

Computer Graphics

Lecture 11 Acceleration Structures Advanced Ray Tracing

 Feedback survey out this afternoon - please respond by Monday night (10pm)

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- Final projects proposals will be due in ~2 weeks; start thinking about topics now.
 More on this later.

Today

- A high-level overview of what comes next in ray tracing.
- Useful for A2 extensions and/or final project ideas.
- Not getting into gory detail see the book references on the slides.

Barycentric ray-triangle intersection

- Every point on the plane can be written in the form: $\mathbf{a}+\beta(\mathbf{b}-\mathbf{a})+\gamma(\mathbf{c}-\mathbf{a})$

for some numbers β and γ .

- If the point is also on the ray then it is $\mathbf{p} + t\mathbf{d}$

for some number *t*.

• Set them equal: 3 linear equations in 3 variables $\mathbf{p} + t\mathbf{d} = \mathbf{a} + \beta(\mathbf{b} - \mathbf{a}) + \gamma(\mathbf{c} - \mathbf{a})$

...solve them to get t, β , and γ all at once!

Barycentric ray-triangle intersection

$$\mathbf{p} + t\mathbf{d} = \mathbf{a} + \beta(\mathbf{b} - \mathbf{a}) + \gamma(\mathbf{c} - \mathbf{a})$$
$$\beta(\mathbf{a} - \mathbf{b}) + \gamma(\mathbf{a} - \mathbf{c}) + t\mathbf{d} = \mathbf{a} - \mathbf{p}$$
$$\begin{bmatrix} \mathbf{a} - \mathbf{b} & \mathbf{a} - \mathbf{c} & \mathbf{d} \end{bmatrix} \begin{bmatrix} \beta \\ \gamma \\ t \end{bmatrix} = \begin{bmatrix} \mathbf{a} - \mathbf{p} \end{bmatrix}$$
$$x_a - x_b & x_a - x_c & x_d \\ y_a - y_b & y_a - y_c & y_d \\ z_a - z_b & z_a - z_c & z_d \end{bmatrix} \begin{bmatrix} \beta \\ \gamma \\ t \end{bmatrix} = \begin{bmatrix} x_a - x_p \\ y_a - y_p \\ z_a - z_p \end{bmatrix}$$

- This is a linear system: Ax = b
- Various ways to solve, but a fast one uses *Cramer's rule*.
- See 4.4.2 for the TL;DR formula
- See 5.3.2 for an explanation of Cramer's rule

for each pixel:
 for each triangle:
 compute barycentric intersection

How expensive? Let's (informally) count some FLOPs. floating-point operations

Last time: barycentric ray-triangle intersection

$$\mathbf{p} + t\mathbf{d} = \mathbf{a} + \beta(\mathbf{b} - \mathbf{a}) + \gamma(\mathbf{c} - \mathbf{a})$$
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9 subtractions
Pre-calculate entries and entries a

rename:

Barycentric Ray-Triangle Intersection

Cramer's rule gives us

5 add/sub 10 mult/div $eta = rac{j(ei-hf)+k(gf-di)+l(dh-eg)}{M},$ $\gamma = rac{i(ak-jb)+h(jc-al)+g(bl-kc)}{M},$ $t = -rac{f(ak-jb)+e(jc-al)+d(bl-kc)}{M},$

where

Reusing from above: 3 mult M=a(ei-hf)+b(gf-di)+c(dh-eg).

Barycentric Ray-Triangle Intersection

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Assume, conservatively that on average, we calculate β and determine that it doesn't intersect (because $\beta < 0$ or $\beta > 1$)

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A typical laptop can currently can do about 100-200 GFLOPS gigaflops per second

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so what's the problem?

https://polycount.com/discussion/141061/polycounts-in-nextgen-games-thread

for each pixel: 720p = 1280×720 = 921600 pixels
for each triangle: computer game model: 40k triangles
 compute barycentric intersection 27 flops

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Want to render this for an interactive game?

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Want to render this for an interactive game? Simply do this 30+ times per second.

Optimize the inner-inner loop: more efficient intersection routines

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- Carefully reduce triangle count

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- Intersect fewer things
 - Most ray intersections don't hit the object!
 - Basic strategy: efficiently find big chunks of the scene that definitely don't intersect your ray

- Quick way to avoid intersections: bound object with a simple volume
 - -Object is fully contained in the volume
 - -If it doesn't hit the volume, it doesn't hit the object
 - -So test bvol first, then test object if it hits



Chapter 12.3.1

Algorithm:

if ray intersects bounding volume:
 if ray intersects object:
 do stuff



Chapter 12.3.1

Chapter 12.3.1

Algorithm: if ray intersects bounding volume: if ray intersects object: do stuff

Cost: more for hits and near misses, but less for far misses

Is this worth it?

- bvol intersection should be much cheaper than object intersection
 - works best for simple bvols, complicated objects
- bvol should bound object as tightly as possible

Tradeoff: efficient intersection vs tightness

Chapter 12.3.1 Bounding Volume Intersection

Exercise: In 2D, devise an algorithm to intersect a ray with an **axis-aligned bounding box**.

Inputs:

- ray (p and d)
- left_x
- right_x
- left_y
- right_y

Output: boolean, whether ray hits box



axis-aligned box

Chapter 12.3.1

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Chapter 12.3.2

Bounding Volume Hierarchy

- Bvols around objects *might* help
- Bvols around groups of objects will help
- Bvols around parts of complex objects will help
- Idea: use bounding volumes all the way from the whole scene down to groups of a few objects

Building the Hierarchy

- Ideally: bound nearby clusters of objects
- Practical solution: partition along axis





























Implementation

- New kind of object: BoundedObject
 - stores references to contained objects (can be BoundedObjects themselves!)
- New ray_intersect routine:
 - Intersect with each child; if any, return closest.

Chapter 12.3.3

Other Approaches:

Uniform Space Subdivision



Uniform Space Subdivision



Grid cells store references to overlapping objects

Compute the grid cells intersected by a ray

Constant offset between cell edge intersections in each dimension:



Ok, what else can't we do?

- Rotate, scale, shear objects *transformations* (more on this next week, and in 13.2)
- Render transparent things transmission and refraction (Ch 13.1)
- Intersect more kinds of objects Constructive Solid Geometry (Ch
- Area light sources, soft shadows, depth of field
 distribution ray tracing (Ch 13.4)

Transformations and Instancing

 Next week we'll talk about how to transform objects:



13.2

Transformations and Instancing

Next week we'll talk about how to transform objects:

When ray tracing, we can alternatively transform the *rays:*



13.2



Same idea allows us to include multiple instances of the same object in a scene.

Transparency and Refraction

13.1

Our framework assumes surfaces reflect light.



What if they don't?

Basically, physics

 Laws of physics govern how light transmits through *dielectric* surfaces. Snell's law:



Basically, physics

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Constructive Solid Geometry

Compose objects from other objects using set operations:



13.3

Constructive Solid Geometry

- Intersections yield intervals of t
- Perform the set operations on those intervals to determine intersection point.



13.3

13.4

Problem: jagged object and shadow edges



13.4

• Problem: jagged object and shadow edges





we want this

we have this



we want this

Idea: supersample rays within each pixel.



we want this

we have this



Idea: supersample rays within each pixel.

13.4

• Problem: area light sources



• Problem: area light sources



13.4

• Problem: area light sources



Next week:

- Transformations positioning, scaling, rotating, shearing, etc. of objects and cameras in the scene.
- Intro to object-order rendering.