CSCI 241

Scott Wehrwein

Dijkstra's Algorithm: Efficient Implementation

Goals

Be prepared to implement Dijkstra's algorithm efficiently.



```
S = \{ \}; F = \{v\}; v.d = 0; v.bp = null;
while (F \neq \{\})
  f = node in F with min d value;
  Remove f from F, add it to S;
  for each neighbor w of f {
    if (w not in S or F) {
        w.d = f.d + weight(f, w);
        w.bp = f;
        add w to F;
    \} else if (f.d+weight(f,w) < w.d) {
        w.d = f.d + weight(f,w);
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- 1. Store Frontier in a min-heap priority queue with d-values as priorities.
- 2. To efficiently iterate over neighbors, use an adjacency list graph representation.
- 3. To store w.d and w.bp, we will use a HashMap<Node,PathData>
- 4. We don't need to explicitly store Settled or Unexplored sets: a node is in S or F iff it is in the map.

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4. We don't need to explicitly store Settled or Unexplored sets: w is in S or $F \Leftrightarrow$ it is in the map.

The only time we need to check membership in S is **here**.

If w is not in S or F, it must be in Unexplored.

therefore, we haven't found a path to it.

therefore, it has no d or bp yet.

therefore, it isn't in the map!