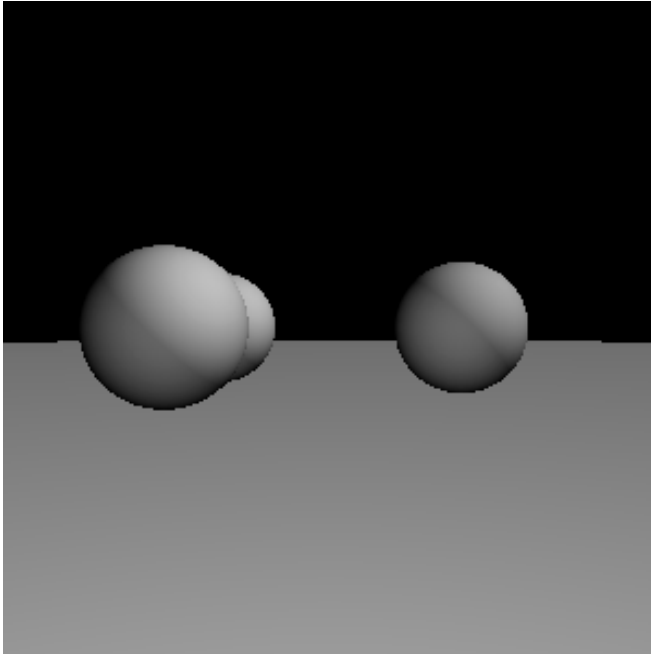
Materials store a **mirror coefficient**: fraction of light that is reflected in a mirror-like fashion



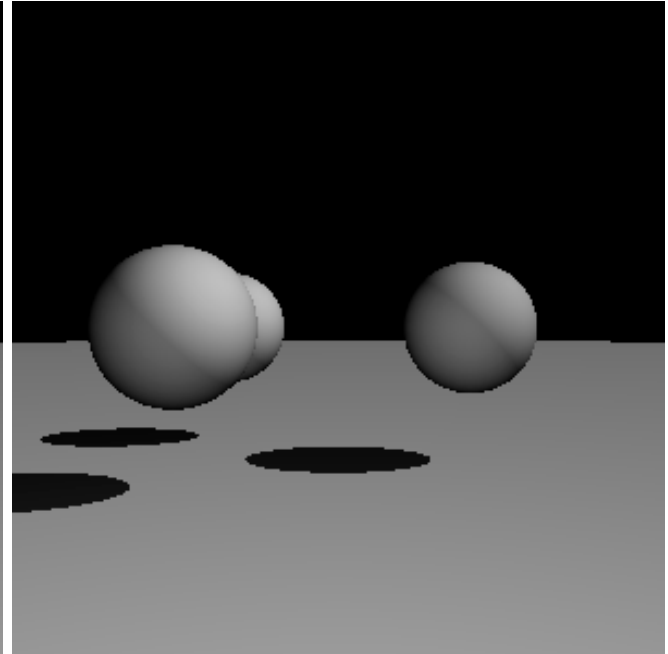
$$L = k_m L_r + (1 - k_m)(L_d + L_s)$$

mirror coefficient      mirror-reflected light      "local" color (Blinn-Phong)

# Shadows



Wrong

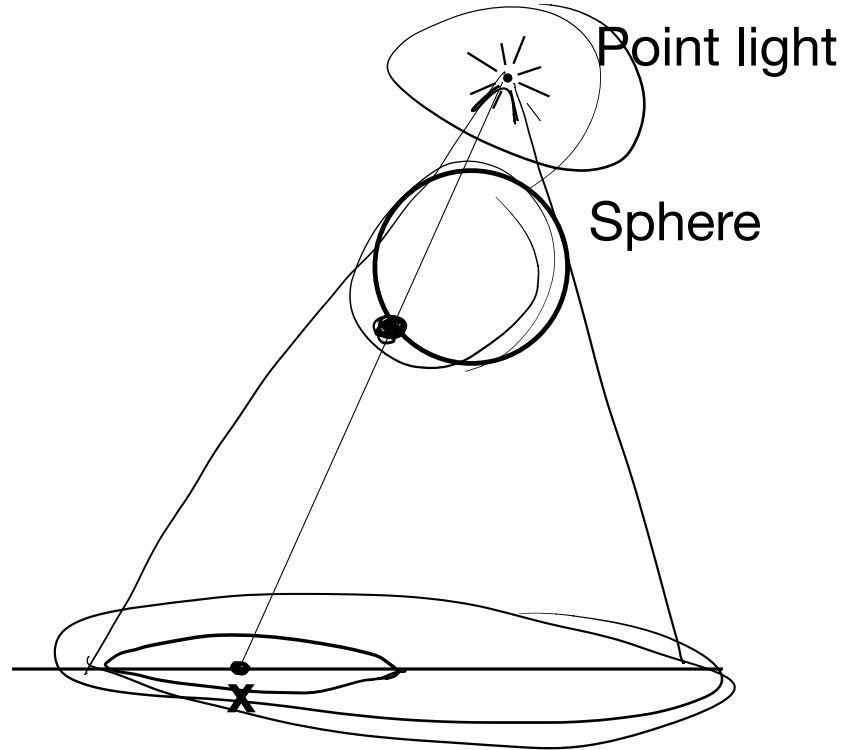


Less Wrong

# Shadows

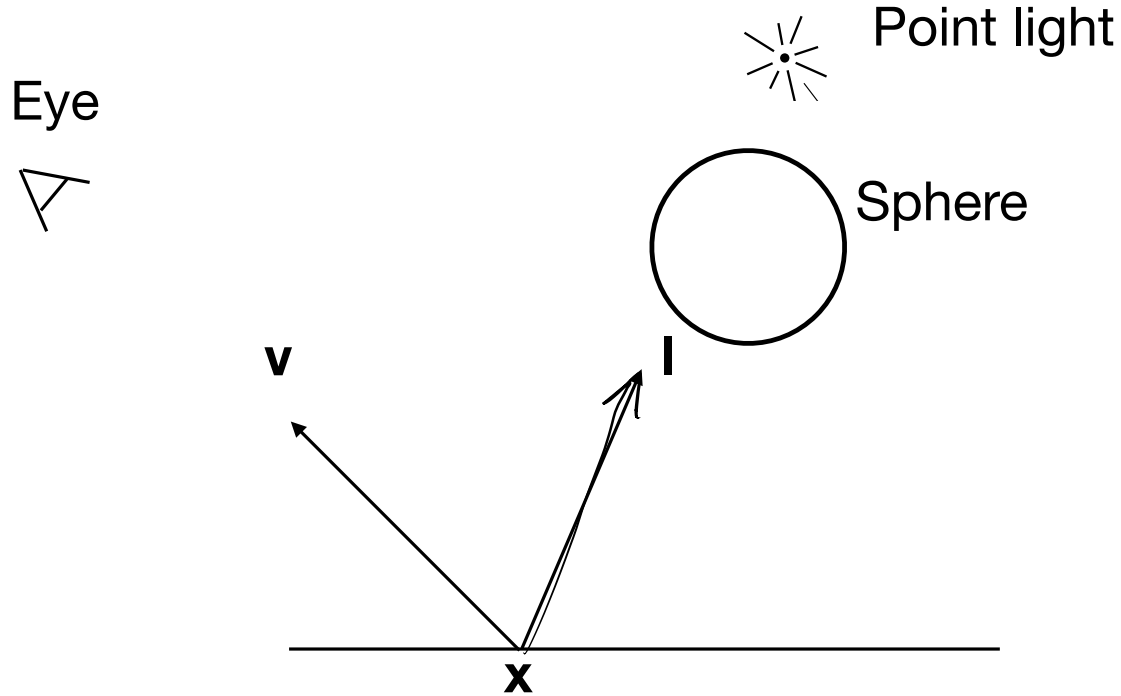
How can we tell if a point is in shadow?

Eye



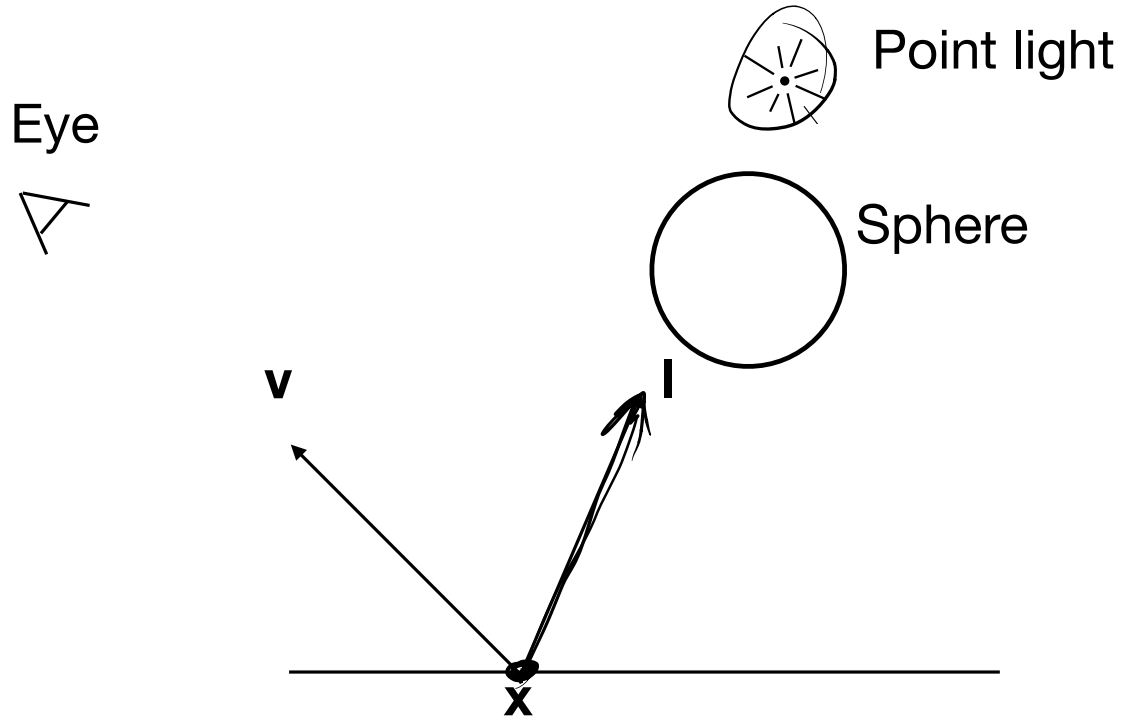
# Shadows

How can we tell if a point is in shadow?



# Shadows

How can we tell if a point is in shadow?



Point is shadowed iff:

`closest_intersect(objs, Ray( $\mathbf{x}$ ,  $\mathbf{l}$ ), tmin, tmax) != nothing`

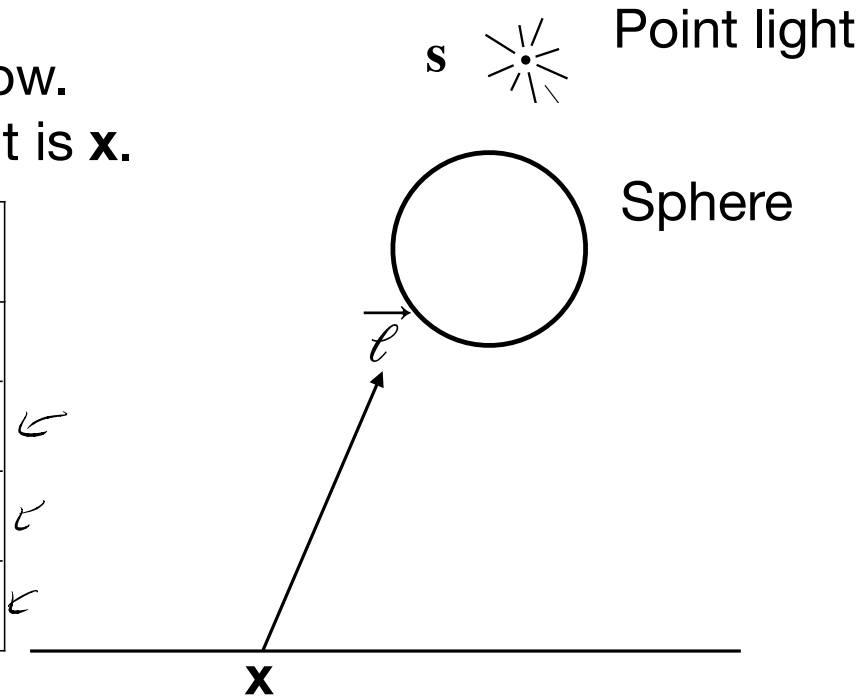


# Shadows

How can we tell if a point is in shadow?

**Problem:** Fill in the table below.  
Assume the intersection point is  $\mathbf{x}$ .

	Directional light $\vec{l}$	Point light S
<b>r.orig</b>	$\mathbf{x}$	$\mathbf{x}$
<b>r.dir</b>	$\vec{l}$	$\vec{s} - \vec{x}$
<b>tmin</b>	eps	eps
<b>tmax</b>	infinity	1



Point is shadowed iff:

`closest_intersect(objs, Ray(orig, dir), tmin, tmax) != nothing`

```
function determine_color(hitrec, ray, scene, ...):  
    color = black  
    for light in scene.lights:  
        if !is_shadowed(scene, light, hitrec)  
            color += shade_light(light, hitrec, ...)
```

# Next time...

## Let's talk about bunnies.



If we want bunnies, we still need to implement  
function `ray_intersect(ray, triangle, tmin, tmax):`

Then, we can treat a triangle mesh as simply a list of triangles.