

CSCI 301 - Lecture 28: Parsing I

$$P \rightarrow \text{Stmt} ; \text{Stmts}$$

$$\text{Stmt} \rightarrow \text{if } \text{Cond} \{$$

$$\Sigma = \{0, 1, \dots, 9, +, -, *, /, (,)\}$$

$$E \rightarrow E + E$$

$$| E - E$$

$$| E * E$$

$$| E / E$$

$$| (E)$$

$$| 0 | 1 | 2 | \dots | 9$$

① $E \Rightarrow \underline{E} + E$

$$E + E * E$$

$$\underline{1} + E * E$$

$$1 + 1 * E$$

$$1 + 1 * 4$$

② $E \Rightarrow \underline{E} + E$

$$\Rightarrow 1 + \underline{E}$$

$$\Rightarrow 1 + \underline{E} * E$$

$$1 + 1 * \underline{E}$$

$$1 + 1 * 4$$

$$w = 1 + 1 * 4$$

left-most derivation

③ $E \Rightarrow E * \underline{E}$

$$E * 4$$

$$\underline{E} + E * 4$$

$$E + 1 * 4$$

$$\underline{1} + 1 * 4$$

④ $E \Rightarrow \underline{E} + E$

$$\Rightarrow E - E + E$$

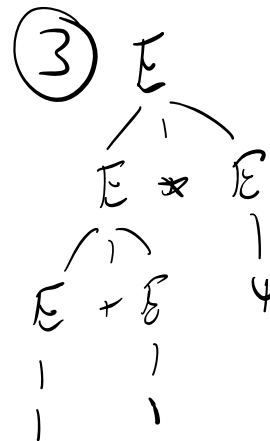
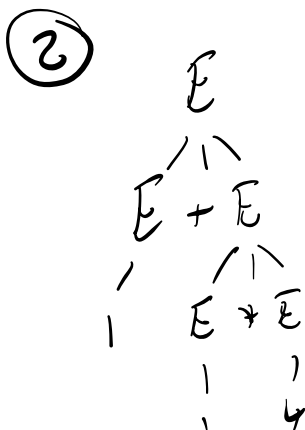
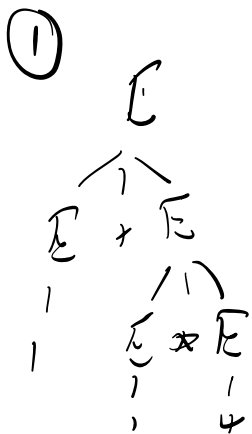
✗

right-most derivation

~~7 - 7~~

$$1 + 2$$

$$(7 * 4) + (6 / 2)$$



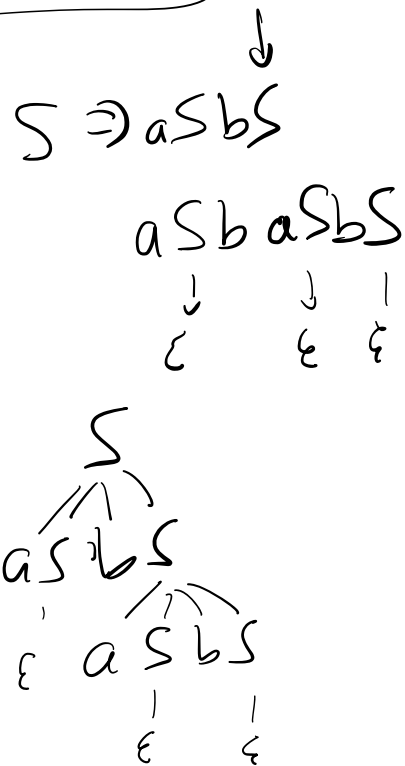
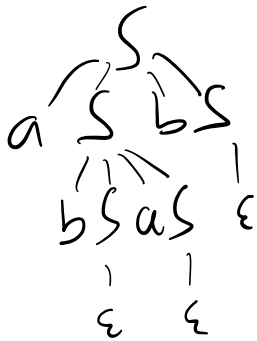
Def: A grammar is **ambiguous** if some string w has more than one parse tree.

Equivalently: A grammar is **ambiguous** if there is more than one left-most derivation for some string.

Ex. A $G_1:$
 $S \rightarrow \epsilon$
 $S \rightarrow aSa$
 $S \rightarrow bSb$

$G_2:$
 $S \rightarrow \epsilon$
 $S \rightarrow aSbS$
 $S \rightarrow bSaS$

$S \Rightarrow aSbS$
 $abSaaS$



Backtracking



top-down
 $S \Rightarrow \dots$

bottom-up
 $w \in \dots \in S$

$LL(k)$
 $LL(1)$

$LR(k)$
right-most
derivation

$LALR$
look-ahead
left to right
rightmost

left-to-right
leftmost derivation
1 token of lookahead
