



Computer Graphics

Lecture 1

Images and Vectors

or: I ordered an image and all I got was this grid of colored boxes

Announcements

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- HW0 and A0 out later today
 - Both due next Wednesday night

How do we graphics?

Let's design a simple graphics system.

The goal: draw a triangle on the screen.



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(why a triangle? more on this next time...)

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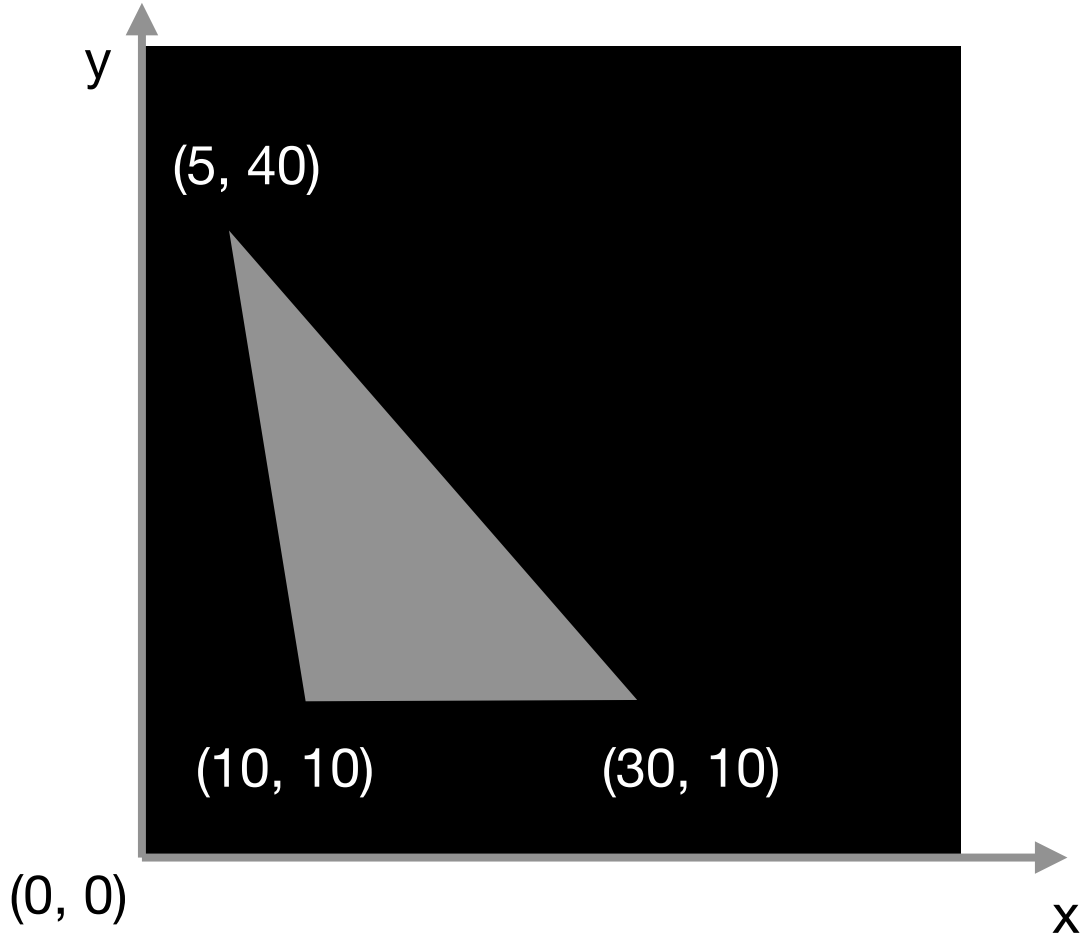


(why a triangle? more on this next time...)

Pseudocode for graphics:

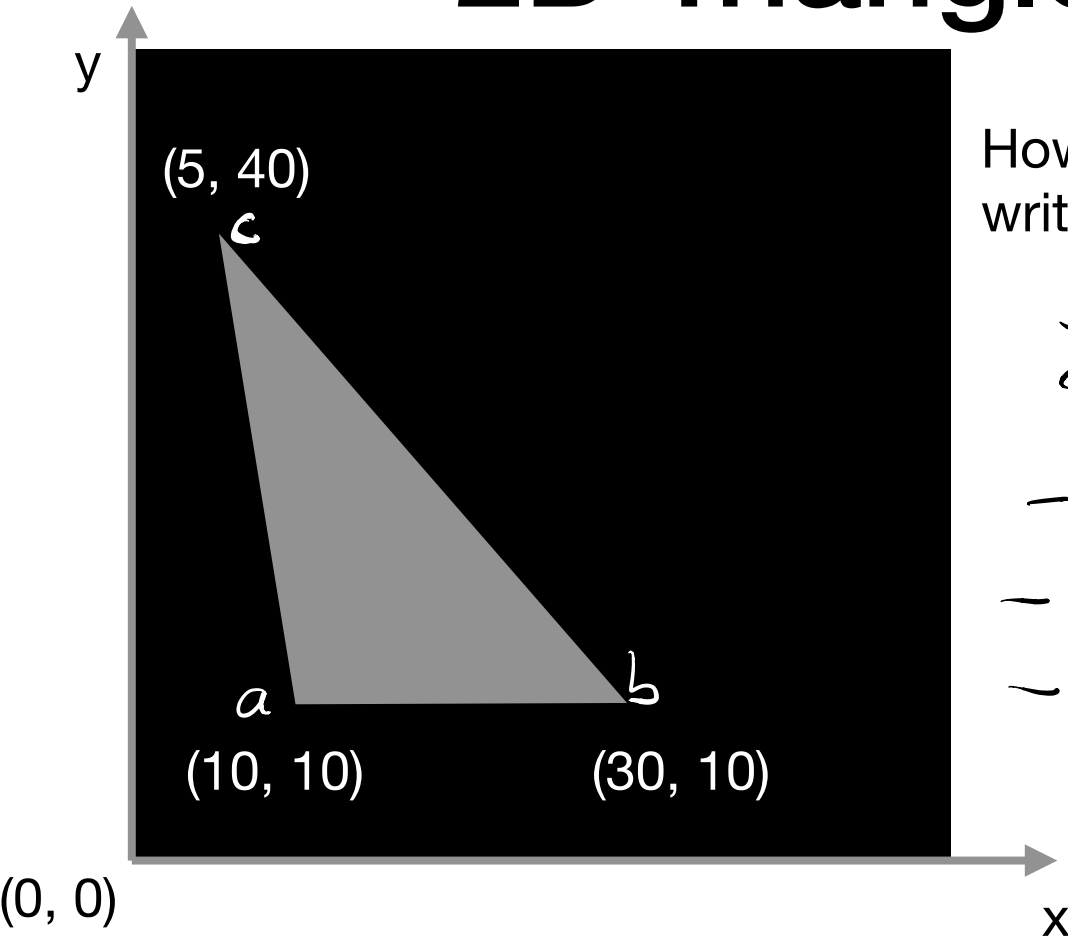
- Create a model of a scene *represent triangle*
- Render an image of the scene *turn on pixels inside triangle*

Create a model of the scene



Convention: list vertices in **counterclockwise** order.

2D Triangles



How many ways can I write down this triangle?

~~$c b a$~~

- $a b c$

- $b c a$

- $c a b$

Convention: list vertices in **counterclockwise** order.

Render an image of the model

what **is** that?



Render an image of the model

What **is** an image anyway?

- A photographic print?
- A photographic negative?
- The screen you're watching this on?
- Some numbers in RAM?

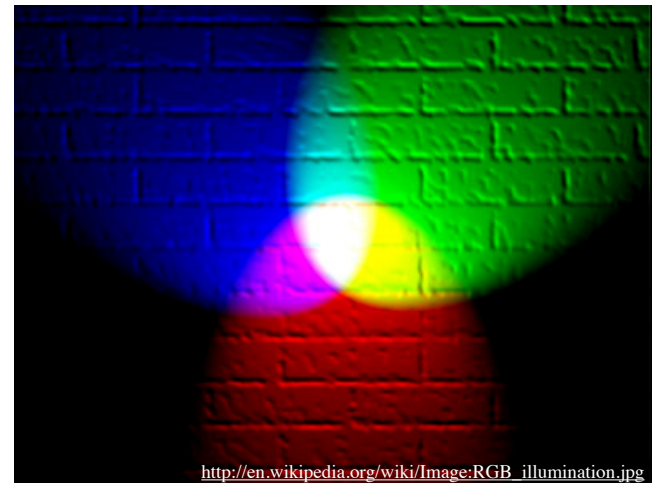
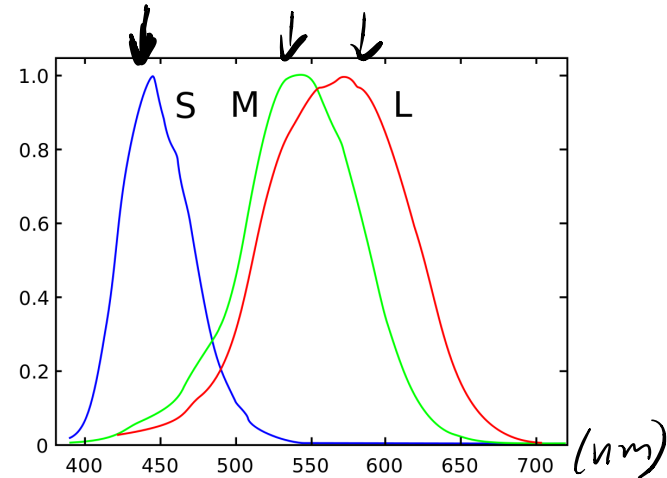
What is an image?

At its most formal and general: a **function** that maps *positions* in 2D to *distributions of radiant energy*

$$I : \mathbb{R}^2 \rightarrow ??$$

What about color?

- Humans are trichromatic, so we usually represent color as combinations of red, green, and blue

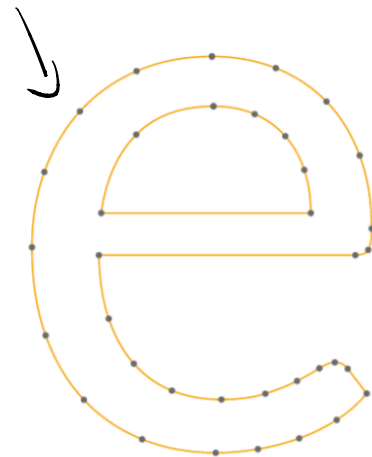


How do we represent images?

- Raster formats - a 2D array of numbers
- Vector formats - mathematical description



Raster Image

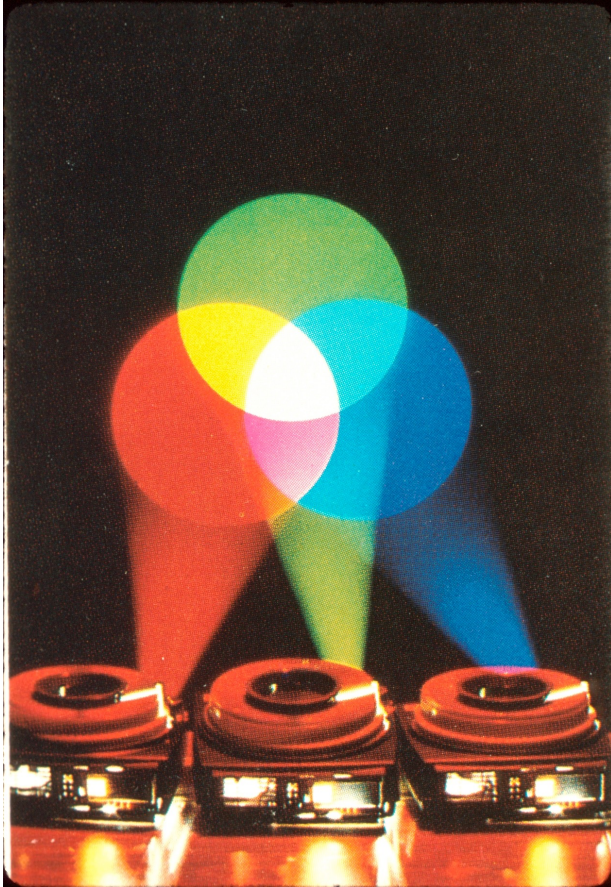


Pavithra Solai, kint.io

Vector Image

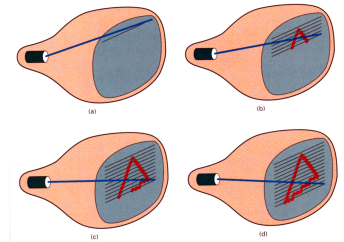
How do we display images? Old School Edition

Color Projector

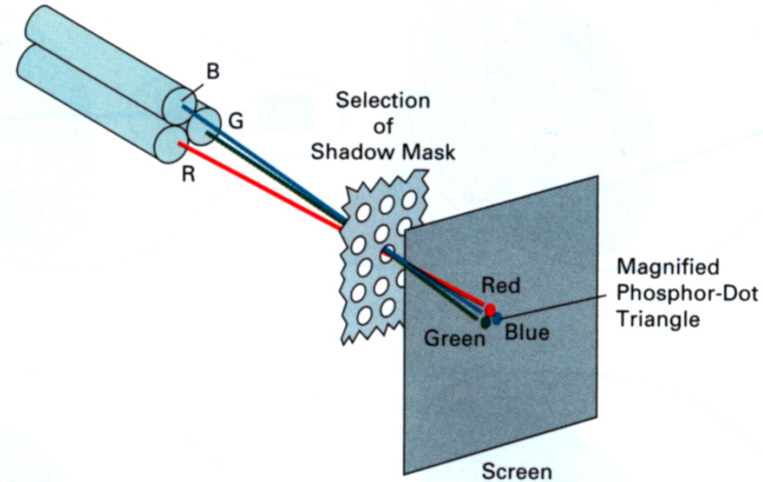


Cathode Ray Tube

Open CRT Monitor

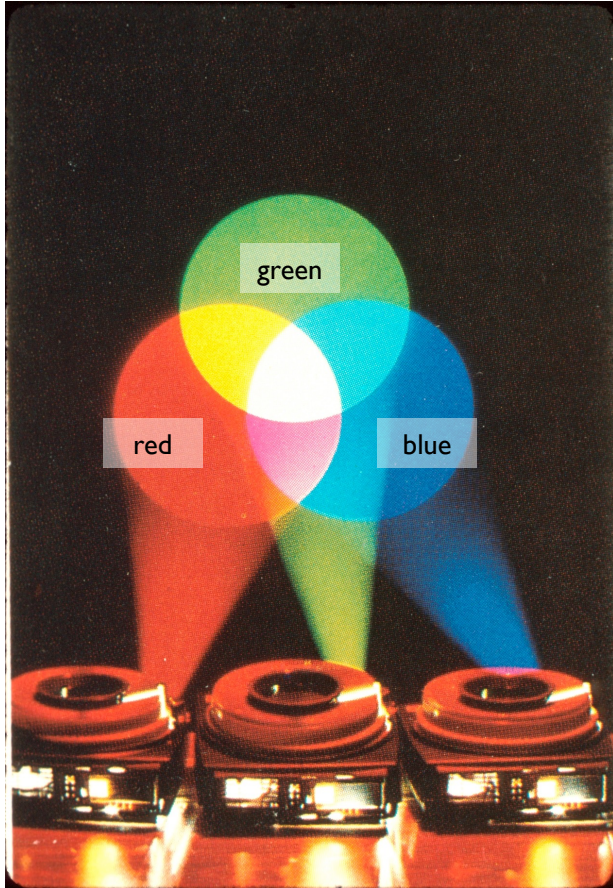


Electron Guns



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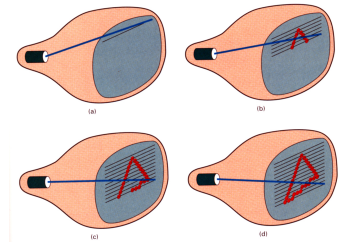


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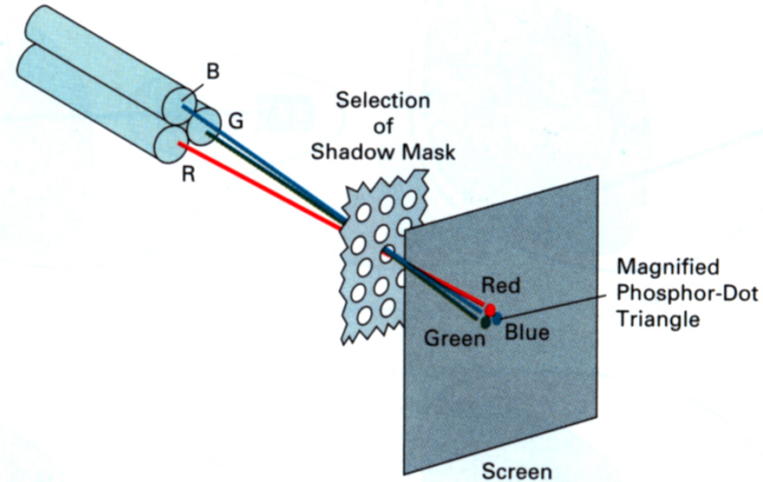
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ComputerHope.com

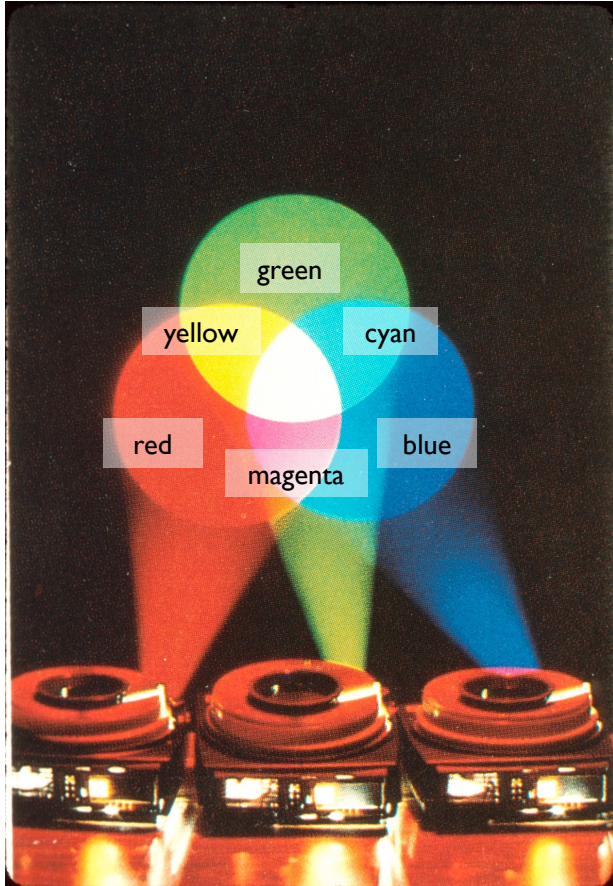


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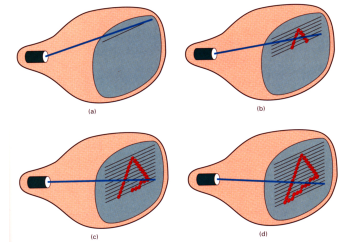
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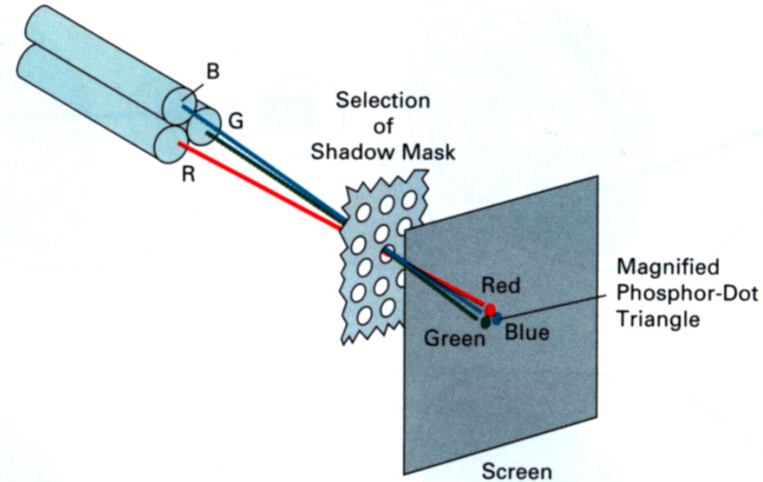


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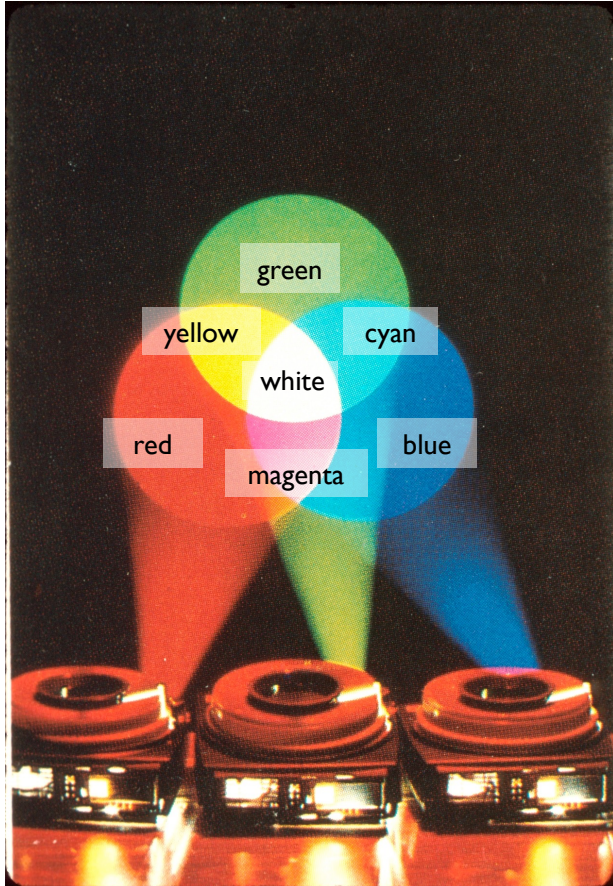


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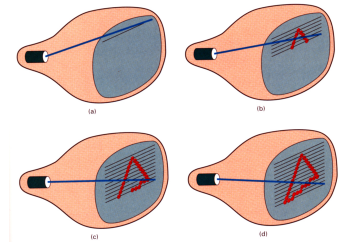
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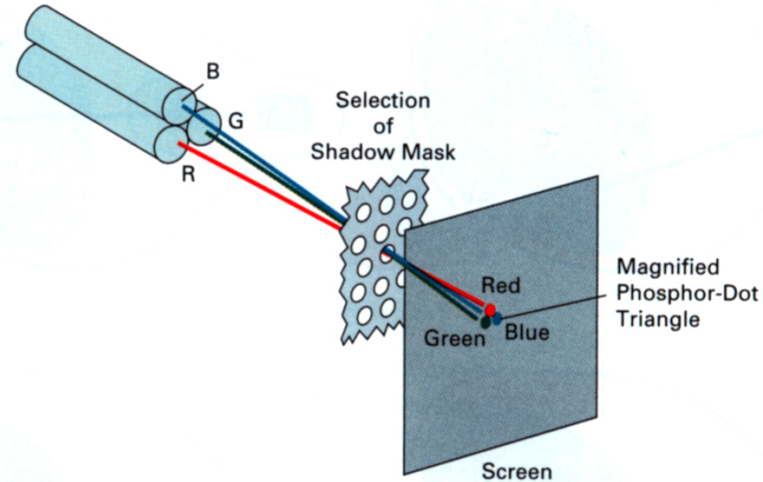


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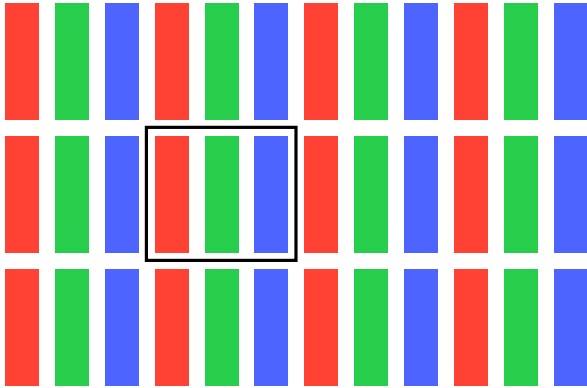


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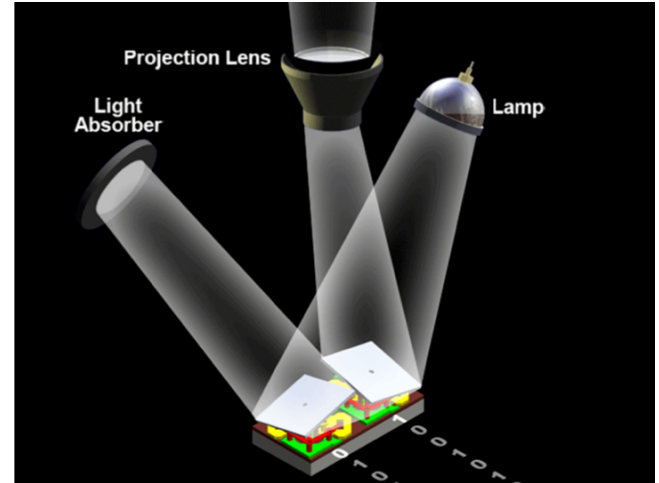


How do we display images? Nowadays Edition

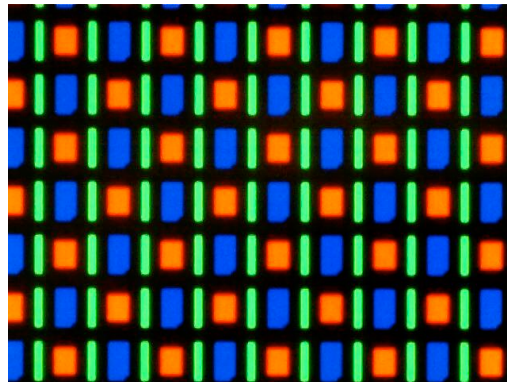
Liquid Crystal Display



Digital Light Processing



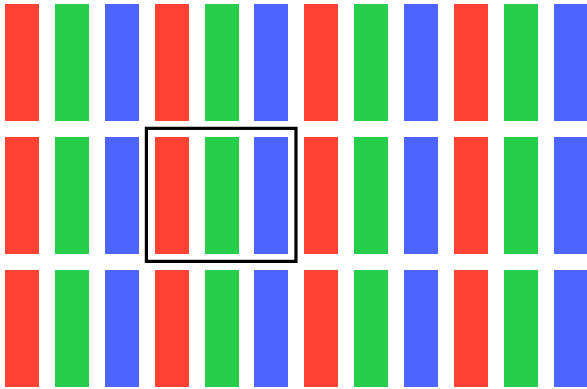
Light Emitting Diode Display



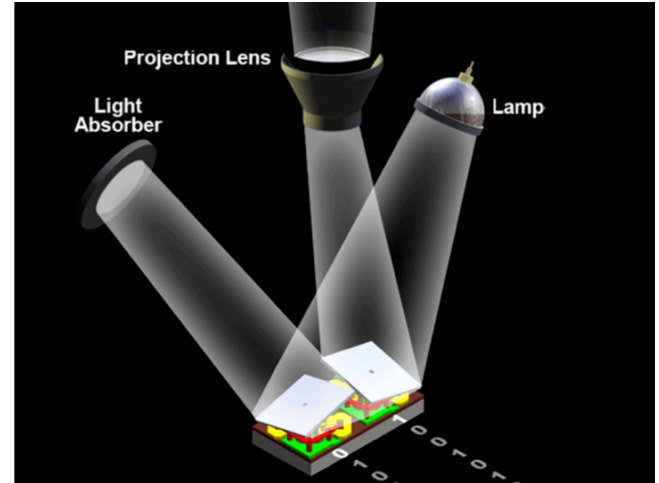
[Wikimedia Commons]

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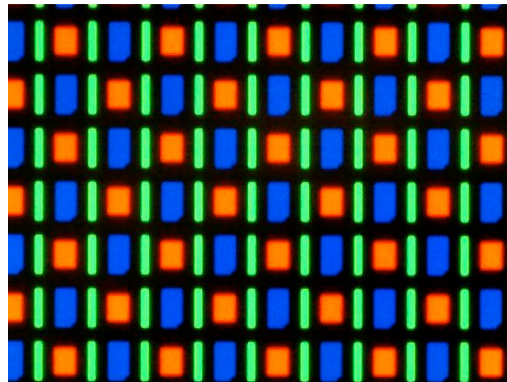
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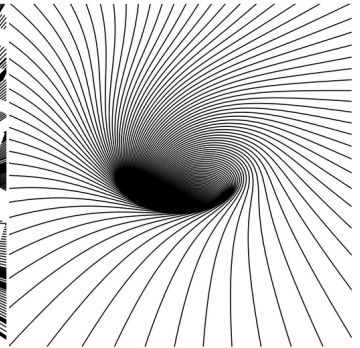
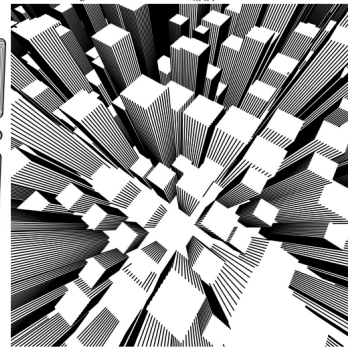
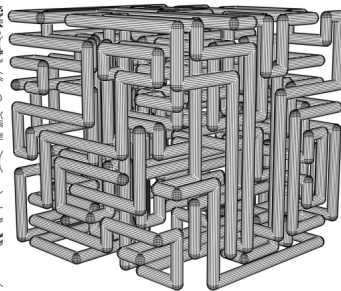
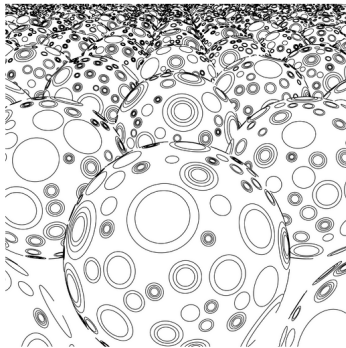
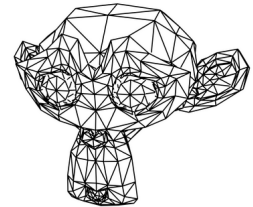
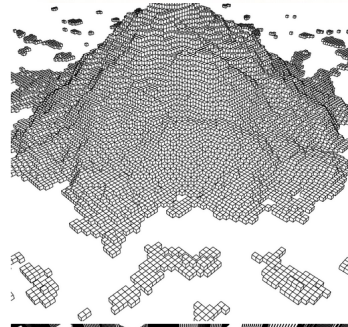
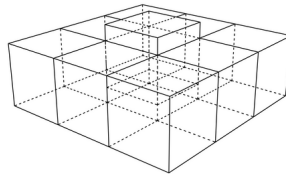
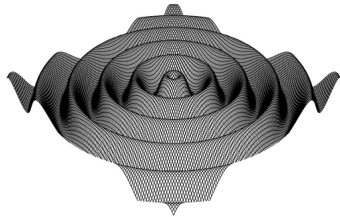
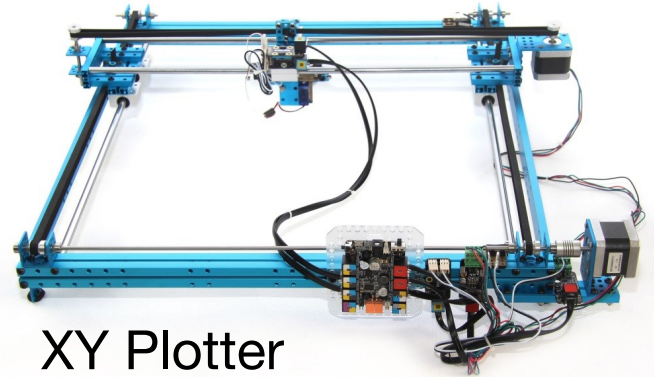


Light Emitting Diode Display



these are all examples
of **raster displays**

Aside: It doesn't
have to be this way...

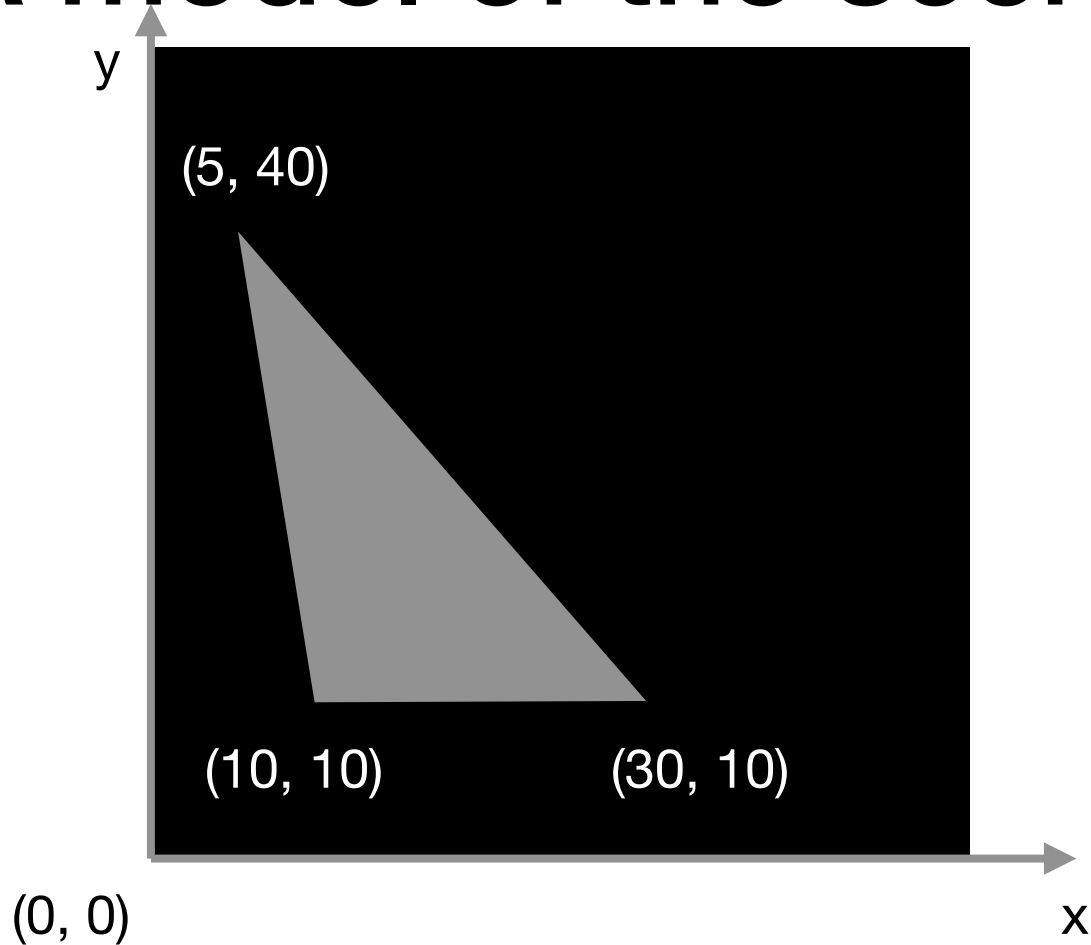


Raster Images

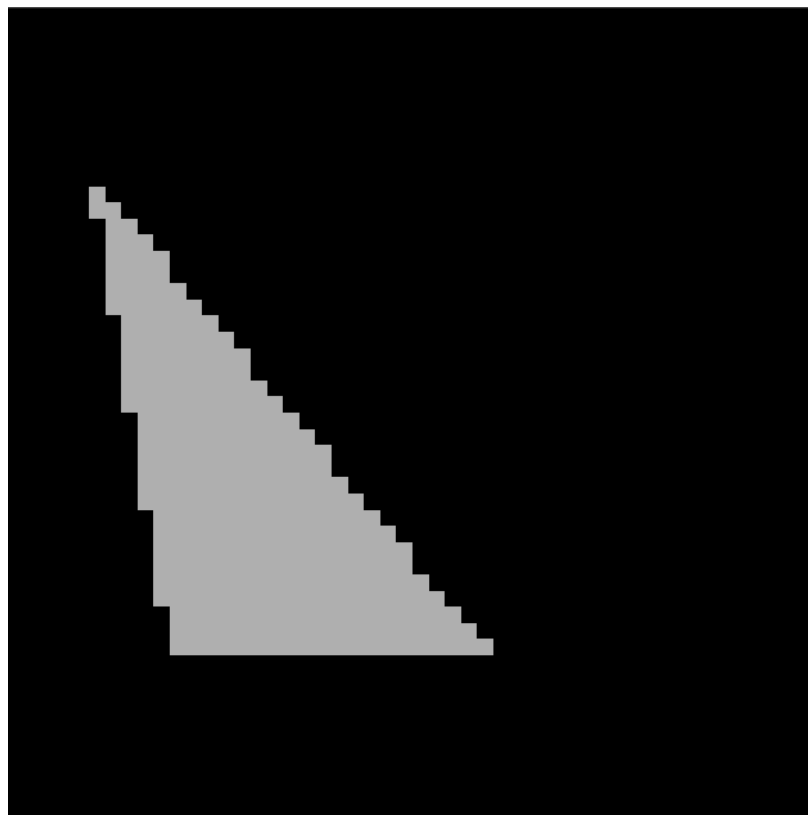
- Flexible
- Display-native
- Expensive
- Not ideal
- But darn useful



A model of the scene



A Raster Image of the Scene



Representing Raster Images: 2D Arrays of Numbers

- Bitmap (1 bit per pixel) $I: \mathbb{R}^2 \rightarrow \{0, 1\}$
- Grayscale (usually 8 bpp) $I: \mathbb{R}^2 \rightarrow [0..MAX]$
- Color (usually 24 bpp) $I: \mathbb{R}^2 \rightarrow [0..MAX]^R$ (e.g. 255)
(R, G, B)
- Floating-point (gray or color) $\mathbb{R}^2 \rightarrow \mathbb{R}^3$
 - Bad for display, but good for processing
 - Allows **high dynamic range**
 - For LDR, values range from 0-1 by convention

Raster Images: Storage

1 **megapixel** image - 1024x1024:

- Bitmap (1 bit per pixel) - **128 KB**
- Grayscale (8 bpp) - **1 MB**
- Color (24 bpp) - **3 MB**
- Floating-point (color) - **12MB**

Aside: Performance

Fact: A 1 megapixel image has
 $1024 \times 1024 = 1048576 = 2^{20}$ pixels.

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Implication: performance matters.

2D Arrays in Julia

- Image: A height-by-width array of pixels.
- For a color image, each pixel is 3 single-precision floats:

```
— canvas = zeros(typeRGB{Float32}, hheight, wwidth)
```

- Matrix-style 1-based indexing (row, column):

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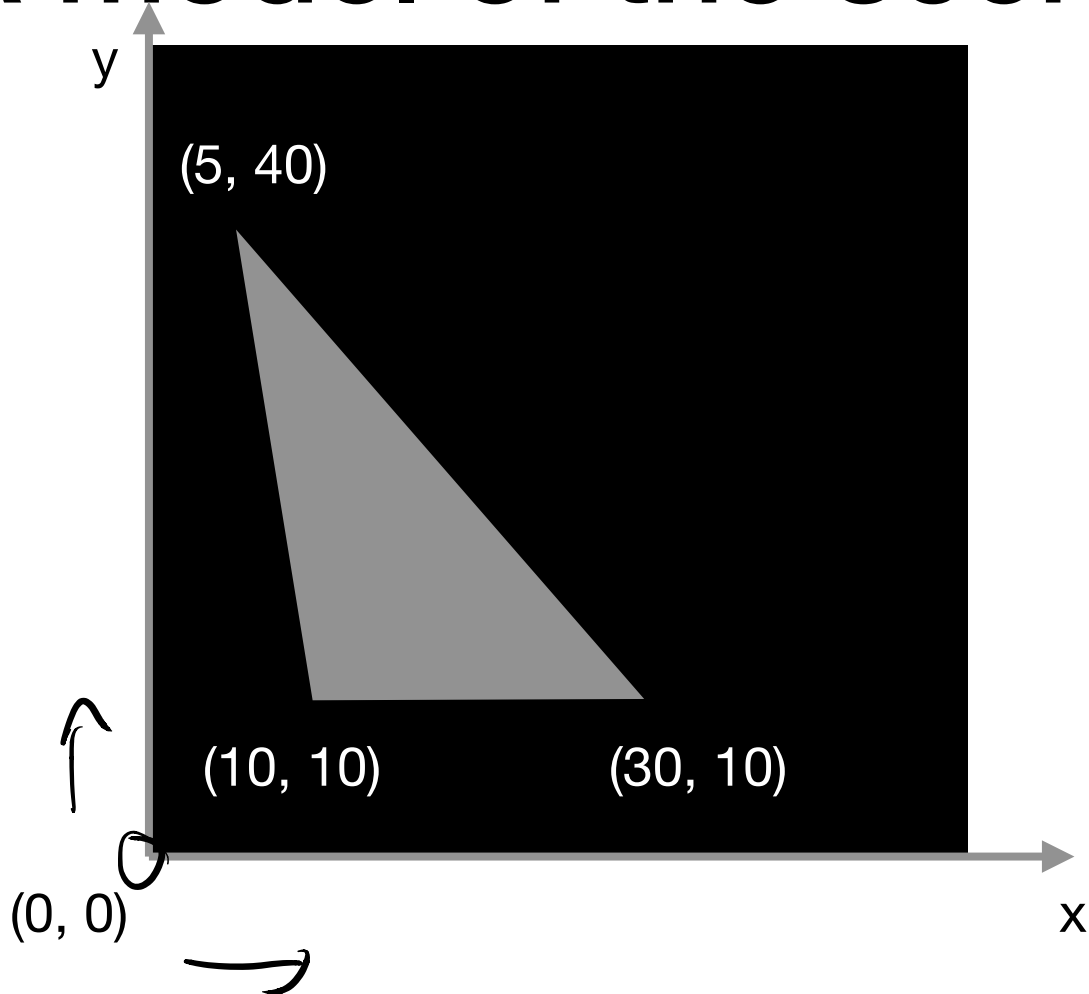
- Matrix-style 1-based indexing (row, column):

```
canvas[i, j] # is the i'th row, j'th column
```

Images in Julia: Demo

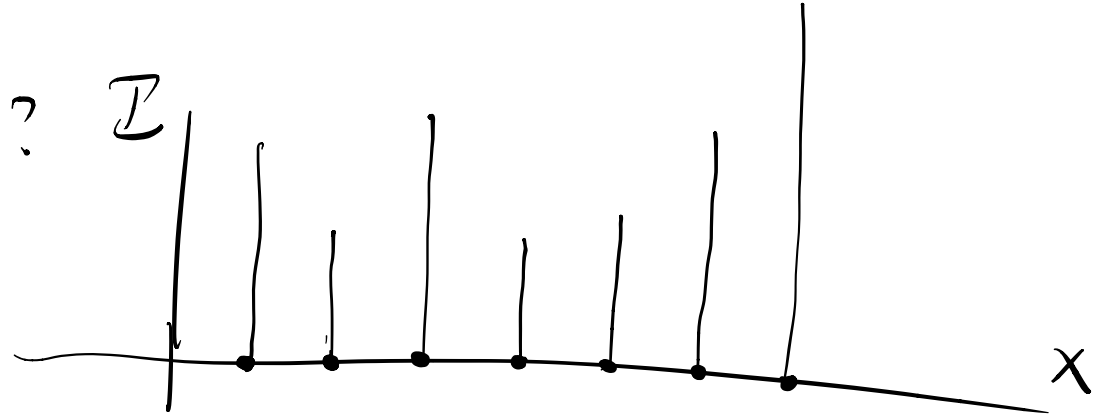
- Draw a rectangle on a canvas
- Demo colors

A model of the scene



Raster images are *sampled*

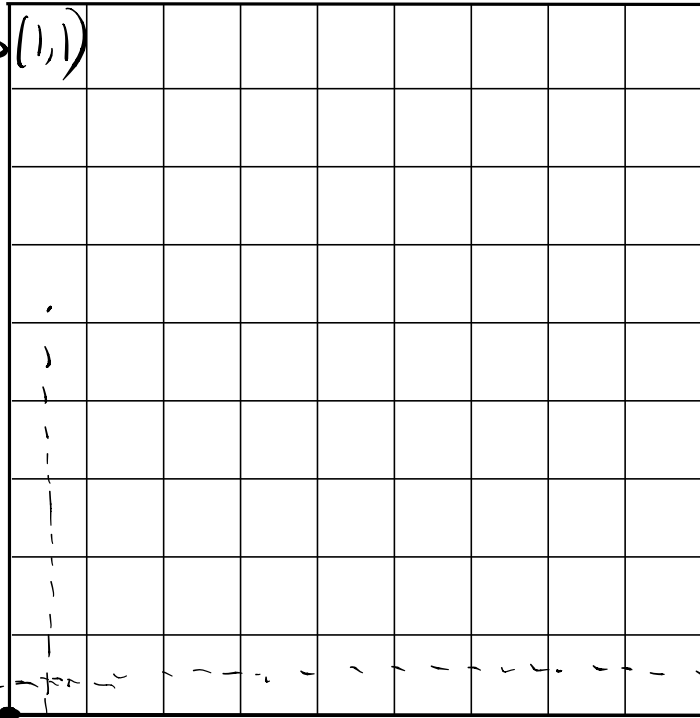
$$I: \mathbb{R}^2 \rightarrow \mathbb{I}$$



Raster Images: Coordinate Systems

Julia $j \rightarrow$

$i \rightarrow$
 \downarrow



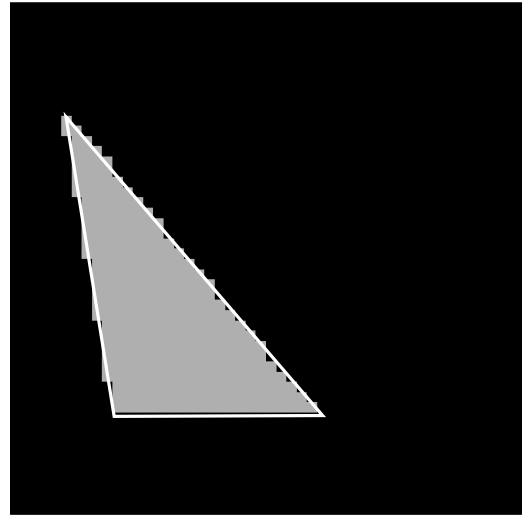
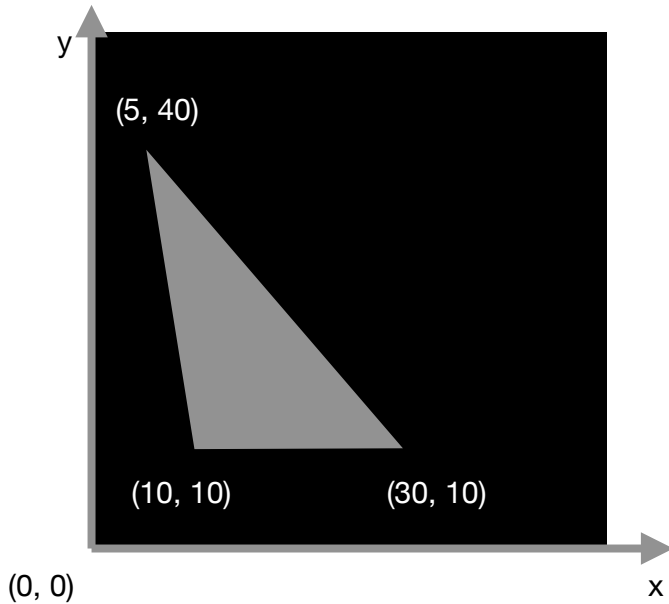
Julia $\rightarrow (h, l)$

0.5

$(0,0)$

$x, y : (0.5, 0.5)$
 \uparrow
 $\rightarrow x$

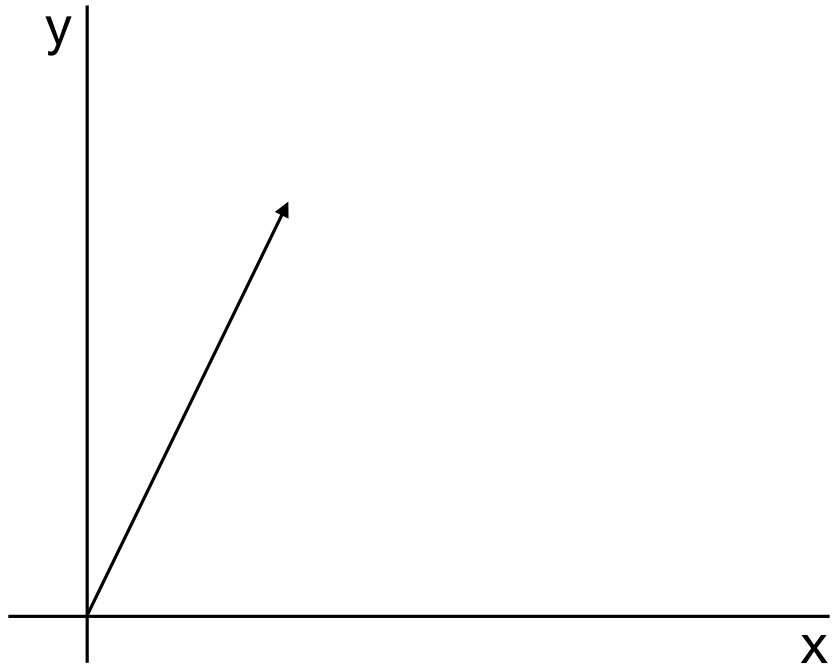
A0: Rendering (*Rasterizing*) a Triangle



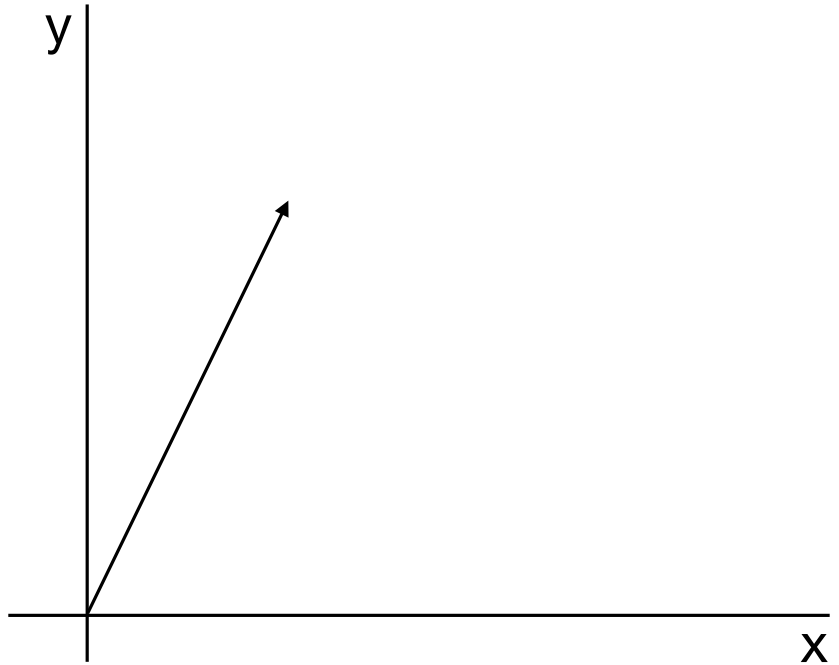
Pseudocode:

for each pixel
if pixel is inside tri
color pixel

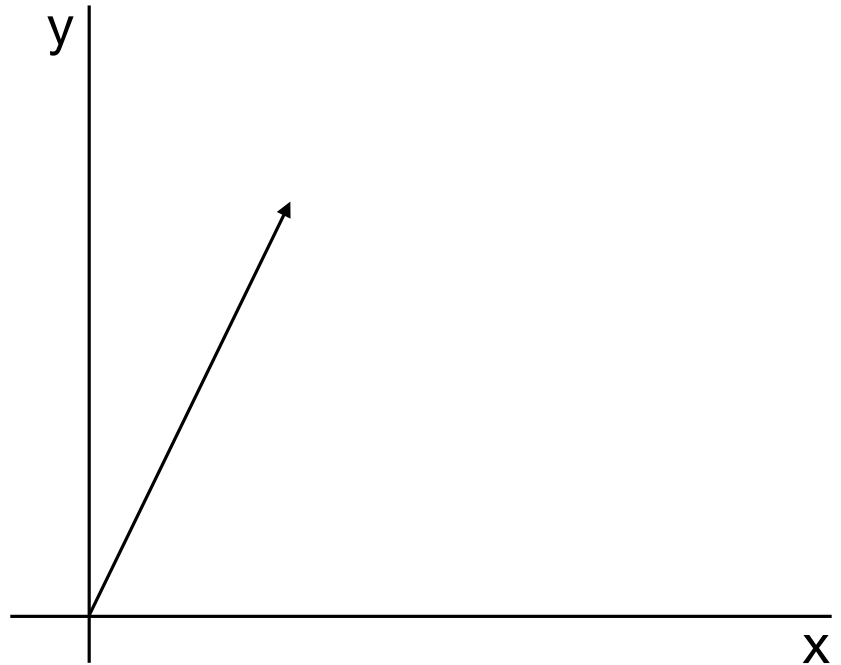
Vectors



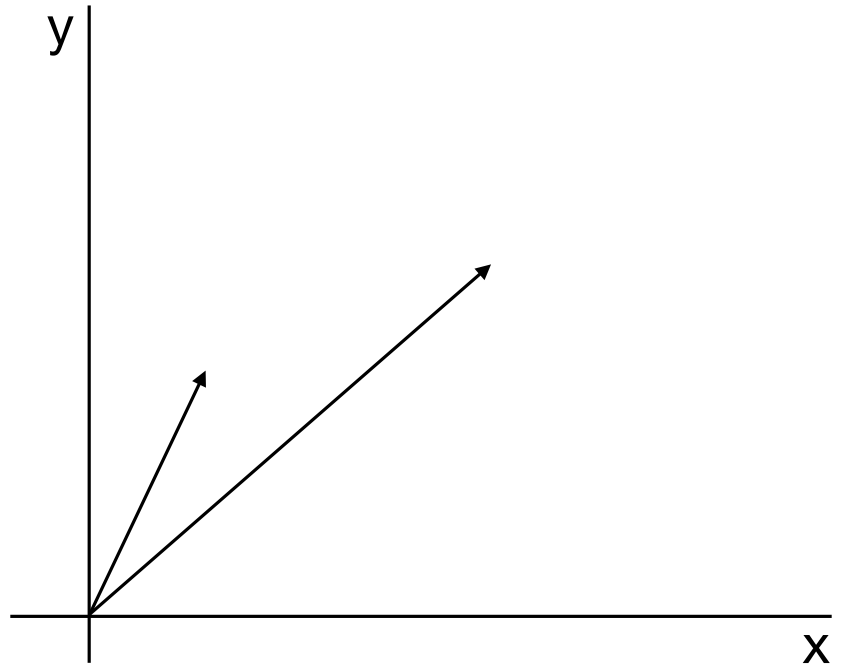
The Canonical Basis



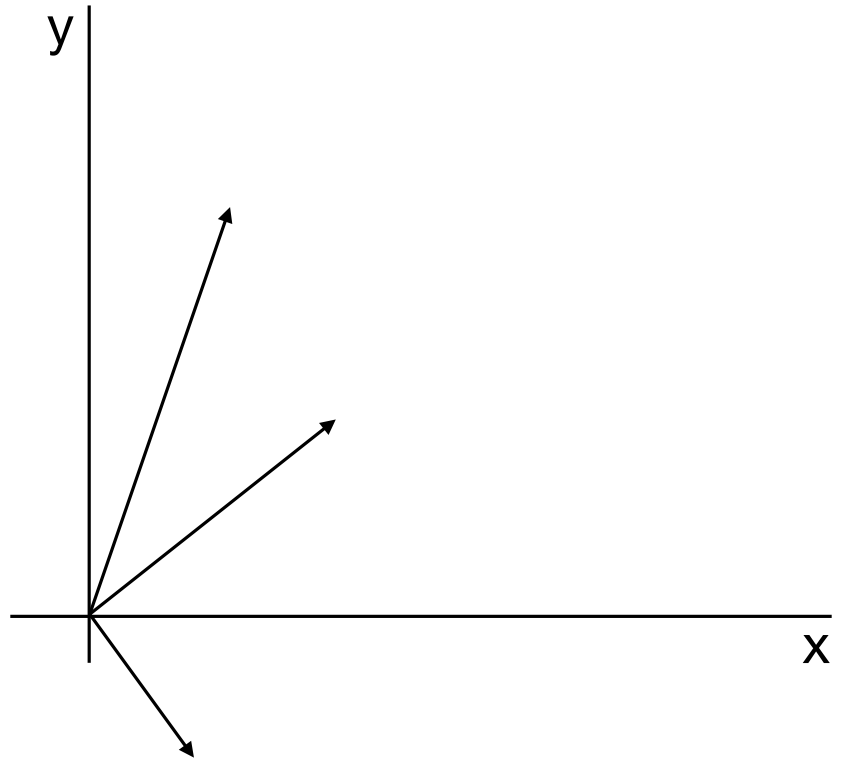
Magnitude (length)



The vector between two points



The dot product



Point-in-Triangle

