

# Computer Graphics

Lecture 8

**Shading**

**Mirror Reflection**

**Shadows**

# Announcements

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  - HW1 Problems 3 and 4 will help with A2 TODO 9 and 8.

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- HW1 is out - due next Monday
  - HW1 Problems 3 and 4 will help with A2 TODO 9 and 8.
- A2 is now due Friday 2/7

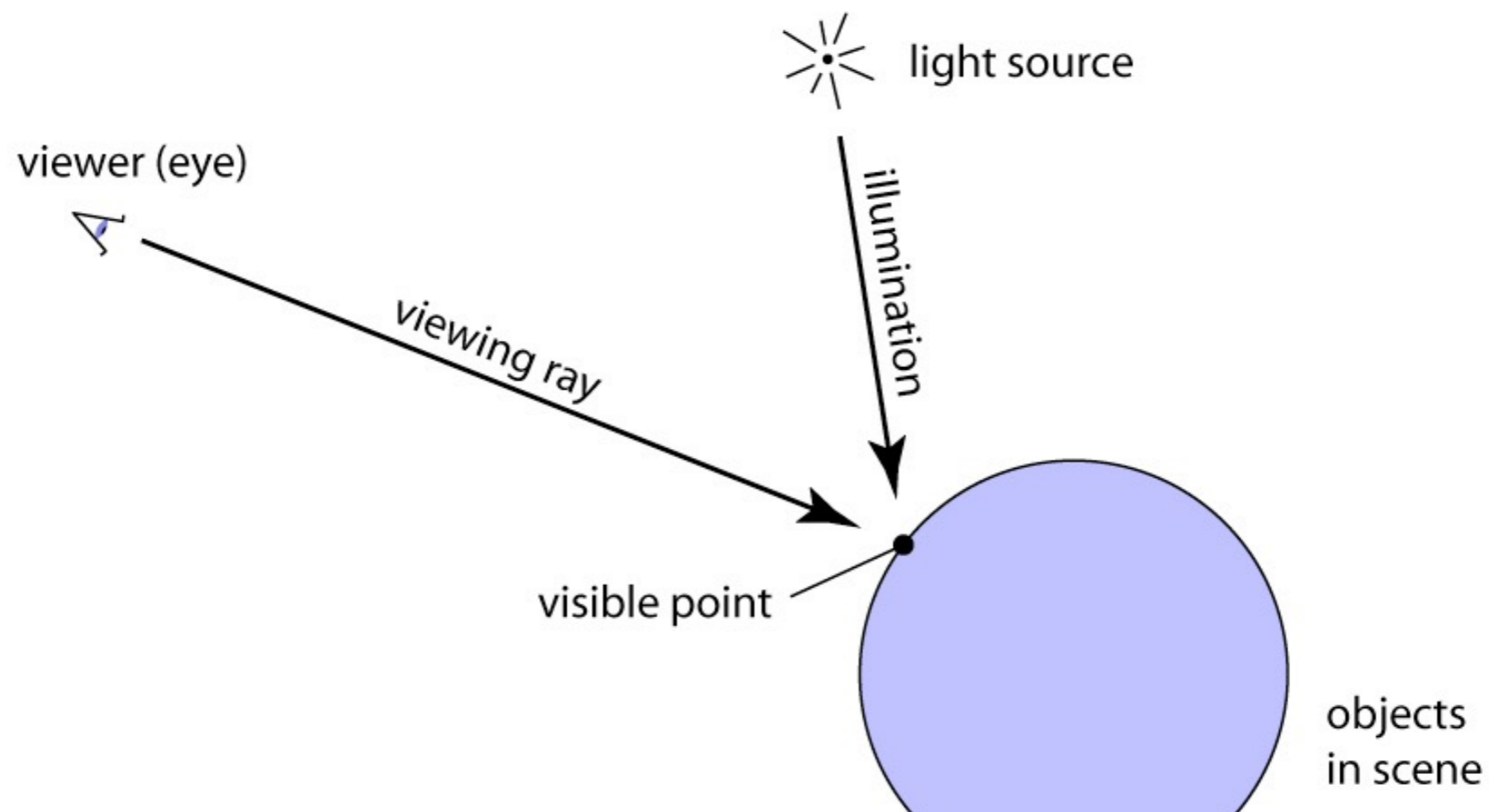
# Ray Tracing: Pseudocode

for each pixel:

generate a viewing ray for the pixel

find the closest object it intersects

determine the color of the object



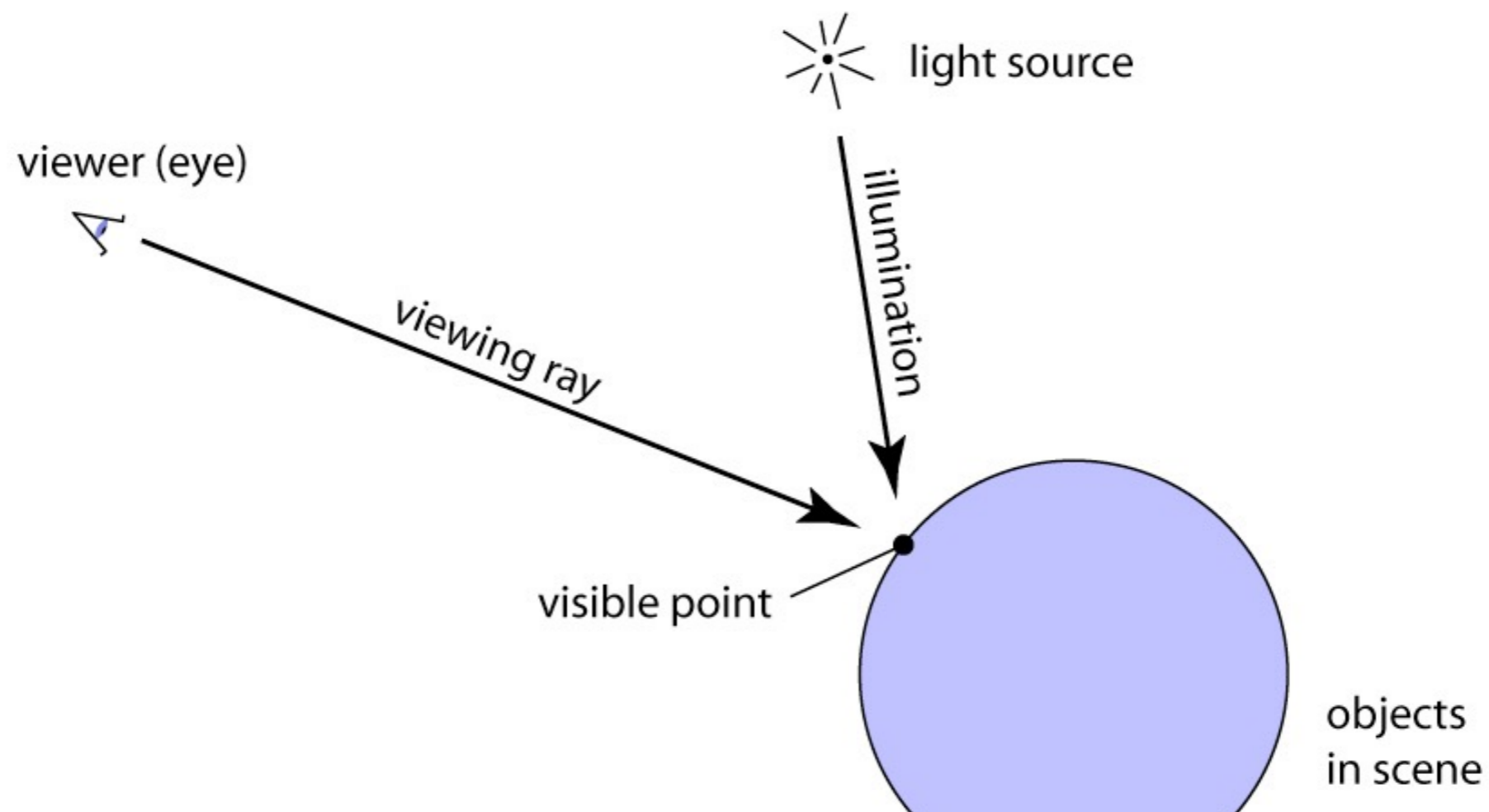
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# Shading

What does the color of a pixel depend on?

- surface normal *stored in or calculated from object*
- surface properties (color, shininess, ...) *stored in object*
- eye direction *calculated from viewing ray and intersection point*
- light direction (for each light) *calculated from light and intersection point*



# Ray-Sphere: Code Sketch

```
function ray_intersect(ray, sphere, tmin, tmax):
```

- Use last lecture's math to find  $\pm t$
- If no real solutions, return `nothing`
- Otherwise, return closest  $t$  that lies between `tmin` and `tmax`
- Also return info needed for shading - store in a `HitRecord` struct.

In A2:  $t$ , intersection point, normal, texture coordinate, object

# Ray-Scene: Code Sketch

**Brute force:** check all objects.

There are better ways - more on this later.

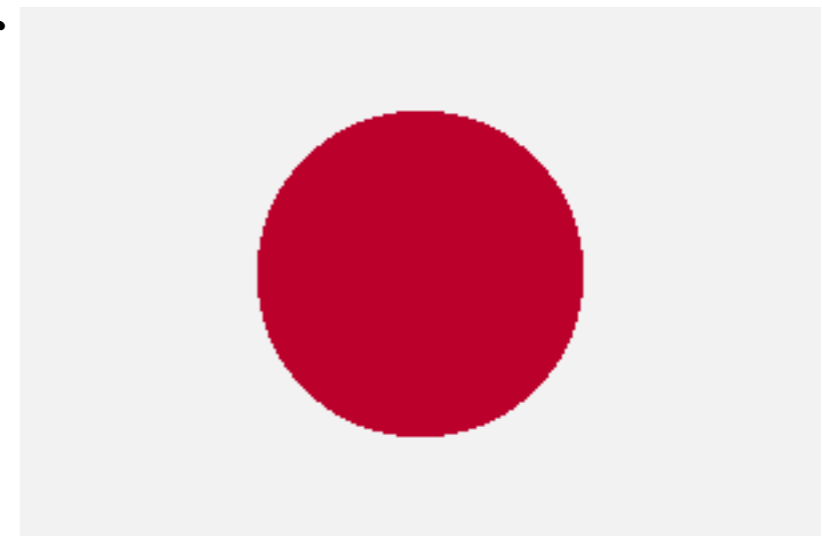
```
find_intersection(ray, scene):
    closest_t = Inf # closest intersection t
    closest_rec = nothing # HitRecord for intersection
    for obj in scene:
        t, rec = ray_intersect(ray, obj, 1, closest_t)
        if rec != nothing:
            closest_t = t
            closest_rec = rec
    return closest_t, closest_rec
```

# Ray Tracing: Code Sketch

```
scene = model_scene()
for each pixel (i,j):
    ray = get_view_ray(i, j)
    t, rec = find_intersection(ray, scene)
    if rec != nothing:
        canvas[i,j] = obj.color
    else:
        canvas[i,j] = scene.bgcolor
```

# Ray Tracing: Code Sketch

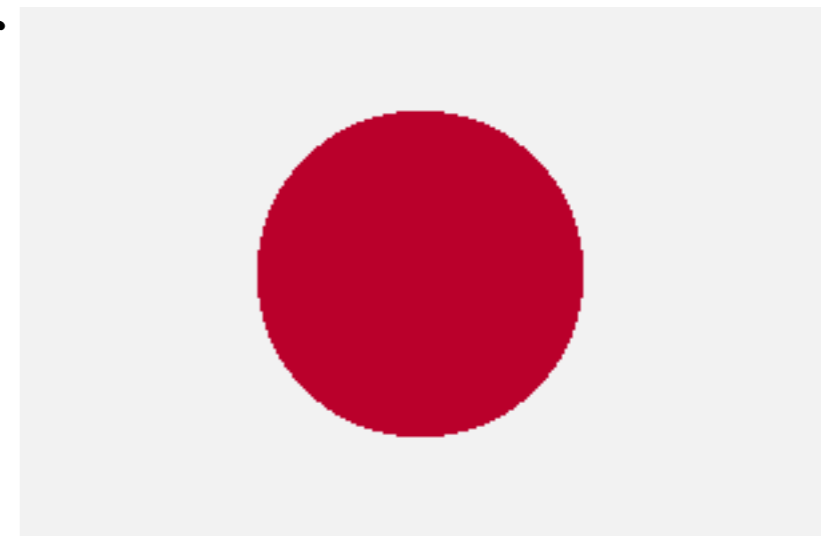
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# Ray Tracing: Code Sketch

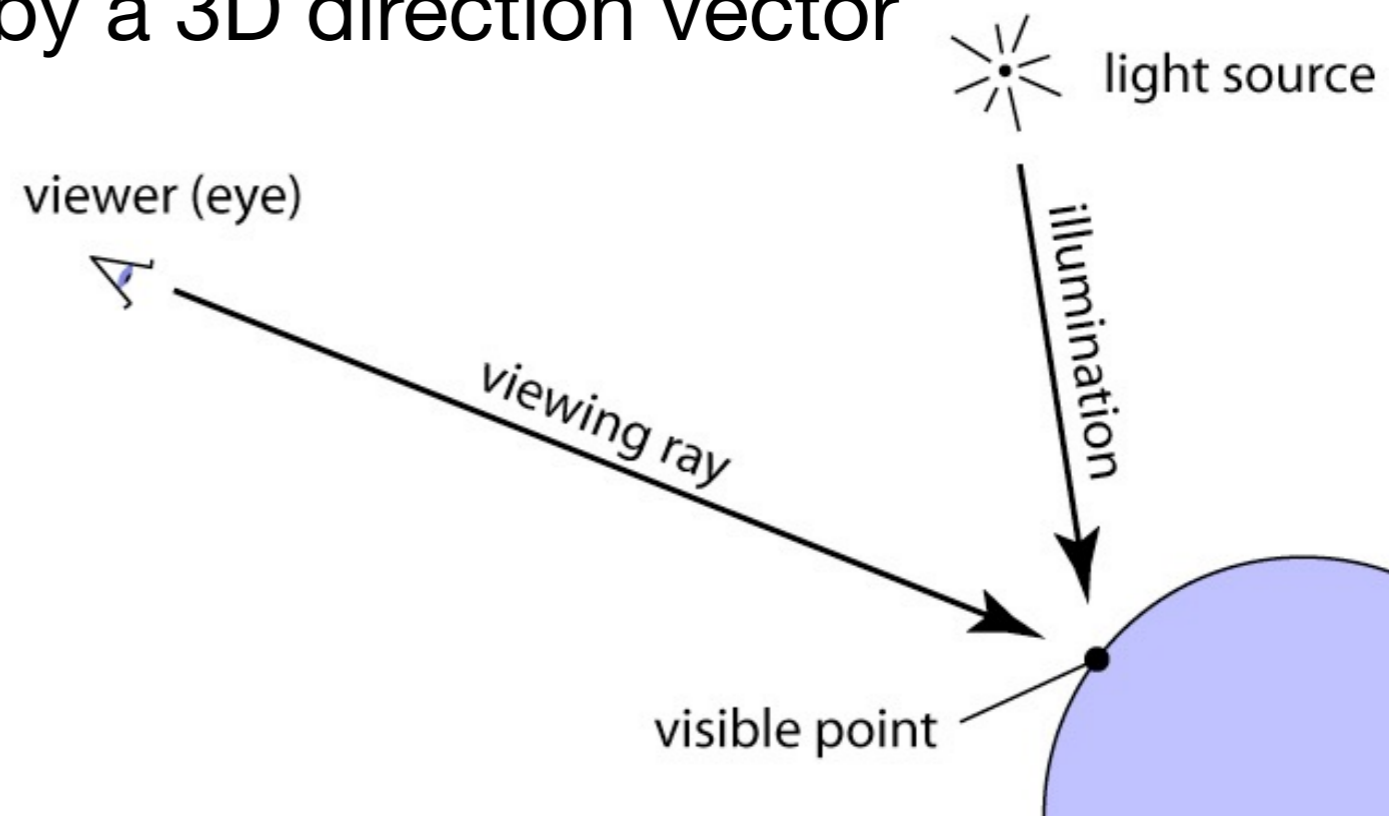
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**Let's work on this.**



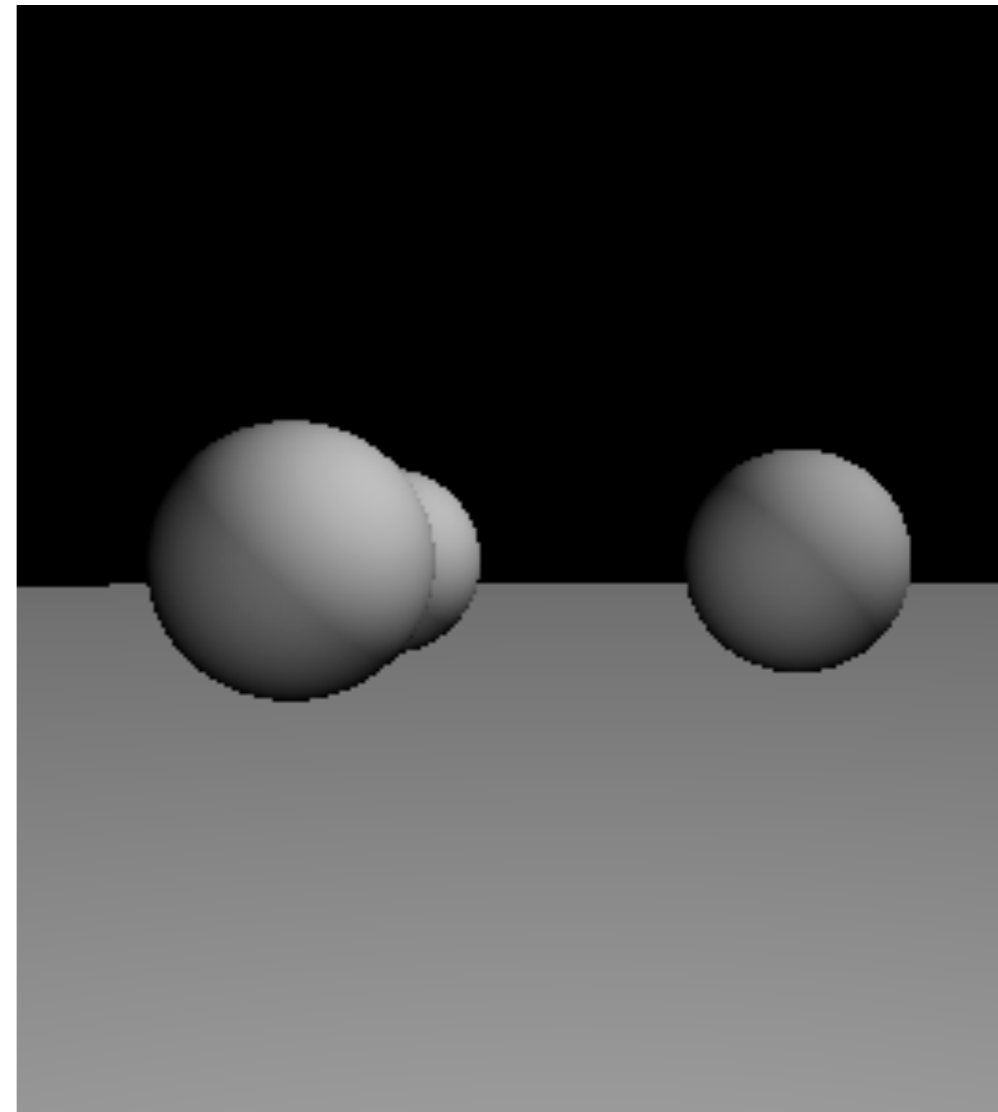
# Light Sources

- Where does light come from?
- Two simple kinds of sources:
  - point source: defined by a 3D position
  - directional source: defined by a 3D direction vector



# Diffuse (Lambertian) Reflection

- On a *diffuse* surface, light scatters uniformly in all directions.
- No dependence on view direction.
- Many surfaces are approximately diffuse:
  - matte painted surfaces, projector screens,
  - anything that doesn't look "shiny"



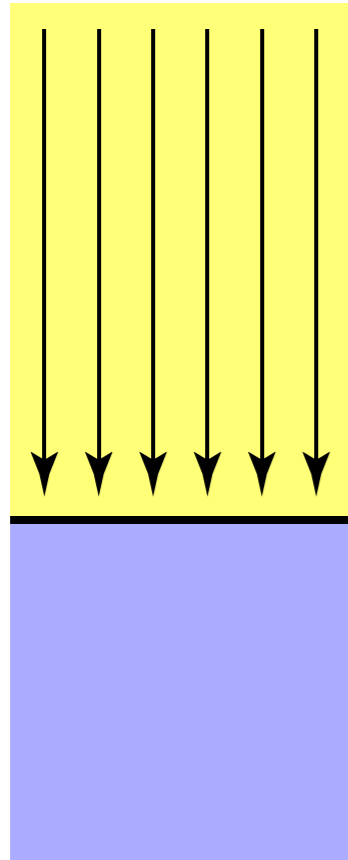
# Diffuse (Lambertian) Reflection

- whiteboard



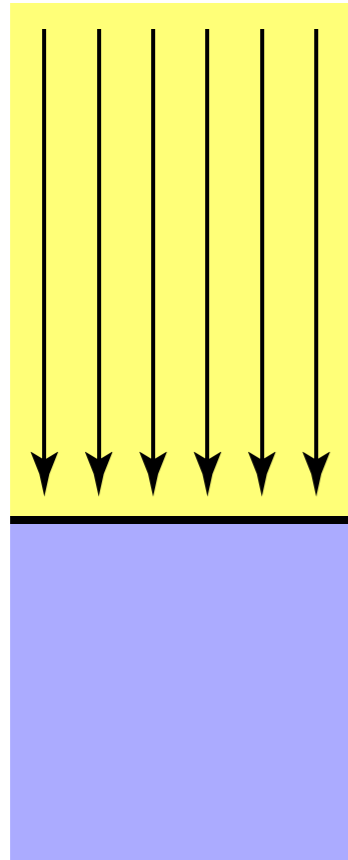
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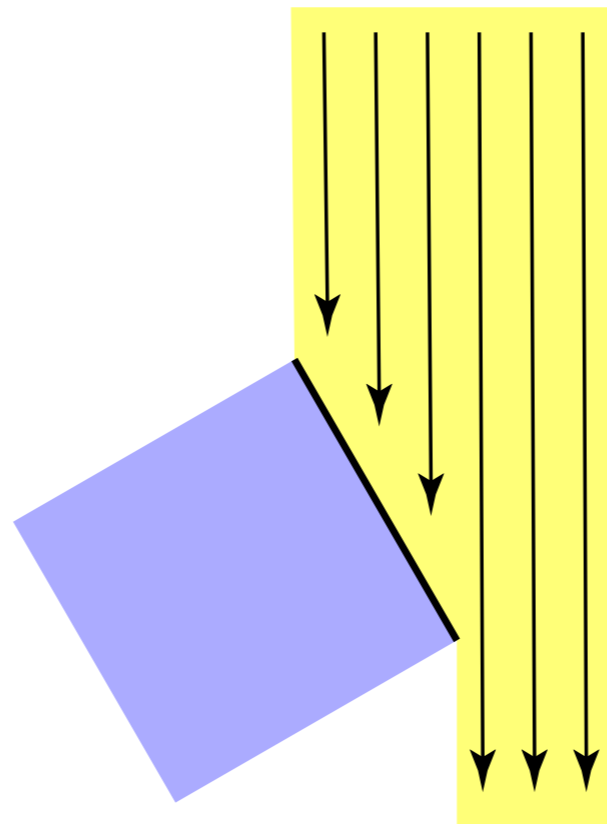


The top face of a cube  
receives some  
amount of light.

# Diffuse (Lambertian) Reflection

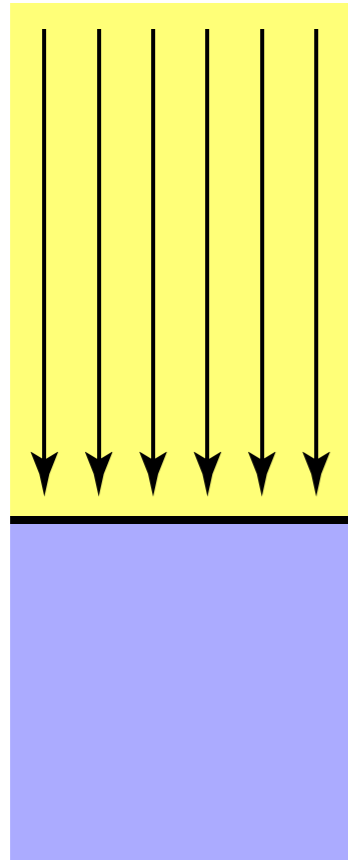


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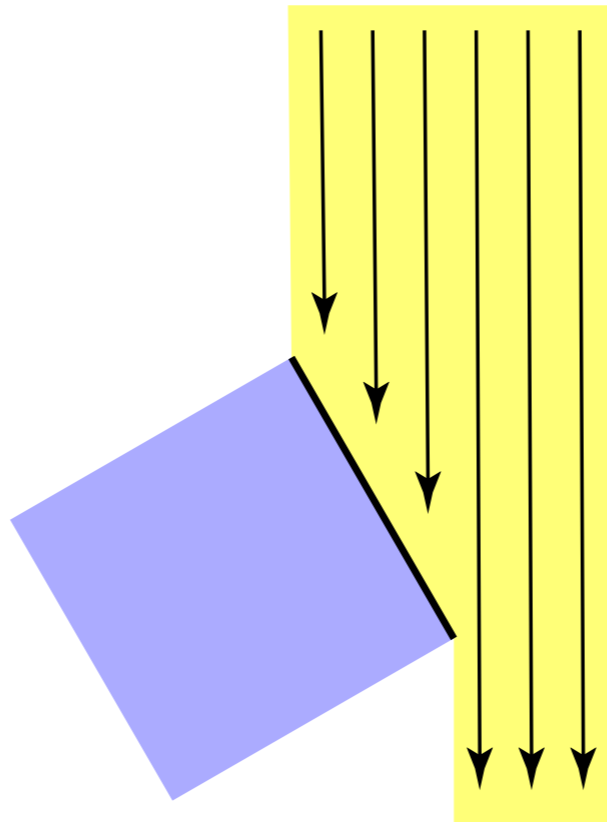


Rotated  $60^\circ$ , the same face receives half the light.

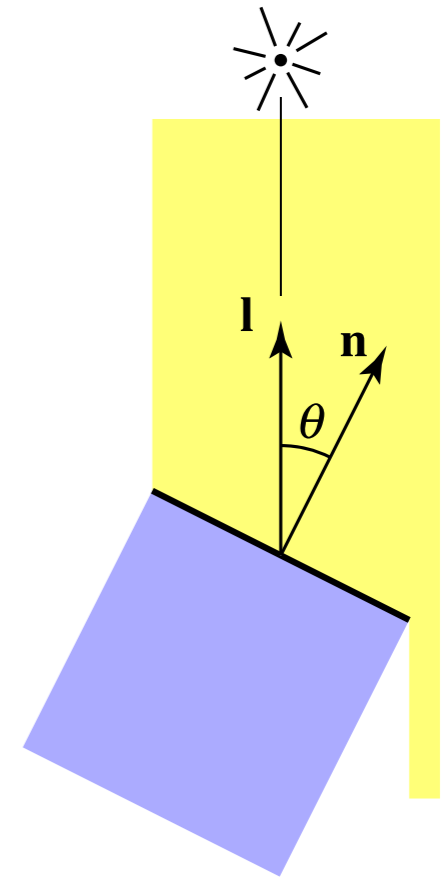
# Diffuse (Lambertian) Reflection



The top face of a cube receives some amount of light.



Rotated  $60^\circ$ , the same face receives half the light.



Light per unit area is proportional to  $\cos \theta = \vec{n} \cdot \vec{l}$

# Diffuse (Lambertian) Shading

- The full model:

$$L_d = k_d I \max(0, \vec{n} \cdot \vec{\ell})$$

diffuse  
coefficient

why max?

diffusely  
reflected light

light intensity

# Diffuse (Lambertian) Shading

- The full model:

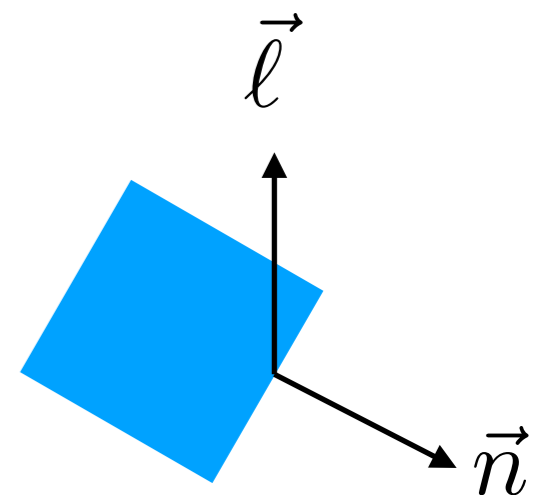
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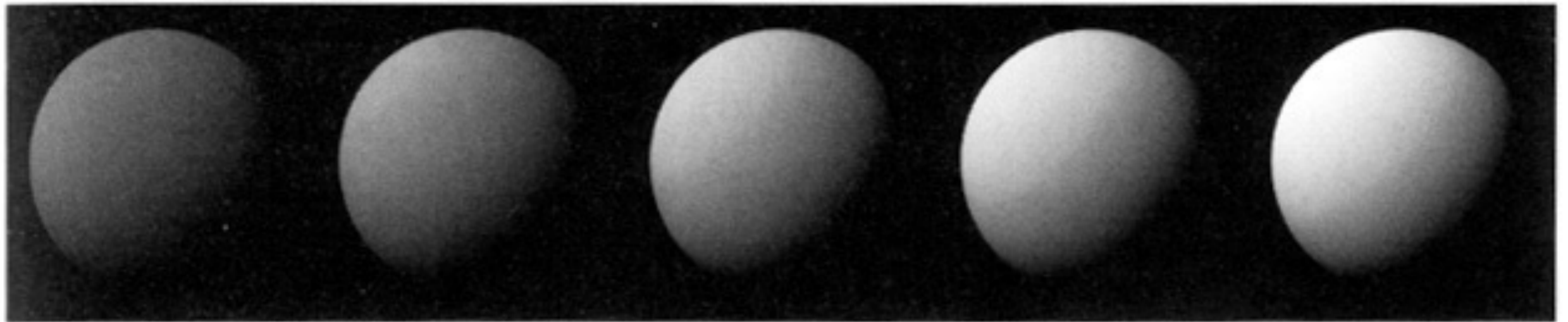
diffusely  
reflected light

light intensity



# Diffuse (Lambertian) Shading

$$L_d = k_d I \max(\vec{n} \cdot \vec{\ell})$$



[Foley et al.]

$k_d$   $\longrightarrow$

For colored objects,  $k_d$  is a 3-vector of R, G, and B reflectances.

# Exercise: Diffuse Reflection



# Let's talk shinies.

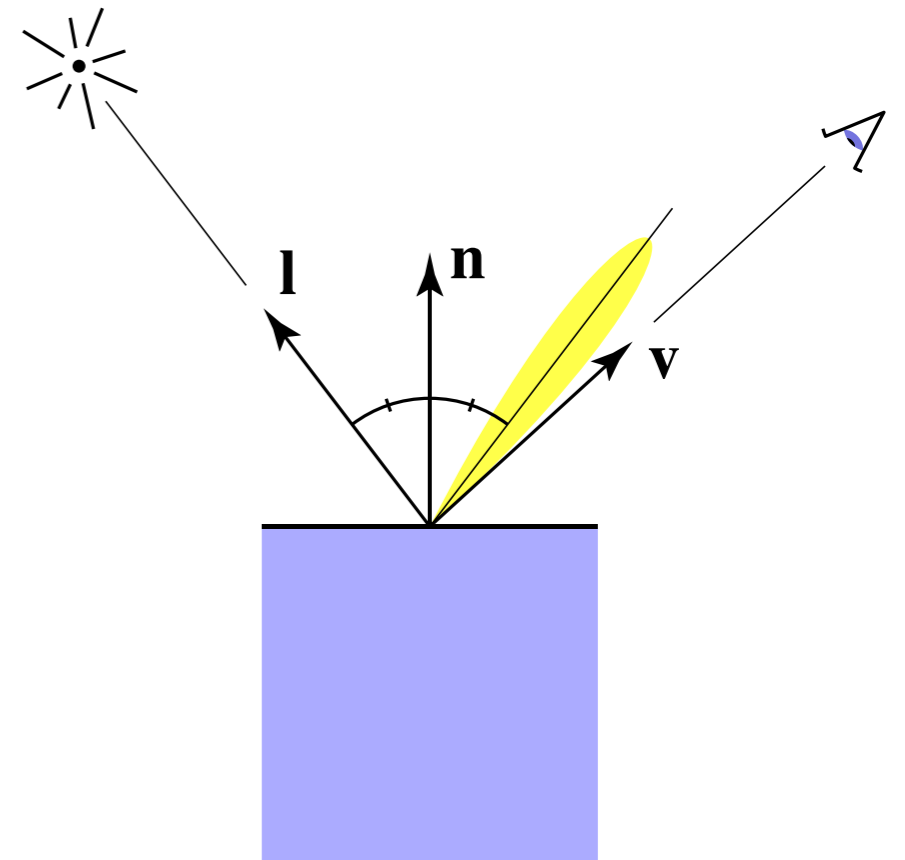
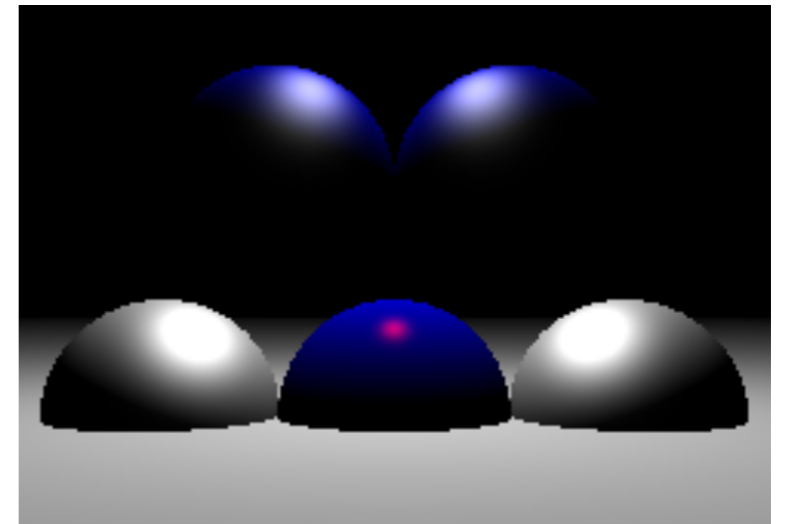
- How does a mirror interact with light?



(whiteboard)

# Specular Reflection

- What about non-mirror shiny surfaces?
- They appear brighter *near* "mirror" configuration
- Phong reflection: specular reflection is a function of angle between  $\mathbf{r}$  and  $\mathbf{v}$ .



# Specular Reflection

- Blinn-Phong: specular reflection is a function of angle between **half-way vector** between view and light and the **normal**.

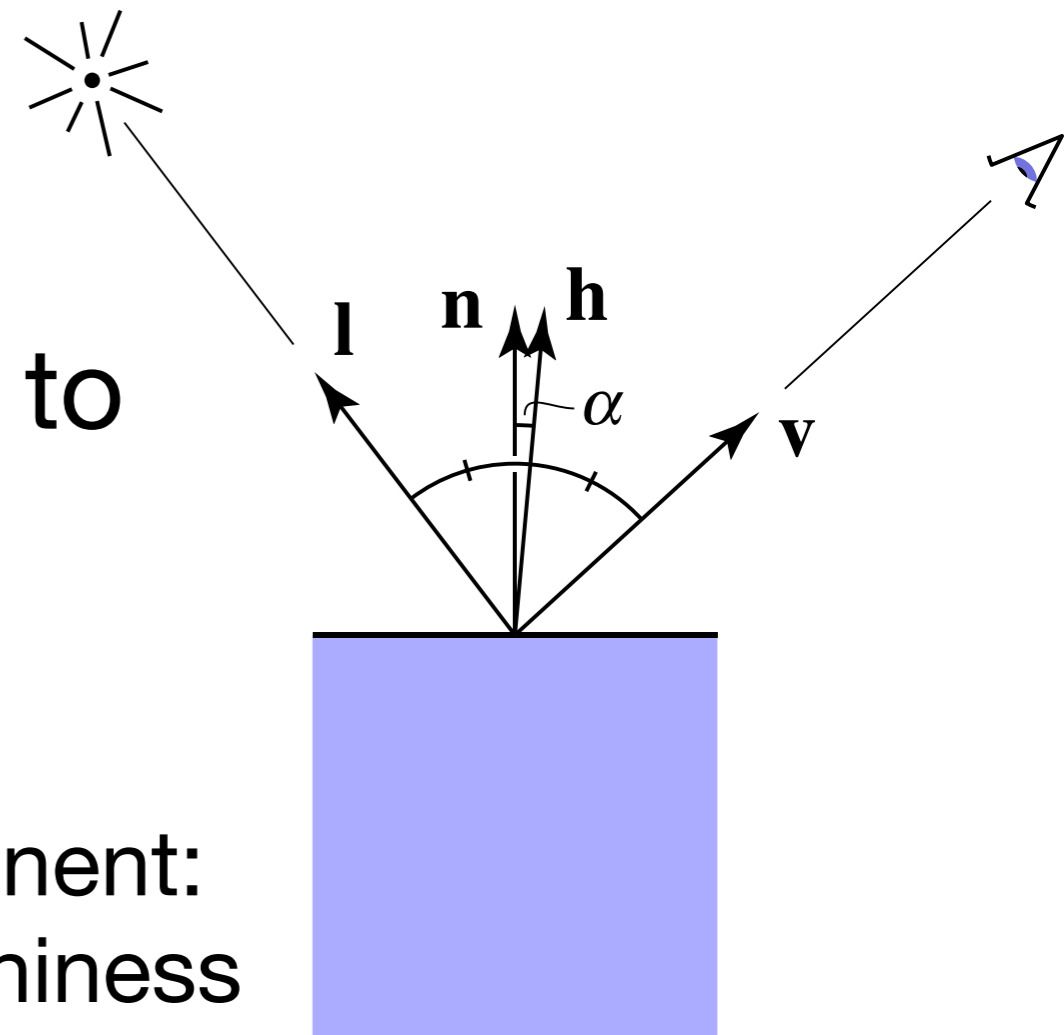
- $h = \text{bisector}(\mathbf{v}, \mathbf{l})$

- Reflected light proportional to

$$k_s \max(0, \vec{n} \cdot \vec{h})^p$$

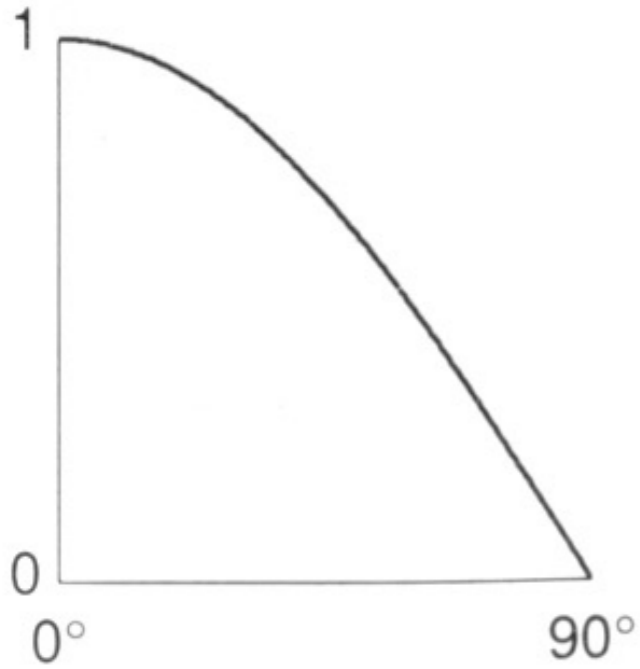
specular coefficient:  
determines strength of  
specularity term

specular exponent:  
determines shininess

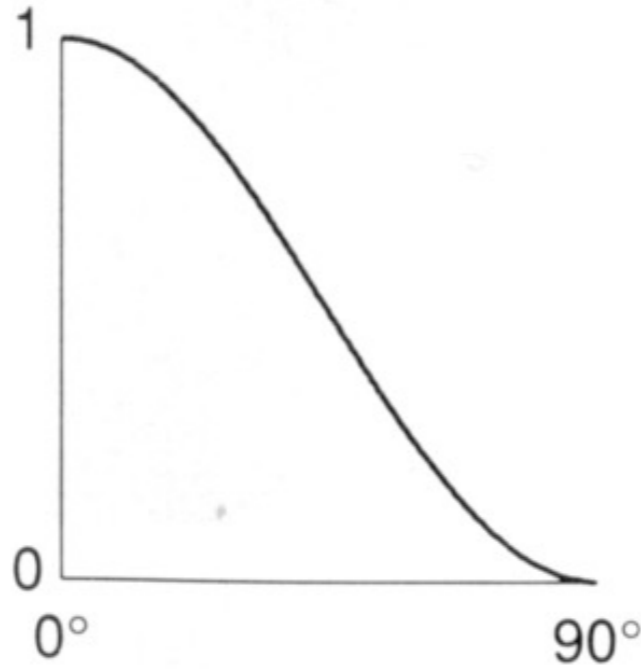


# Effect of $p$

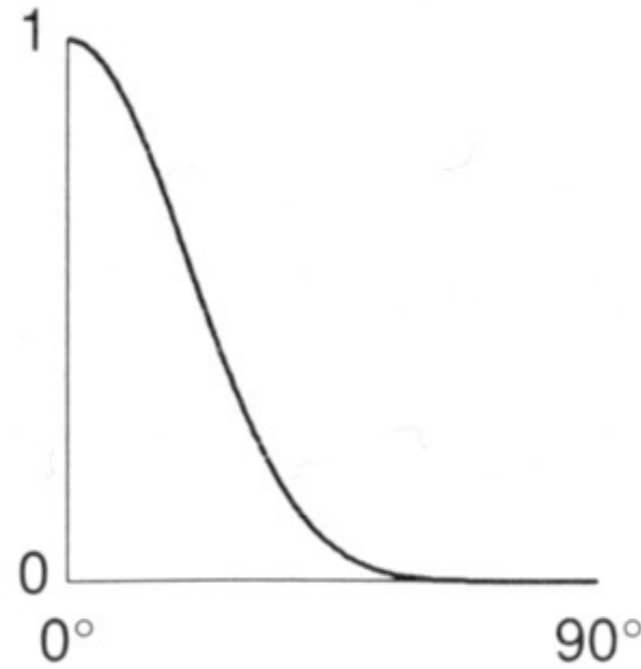
$\cos \alpha$



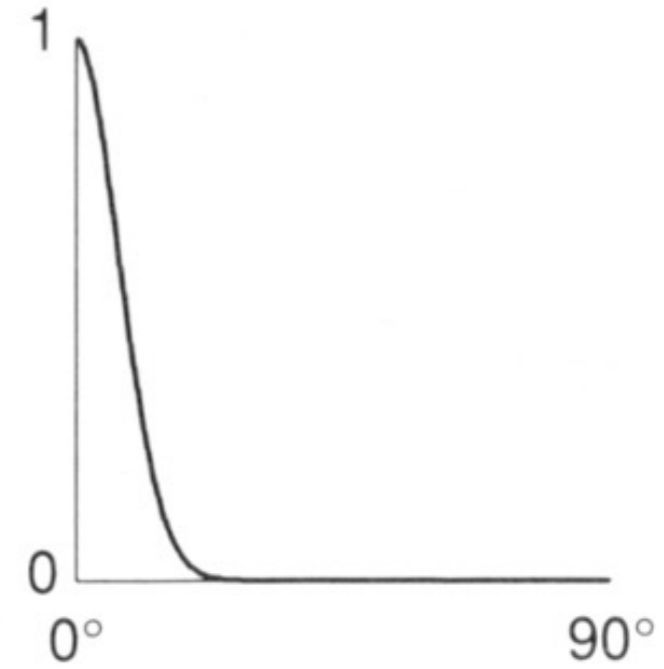
$\cos^2 \alpha$



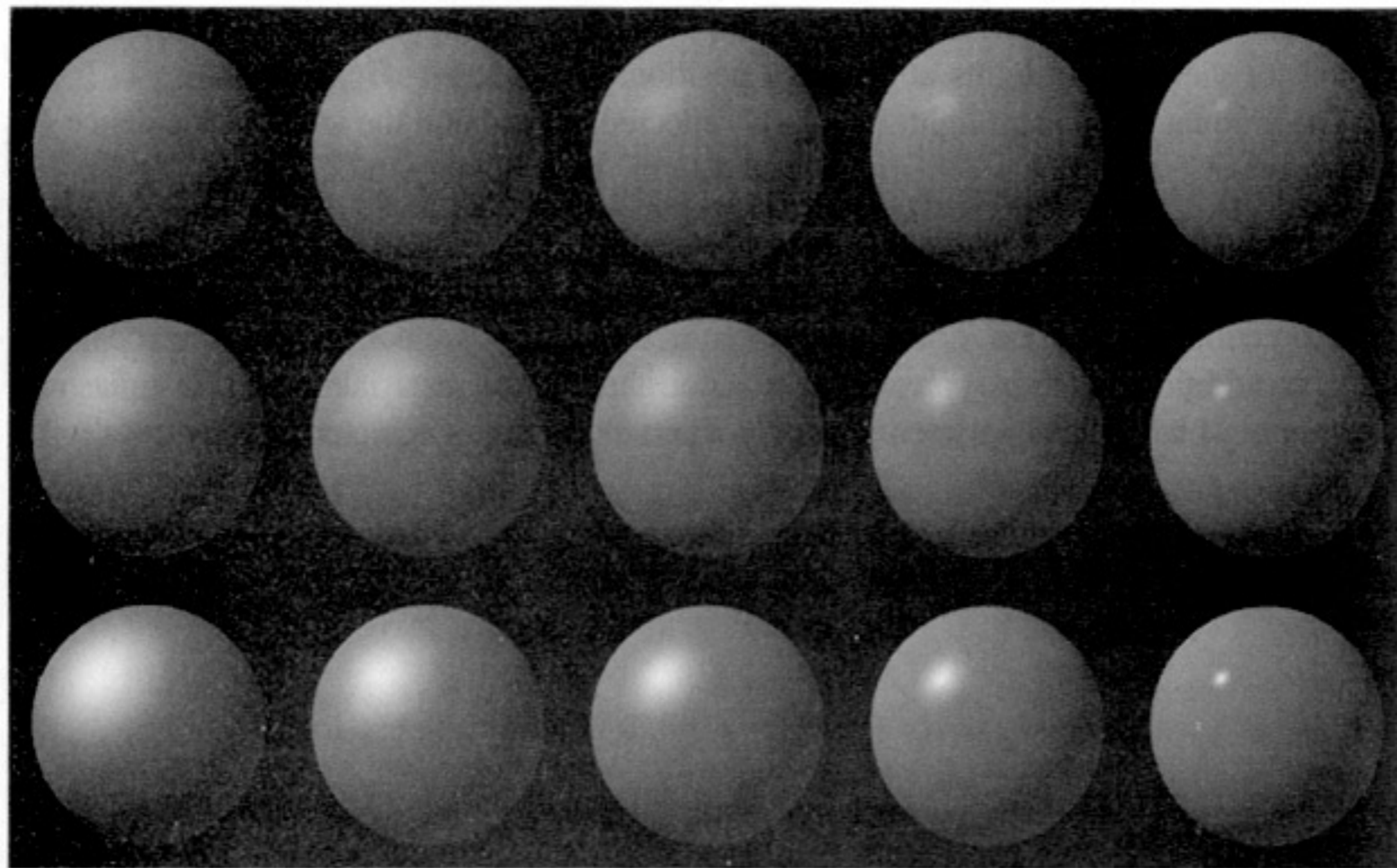
$\cos^8 \alpha$



$\cos^{64} \alpha$



$k_s$



$p$   $\longrightarrow$

# Putting it all Together: Blinn-Phong Reflection Model

Usually surfaces have both diffuse *and* specular components, so we'll combine the two:

light reflected

diffuse reflection      specular reflection

$$L = L_d + L_s$$

specular exponent  
(sharpness of specularity)

$$= k_d I \max(0, \vec{n} \cdot \vec{l}) + k_s I \max(0, \vec{n} \cdot \vec{h})^p$$

diffuse coefficient  
(surface brightness and color)

light intensity

normal

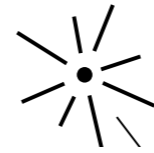
light direction

specular coefficient  
(strength [and color] of specularity)

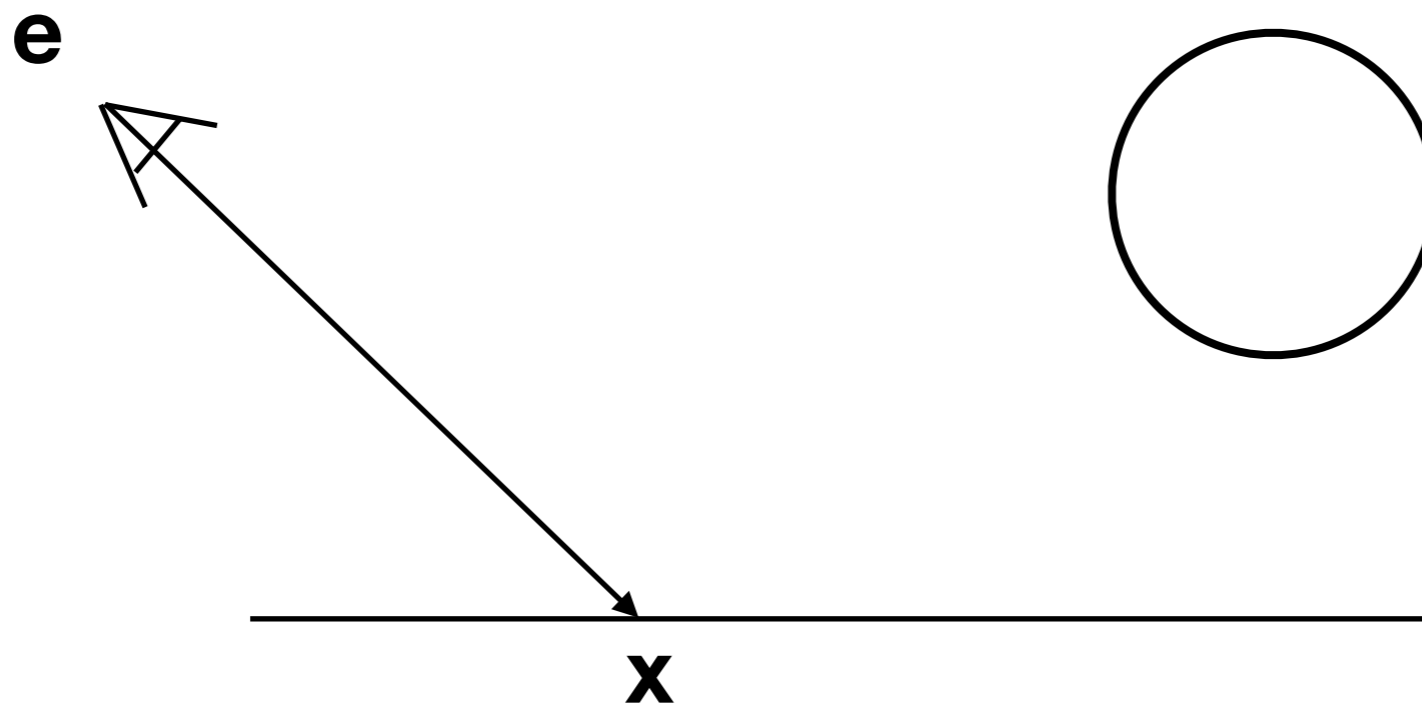
half-vector  
between  $\mathbf{l}$  and  $\mathbf{v}$

The diagram illustrates the Blinn-Phong reflection model equation. At the top, it shows the total light reflected  $L$  as the sum of diffuse reflection  $L_d$  and specular reflection  $L_s$ . Below this, the equation is expanded to  $L = k_d I \max(0, \vec{n} \cdot \vec{l}) + k_s I \max(0, \vec{n} \cdot \vec{h})^p$ . Arrows point from descriptive text to various parts of the equation:  $k_d$  is the diffuse coefficient (surface brightness and color);  $I$  is the light intensity;  $\vec{n}$  is the surface normal;  $\vec{l}$  is the light direction;  $k_s$  is the specular coefficient (strength and color of specularity);  $\vec{h}$  is the half-vector between the light direction  $\vec{l}$  and the view direction  $\vec{v}$ ; and  $p$  is the specular exponent (sharpness of specularity).

# Mirror Reflection



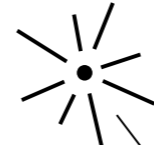
What does a camera see when it looks at a mirror?



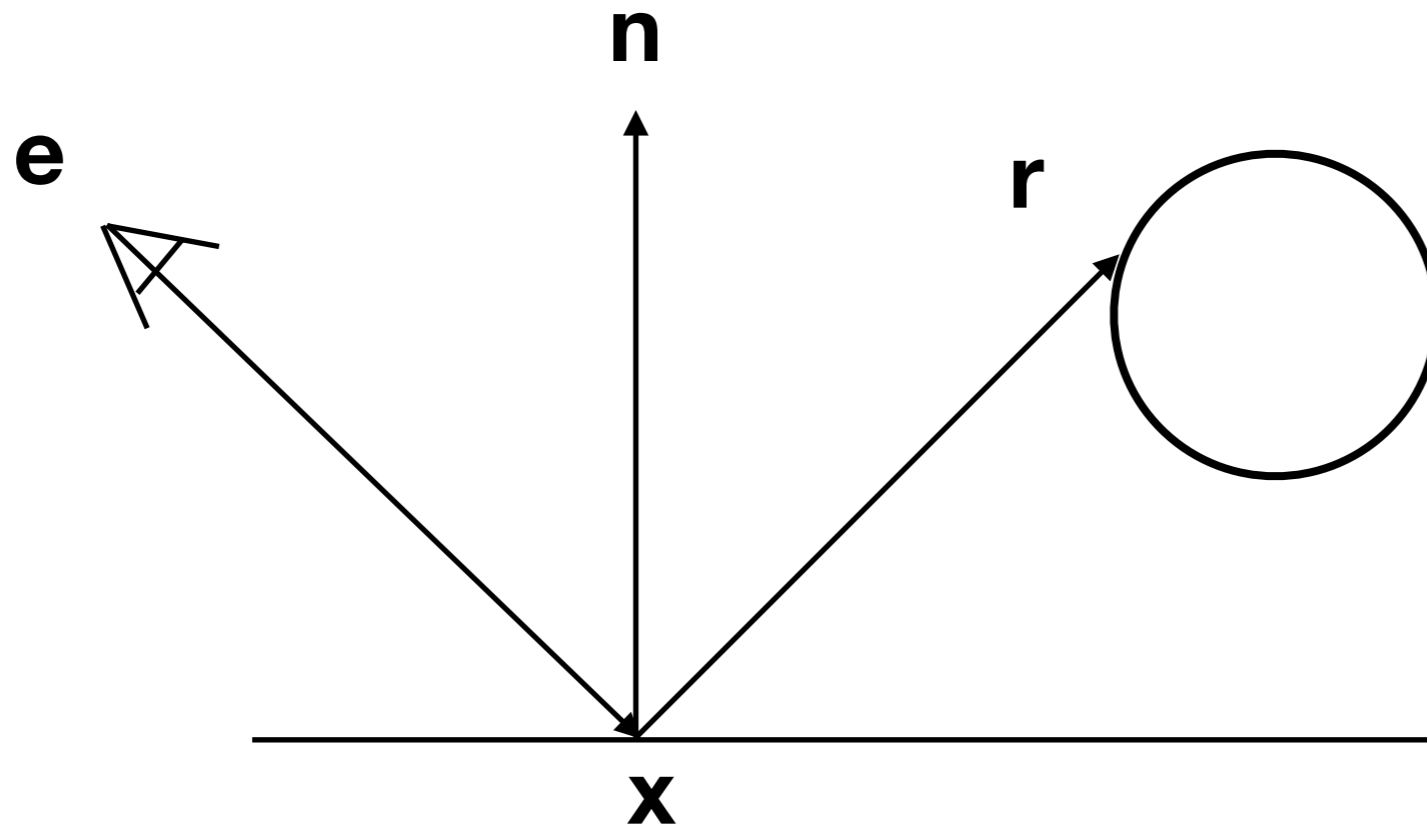
Can we do this using the tools we already have?

(Exercise 2)

# Mirror Reflection



What does a camera see when it looks at a mirror?

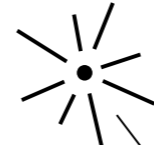


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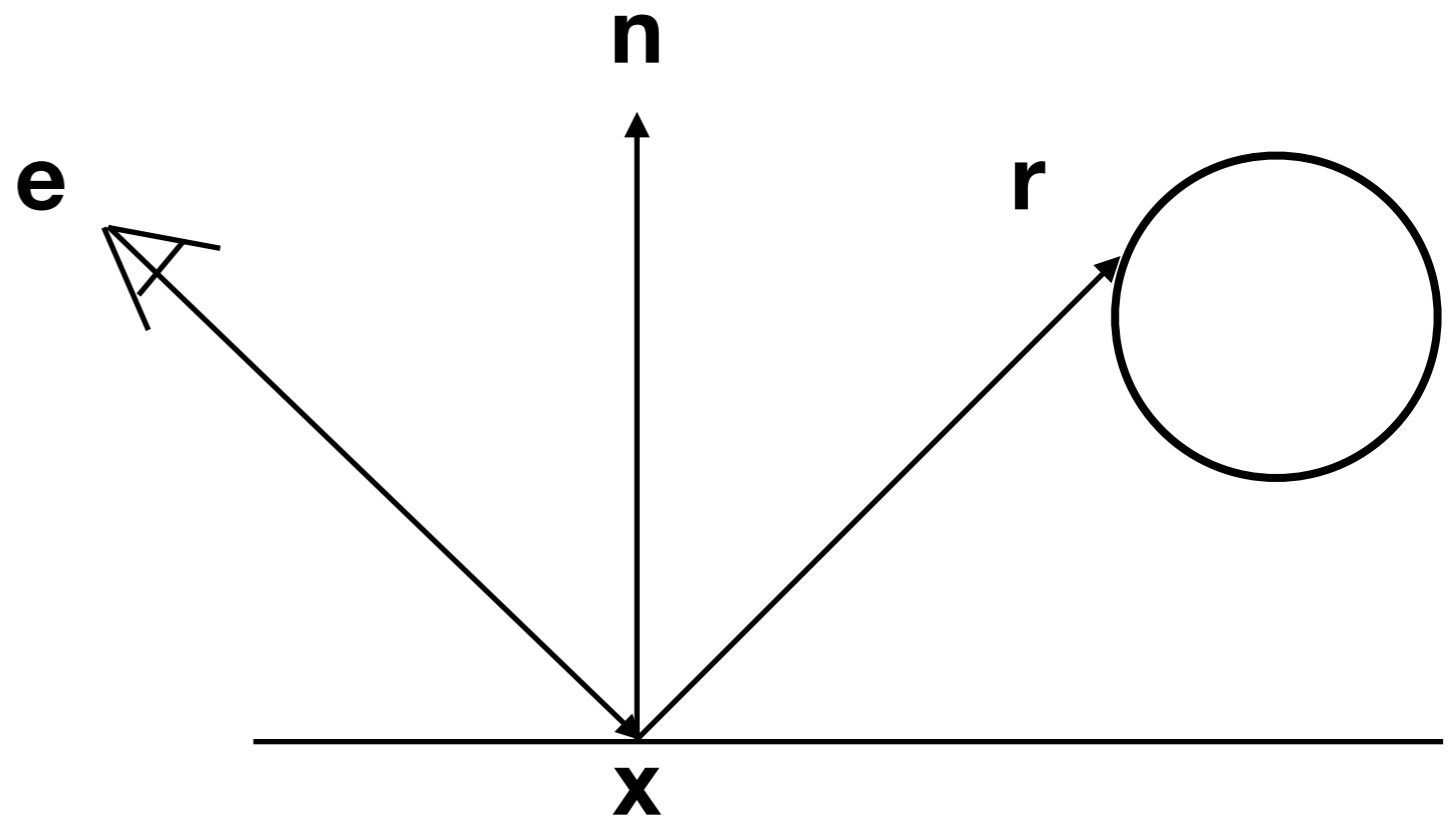
```
find_intersection(ray, scene)
```



# Mirror Reflection



What does a camera see when it looks at a mirror?



```
compute  $\mathbf{r}$ 
```

```
ray = Ray( $\mathbf{x}$ ,  $\mathbf{r}$ )
```

```
find_intersection(ray, scene)
```

# Recursion!?

```
traceray(ray, scene):  
    t, rec = find_intersection(ray, scene)  
    if rec.obj is a mirror:  
        compute r, the reflection direction  
        mirror_ray = Ray(rec.x, r)  
        return traceray(mirror_ray, scene)  
    # other cases, ...
```

# Mirror Coefficient

- Most surfaces aren't perfect mirrors. Object stores a *mirror coefficient*  $k_m$  between 0 and 1.
- "Local color" computed as usual
- "reflected color" computed recursively
- Final color:  $k_m * \text{reflected} + (1 - k_m) * \text{local}$