

CSCI 241

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Quick Sort: Algorithm

Goals

Thoroughly understand the mechanism of
quicksort.

Be able to execute quicksort on paper.

Be prepared to implement quicksort and its
partition helper method.

Mergesort vs Quicksort

```
/** mergesort A[st..end]*/
mergeSort(A, st, end):
    if (small):
        return
```

mid = (end+st)/2

Divide

(Quick: the "real work" happens here)

```
mergeSort(A,st, mid)
mergeSort(A,mid,end)
```

Conquer

```
merge(A, st, mid, end)
```

Combine

(Merge: the "real work" happens here)

Mergesort vs Quicksort

```
/** mergesort A[st..end]*/
mergeSort(A, st, end):
    if (small):
        return

    mid = (end+st)/2
```

```
    mergeSort(A,st, mid)
    mergeSort(A,mid,end)
```

```
    merge(A, st, mid, end) # (nothing to do!)
```

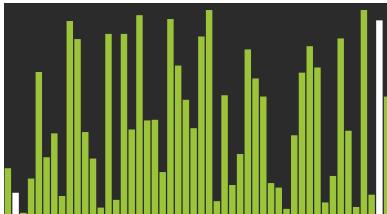
```
/** quicksort A[st..end]*/
quickSort(A, st, end):
    if (small):
        return
```

Divide `mid = partition(A,st,end)`

Conquer `quickSort(A,st,mid)`
 `quickSort(A,mid+1,end)`

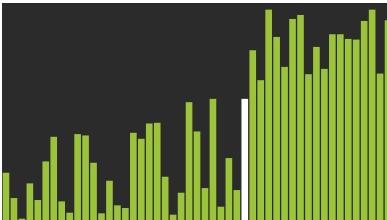
Quicksort: Algorithm

Unsorted:



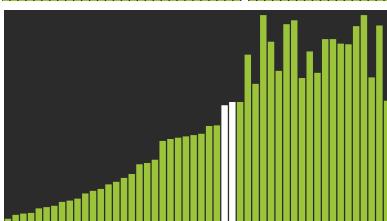
```
/** quicksort A[st..end]*/
quickSort(A, st, end):
    if (small):
        return
```

Small things left
big things right:



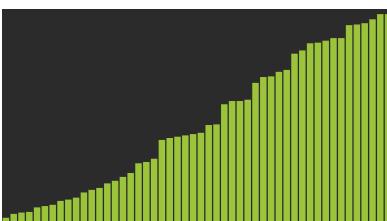
```
← mid = partition(A, st, end)
```

Sort left things:



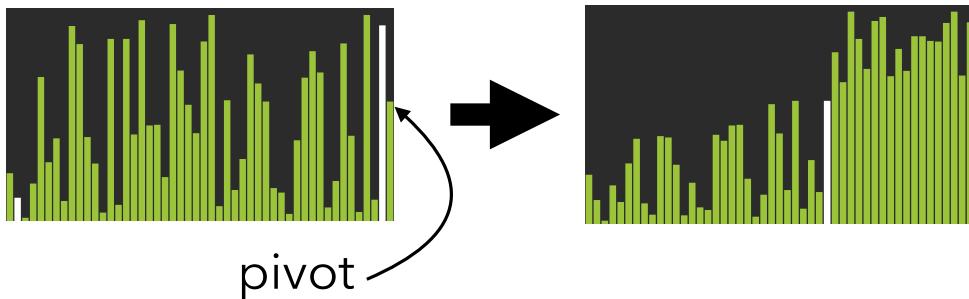
```
← quickSort(A, st, mid)
```

Sort right things:



```
← quickSort(A, mid+1, end)
```

Quicksort: Partition



partition: choose a **pivot**, then:

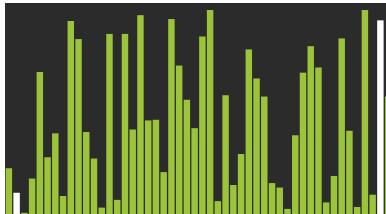
- elements \leq pivot go to its left
- elements $>$ pivot to the right

What pivot should we choose?

- First, middle, or last
- Median of first, middle, and last

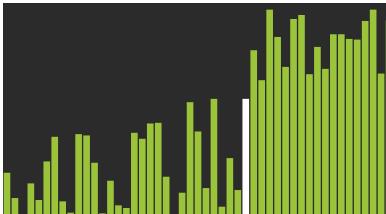
Quicksort: Algorithm

Unsorted:



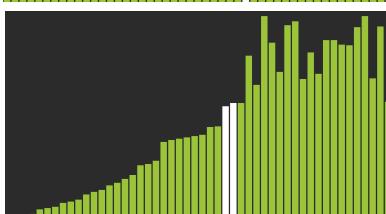
```
/** quicksort A[st..end]*/
quickSort(A, st, end):
    if (small):
        return
```

Small things left
big things right:



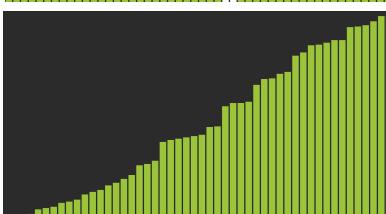
```
← mid = partition(A, st, end)
```

Sort left things:



```
← quickSort(A, st, mid)
```

Sort right things:



```
← quickSort(A, mid+1, end)
```

Tiny Example

`quickSort([2 8 9 1])`

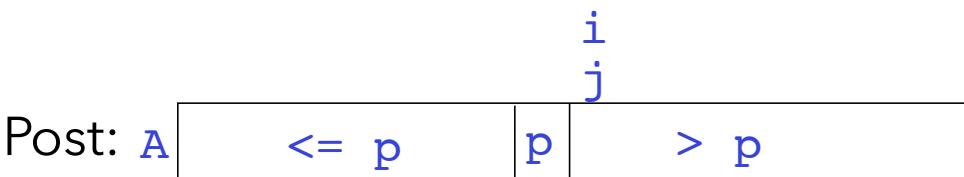
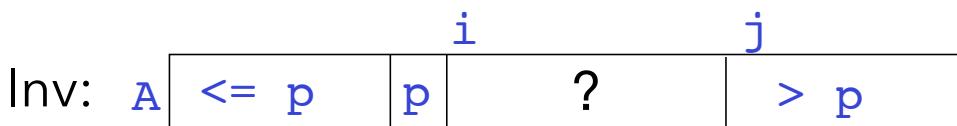
For now: choose the first element as the pivot.

[2 8 9 1]

[1 2 9 8]

[1 2 8 9]

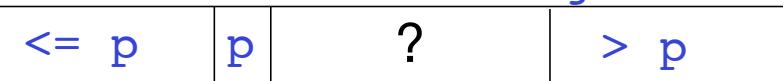
Quicksort: Partition



Quicksort: Partition

Pre: A  i j

A	p	?
---	---	---

Inv: A  i j

A	<= p	p	?	> p
---	------	---	---	-----

Post: A  i j

A	<= p	p	> p
---	------	---	-----

```
partition(A, start, end)
    initialize i, j
    choose pivot
    swap pivot to A[0]
    while [?] section != []
        # process A[i]:
        if <= p:
            grow <= p section
        else:
            grow > p section
```

Note: this is just one of several ways to implement partition.